

NDA MATHS MOCK TEST - 154 (SOLUTION)

1. (C) Let $\frac{x}{\cos\theta} = \frac{y}{\cos\left(\theta + \frac{\pi}{3}\right)} = \frac{z}{\cos\left(\theta - \frac{\pi}{3}\right)} = k$

$$x = k \cos\theta, y = k \cos\left(\theta + \frac{\pi}{3}\right), z = k \cos\left(\theta - \frac{\pi}{3}\right)$$

$$\text{Now, } y + z - x = k \cos\left(\theta + \frac{\pi}{3}\right) + k \cos\left(\theta - \frac{\pi}{3}\right) - k \cos\theta$$

$$\Rightarrow y + z - x = k \left[\cos\left(\theta + \frac{\pi}{3}\right) + \cos\left(\theta - \frac{\pi}{3}\right) - \cos\theta \right]$$

$$\Rightarrow y + z - x = k \left[2 \cos\theta \cos \frac{\pi}{3} - \cos\theta \right]$$

$$\Rightarrow y + z - x = k \left[2(\cos\theta) \times \frac{1}{2} - \cos\theta \right]$$

$$\Rightarrow y + z - x = k \times 0 = 0$$

2. (B) Let $y = \tan^{-1}\left(\frac{2\sqrt{x}}{1-x}\right)$

$$\text{Let } x = \tan^2\theta \Rightarrow \theta = \tan^{-1}\sqrt{x}$$

$$\Rightarrow y = \tan^{-1}\left(\frac{2 \tan\theta}{1 - \tan^2\theta}\right)$$

$$\Rightarrow y = \tan^{-1}(\tan 2\theta)$$

$$\Rightarrow y = 2\theta$$

$$\Rightarrow y = 2 \tan^{-1}\sqrt{x}$$

On differentiating both side w.r.t.'x'

$$\Rightarrow \frac{dy}{dx} = 2 \times \frac{1}{1+(\sqrt{x})^2} \times \frac{1}{2\sqrt{x}}$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{\sqrt{x}(1+x)}$$

3. (A) In ABC, $a = 2\sqrt{2}$, $b = 3$ and $C = 45^\circ$

$$\text{Now, } \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

$$\Rightarrow \cos 45 = \frac{(2\sqrt{2})^2 + (3)^2 - c^2}{2 \times 2\sqrt{2} \times 3}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{8+9-c^2}{12\sqrt{2}}$$

$$\Rightarrow 12 = 17 - c^2 \Rightarrow c = \sqrt{5}$$

4. (D) Given that $a = \frac{dy}{dx}$, $b = \frac{d^2y}{dx^2}$

$$y = f(x)$$

On differentiating both side w.r.t.'x'

$$\Rightarrow \frac{dy}{dx} = f'(x)$$

$$\Rightarrow \frac{dx}{dy} = \frac{1}{f'(x)}$$

Again, differentiating

$$\Rightarrow \frac{d^2x}{dy^2} \times \frac{dy}{dx} = -1[f'(x)]^{-2} f''(x)$$

$$\Rightarrow \frac{d^2x}{dy^2} \times a = -(a)^{-2} \times b$$

$$\Rightarrow \frac{d^2x}{dy^2} = \frac{-b}{a^3}$$

5. (D)

6. (C) $I = \int_0^{\pi/2} \frac{\sin x - \cos x}{1 + \sin x \cdot \cos x} dx$... (i)

$$\text{Prop. IV } \int_0^a f(x) dx = \int_0^a f(a-x) dx$$

$$I = \int_0^{\pi/2} \frac{\sin\left(\frac{\pi}{2}-x\right) - \cos\left(\frac{\pi}{2}-x\right)}{1 + \sin\left(\frac{\pi}{2}-x\right) \cdot \cos\left(\frac{\pi}{2}-x\right)} dx$$

$$I = \int_0^{\pi/2} \frac{\cos x - \sin x}{1 + \cos x \cdot \sin x} dx$$
 ... (ii)

from eq(i) and eq(ii)

$$2I = 0 \Rightarrow I = 0$$

7. (D) $\begin{vmatrix} ab - a^2 & a - b & b^2 - ab \\ bc - ac & c - a & ab - a^2 \\ b^2 - ab & b - c & bc - ac \end{vmatrix}$

$$\Rightarrow \begin{vmatrix} a(b-a) & a-b & b(b-a) \\ c(b-a) & c-a & a(b-a) \\ b(b-a) & b-c & c(b-a) \end{vmatrix}$$

$$\Rightarrow (b-a)^2 \begin{vmatrix} a & a-b & b \\ c & c-a & a \\ b & b-c & c \end{vmatrix}$$

$$C_2 \rightarrow C_2 + C_3 - C_1$$

$$\Rightarrow (b-a)^2 \begin{vmatrix} a & 0 & b \\ c & 0 & a \\ b & 0 & c \end{vmatrix} = 0$$

8. (B)
$$\left[\frac{\sin \frac{\pi}{4} - i \cos \frac{\pi}{4}}{\sin \frac{\pi}{4} + i \cos \frac{\pi}{4}} \right]^2$$

$$\Rightarrow \left[\frac{\frac{1}{\sqrt{2}} - i \times \frac{1}{\sqrt{2}}}{\frac{1}{\sqrt{2}} + i \times \frac{1}{\sqrt{2}}} \right]^2$$

$$\Rightarrow \left(\frac{1-i}{1+i} \right)^2$$

$$\Rightarrow \left[\frac{(1-i)^2}{2} \right]^2$$

$$\Rightarrow \left(\frac{-2i}{2} \right)^2$$

$$\Rightarrow i^2 = -1$$

9. (D) $I = \int \sin x \cdot \log(\sin x) dx$

$$I = \log(\sin x) \cdot \int \sin x dx - \int \left\{ \frac{d}{dx}(\log(\sin x)) \cdot \int \sin x dx \right\} dx$$

$$I = -\cos x \cdot \log(\sin x) - \int \frac{1}{\sin x} \times \cos x (-\cos x) dx$$

$$I = -\cos x \cdot \log(\sin x) + \int \frac{\cos^2 x}{\sin x} dx$$

$$I = -\cos x \cdot \log(\sin x) + \int \frac{(1 - \sin^2 x)}{\sin x} dx$$

$$I = -\cos x \cdot \log(\sin x) + \int (\operatorname{cosec} x - \sin x) dx$$

$$I = -\cos x \cdot \log(\sin x) + \log \left(\tan \frac{x}{2} \right) + \cos x + c$$

10. (B) $I = \int_0^{\pi/2} \frac{\sin x}{\sin x + \cos x} dx \quad \dots(i)$

Prop. IV

$$I = \int_0^{\pi/2} \frac{\sin \left(\frac{\pi}{2} - x \right)}{\sin \left(\frac{\pi}{2} - x \right) + \cos \left(\frac{\pi}{2} - x \right)} dx$$

$$I = \int_0^{\pi/2} \frac{\cos x}{\cos x + \sin x} dx \quad \dots(ii)$$

from eq(i) and eq(ii)

$$2I = \int_0^{\pi/2} \frac{\sin x + \cos x}{\sin x + \cos x} dx$$

$$2I = \int_0^{\pi/2} 1 dx$$

$$2I = [x]_0^{\pi/2}$$

$$2I = \frac{\pi}{2} - 0 \Rightarrow I = \frac{\pi}{4}$$

11. (C) $y = \tan^{-1} \left[\frac{\cos x - \sin x}{\cos x + \sin x} \right]$

$$y = \tan^{-1} \left[\frac{1 - \tan x}{1 + \tan x} \right]$$

$$y = \tan^{-1} \left[\frac{\tan \frac{\pi}{4} - \tan x}{1 + \tan \frac{\pi}{4} \cdot \tan x} \right]$$

$$y = \tan^{-1} \left[\tan \left(\frac{\pi}{4} - x \right) \right]$$

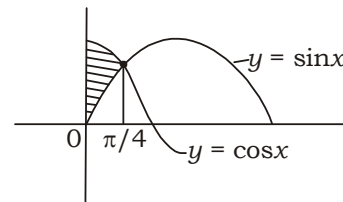
$$y = \frac{\pi}{4} - x$$

On differentiating both side w.r.t. 'x'

$$\frac{dy}{dx} = -1$$

12. (C)

13. (B)



$$\text{Area} = \int_0^{\pi/4} (\cos x - \sin x) dx$$

$$\text{Area} = [\sin x + \cos x]_0^{\pi/4}$$

$$\text{Area} = \sin \frac{\pi}{4} + \cos \frac{\pi}{4} - \sin 0 - \cos 0$$

$$\text{Area} = \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} - 0 - 1$$

$$\text{Area} = (\sqrt{2} - 1) \text{ sq. unit}$$

14. (C) $A = \{1, 3, 4, 5\}$, $B = \{2, 3, 4, 6\}$ and $C = \{x, y\}$

$$(A \cap B) = \{3, 4\}$$

$$\text{Now, } (A \cap B) \times C = \{3, 4\} \times \{x, y\}$$

$$\text{No. of elements in } (A \cap B) \times C = 2 \times 2 = 4$$

15. (B) The required Probability = $\frac{{}^5C_1 \times {}^8C_2}{{}^{13}C_3}$

$$= \frac{5 \times 28}{13 \times 22}$$

$$= \frac{70}{143}$$

16. (C) $z = \frac{3+2i}{2-3i} - \frac{2-3i}{3+2i}$

$$z = \frac{(3+2i)(2+3i)}{(2-3i)(2+3i)} - \frac{(2-3i)(3-2i)}{(3+2i)(3-2i)}$$

$$z = \frac{13i}{4-9i^2} - \frac{-13i}{9-4i^2}$$

$$z = \frac{13i}{13} + \frac{13i}{13}$$

$z = i + i = 2i$ and $\bar{z} = -2i$

Now, $z^2 + z\bar{z} = z(z + \bar{z})$

$\Rightarrow z^2 + z\bar{z} = 2i(2i - 2i) = 0$

17. (D) Digits 0, 1, 3, 5, 7, 8

$\boxed{3 \ 6 \ 6 \ 6} = 3 \times 6 \times 6 \times 6 = 648$

(5, 7, 8)

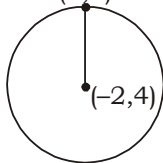
18. (C) Given that $b_{xy} = \frac{-13}{8}$ and $b_{yx} = \frac{-2}{13}$

Now, $r = \sqrt{b_{xy} \times b_{yx}}$

$\Rightarrow r = \sqrt{\left(\frac{-13}{8}\right) \times \left(\frac{-2}{13}\right)}$

$\Rightarrow r = \sqrt{\frac{1}{4}} = \frac{-1}{2}$

19. (C) (0, 0)



Equation of circle

$x^2 + y^2 + 4x - 8y = 0$

$\Rightarrow (x+2)^2 - 4 + (y-4)^2 - 16 = 0$

$\Rightarrow (x+2)^2 + (y-4)^2 = 20$

Equation of diameter

$y - 0 = \frac{4-0}{-2-0}(x-0)$

$y = -2x \Rightarrow 2x + y = 0$

20. (D) Given that $\vec{a} = 3\hat{i} - \hat{j} - 2\hat{k}$ and $\vec{b} = \hat{i} + \hat{j} - 2\hat{k}$

Now, $(\vec{a} + 2\vec{b}) \times (2\vec{a} - \vec{b})$

$\Rightarrow 2(\vec{a} \times \vec{a}) + 4(\vec{b} \times \vec{a}) - (\vec{a} \times \vec{b}) - 2(\vec{b} \times \vec{b})$

$\Rightarrow 0 - 4(\vec{a} \times \vec{b}) - (\vec{a} \times \vec{b}) - 0 = -5(\vec{a} \times \vec{b})$

21. (B) $f(x) = e^{\sin(\log \sin x)}$

On differentiating both sides w.r.t. 'x'

$f'(x) = e^{\sin(\log \sin x)} \times \cos(\log \sin x) \times \frac{\cos x}{\sin x}$

$f'(x) = \cot x \cdot \cos(\log \sin x) \cdot e^{\sin(\log \sin x)}$

$f'\left(\frac{\pi}{2}\right) = \cot \frac{\pi}{2} \cdot \cos\left(\log \sin \frac{\pi}{2}\right) \cdot e^{\sin\left(\log \sin \frac{\pi}{2}\right)}$

$f'\left(\frac{\pi}{2}\right) = 0 \cdot \cos(\log 1) \cdot e^{\sin(\log 1)}$

$f'\left(\frac{\pi}{2}\right) = 0 \cdot \cos 0 \cdot e^{\sin 0}$

$f'\left(\frac{\pi}{2}\right) = 0 \times 1 \times 1 = 0$

22. (C) $\log_5(5 \cdot 3^x - 13)$, $\log_5(3^x - 1)$ and $\log_5 2$ are in A.P.,

then $2 \log_5(3^x - 1) = \log_5(5 \cdot 3^x - 13) + \log_5 2$

$\Rightarrow \log_5(3^x - 1)^2 = \log_5\{(5 \cdot 3^x - 13) \times 2\}$

$\Rightarrow (3^x - 1)^2 = 2(5 \cdot 3^x - 13)$

$\Rightarrow (3^x)^2 + 1 - 2 \cdot 3^x = 10 \cdot 3^x - 26$

$\Rightarrow (3^x)^2 - 12 \cdot 3^x + 27 = 0$

$\Rightarrow (3^x - 9)(3^x - 3) = 0$

$\Rightarrow 3^x - 9 = 0 \Rightarrow 3^x = 3^2 \Rightarrow x = 2$

and $3^x - 3 = 0 \Rightarrow 3^x = 3^1 \Rightarrow x = 1$

Hence $x = 1, 2$

23. (B) The required Probability

$= \frac{{}^6C_3 + {}^6C_4 + {}^6C_5 + {}^6C_6}{2^6}$

$= \frac{20 + 15 + 6 + 1}{64}$

$= \frac{42}{64} = \frac{21}{32}$

24. (A) $\begin{vmatrix} 1+c & 1 & 1 \\ 1 & 1+a & 1 \\ 1 & 1 & 1+b \end{vmatrix} = k$

$\Rightarrow (1+c)[(1+a)(1+b) - 1] - 1(1+b-1) + 1(1-1-a) = k$

$\Rightarrow (1+c)(a+b+ab) - b - a = k$

$\Rightarrow a + ac + b + bc + ab + abc - a - b = k$

$\Rightarrow ac + bc + ab + abc = k$

$\Rightarrow \frac{ac + bc + ab + abc}{abc} = \frac{k}{abc}$

$\Rightarrow b^{-1} + a^{-1} + c^{-1} + 1 = \frac{k}{abc}$

$\Rightarrow 0 + 1 = \frac{k}{abc}$

$\Rightarrow k = abc$ [$\because a^{-1} + b^{-1} + c^{-1} = 0$]

25. (C) Circle $x^2 + y^2 - 2x - 6y + 15 = 0$

Equation of circle concentric with given circle

$x^2 + y^2 - 2x - 6y + c = 0$... (i)

its passing through (-1, 4)

$(-1)^2 + (4)^2 - 2 \times (-1) - 6 \times 4 + c = 0$

$\Rightarrow 1 + 16 + 2 - 24 + c = 0 \Rightarrow c = 5$

from eq(i)

Equation of circle

$\Rightarrow x^2 + y^2 - 2x - 6y + 5 = 0$

26. (D) Angle describe in 12 hr by hour-hand = 360°
 Angle describe in 1 hr(60 min) by hour-hand = $\frac{360}{12}$
 Angle describe in 1 min by hour-hand = $\frac{360}{12 \times 60}$
 Angle describe in 24 min by hour-hand = $\frac{360}{12 \times 60} \times 24 = 12^\circ$

27. (C) We know that
 curve $\sqrt{x} + \sqrt{y} = \sqrt{a}$

$$\text{Area} = \frac{a^2}{b}$$

$$\text{Given that } \sqrt{x} + \sqrt{y} = \sqrt{3}$$

$$\text{The required area} = \frac{3^2}{6} = \frac{3}{2} \text{ sq. unit}$$

28. (C) Let $A = \begin{bmatrix} 1 & -3 & -2 \\ 4 & 0 & 5 \\ 1 & 2 & -1 \end{bmatrix}$

Co-factors of A

$$C_{11} = (-1)^{1+1} \begin{vmatrix} 0 & 5 \\ 2 & -1 \end{vmatrix}, C_{12} = (-1)^{1+2} \begin{vmatrix} 4 & 5 \\ 1 & -1 \end{vmatrix}, C_{13} = (-1)^{1+3} \begin{vmatrix} 4 & 0 \\ 1 & 2 \end{vmatrix}$$

$$= -10 \quad = -(-4 - 5) = 9 \quad = 8 - 0 = 8$$

$$C_{21} = (-1)^{2+1} \begin{vmatrix} -3 & -2 \\ 2 & -1 \end{vmatrix}, C_{22} = (-1)^{2+2} \begin{vmatrix} 1 & -2 \\ 1 & -1 \end{vmatrix}, C_{23} = (-1)^{2+3} \begin{vmatrix} 1 & -3 \\ 1 & 2 \end{vmatrix}$$

$$= -(3 + 4) = -7 \quad = -1 + 2 = 1 \quad = -(2 + 3) = -5$$

$$C_{31} = (-1)^{3+1} \begin{vmatrix} 3 & -2 \\ 0 & 5 \end{vmatrix}, C_{32} = (-1)^{3+2} \begin{vmatrix} 1 & -2 \\ 4 & 5 \end{vmatrix}, C_{33} = (-1)^{3+3} \begin{vmatrix} 1 & -3 \\ 4 & 0 \end{vmatrix}$$

$$= -15 = -15 \quad = -(5 + 8) = -13 \quad = 0 + 12 = 12$$

$$C = \begin{bmatrix} -10 & 9 & 8 \\ -7 & 1 & -5 \\ -15 & -13 & 12 \end{bmatrix}, C^T = \begin{bmatrix} -10 & -7 & -15 \\ 9 & 1 & -13 \\ 8 & -5 & 12 \end{bmatrix}$$

$$\text{Adj } A = C^T$$

$$\text{Adj } A = \begin{bmatrix} -10 & -7 & -15 \\ 9 & 1 & -13 \\ 8 & -5 & 12 \end{bmatrix}$$

29. (B) $A = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$

$$A^2 = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 4 & 4 \\ 4 & 4 \end{bmatrix} = \begin{bmatrix} 4 & 4 \\ 4 & 4 \end{bmatrix}$$

$$\text{Similarly } A^3 = \begin{bmatrix} 2^3 & 2^3 \\ 2^3 & 2^3 \end{bmatrix}$$

$$\text{and } A^4 = \begin{bmatrix} 2^4 & 2^4 \\ 2^4 & 2^4 \end{bmatrix} = \begin{bmatrix} 16 & 16 \\ 16 & 16 \end{bmatrix}$$

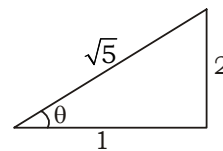
30. (C) $a^{1/3} - \frac{1}{a^{1/3}} = 4$

$$\Rightarrow \left(a^{1/3} - \frac{1}{a^{1/3}} \right)^3 = 4^3$$

$$\Rightarrow a - \frac{1}{a} - 3 \times a = 64$$

$$\Rightarrow a - \frac{1}{a} = 64 + 12 = 76$$

31. (D)



$$\sin^{-1} \left(\frac{2}{\sqrt{5}} \right) = \theta$$

$$\Rightarrow \sin \theta = \frac{2}{\sqrt{5}}$$

$$\text{Now, } \sec \theta = \sqrt{5}$$

$$\Rightarrow \sec^{-1}(\sqrt{5}) = \theta$$

32. (A) $I = \int_{-1}^1 x^2 |x| dx$

$$I = \int_{-1}^0 x^2 |x| dx + \int_0^1 x^2 |x| dx$$

$$I = - \int_{-1}^0 x^3 dx + \int_0^1 x^3 dx$$

$$I = - \left[\frac{x^4}{4} \right]_{-1}^0 + \left[\frac{x^4}{4} \right]_0^1$$

$$I = \frac{-1}{4} [0 - (-1)^4] + \frac{1}{4} [1^4 - 0]$$

$$I = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

33. (B) The no. of ways = ${}^{15-1}C_{11-1}$
 $= {}^{14}C_{10} = 1001$

34. (C) $n = 25$

$$\begin{aligned} \text{No. of diagonals} &= \frac{n(n-3)}{2} \\ &= \frac{25 \times 23}{2} = 275 \end{aligned}$$

35. (B) zero

36. (C) Let $a - ib = \sqrt{5 - 12i}$

On squaring

$$\Rightarrow (a^2 - b^2) - (2ab)i = 5 - 12i$$

On comparing

$$a^2 - b^2 = 5 \text{ and } 2ab = 12 \quad \dots(i)$$

$$\text{Now, } (a^2 + b^2)^2 = (a^2 - b^2)^2 + (2ab)^2$$

$$\Rightarrow (a^2 + b^2)^2 = 5^2 + (12)^2$$

$$\Rightarrow (a^2 + b^2)^2 = 13 \Rightarrow a^2 + b^2 = 13 \quad \dots(iii)$$

On solving eq(i) and eq(ii)

$$2a^2 = 18 \text{ and } 2b^2 = 8$$

$$\Rightarrow a = \pm 3 \quad b = \pm 2$$

$$\text{Hence } \sqrt{5 - 12i} = \pm(3 - 2i)$$

37. (D) Given that $P(A) = \frac{2}{5}$, $P(B) = \frac{1}{2}$ and

$$P\left(\frac{A}{B}\right) = \frac{3}{4}$$

$$\text{Now, } P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$\Rightarrow \frac{3}{4} = \frac{P(A \cap B)}{1/2}$$

$$\Rightarrow P(A \cap B) = \frac{3}{4} \times \frac{1}{2} = \frac{3}{8}$$

$$\text{and } P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$

$$\Rightarrow P\left(\frac{B}{A}\right) = \frac{3/8}{2/5} = \frac{15}{16}$$

38. (C) $\begin{bmatrix} 3 & -2 \\ x & -1 \end{bmatrix} \times \begin{bmatrix} -2 & 6 \\ 2 & 5 \end{bmatrix} = \begin{bmatrix} -10 & y \\ -4 & 1 \end{bmatrix}$

$$\Rightarrow \begin{bmatrix} -6 - 4 & 18 - 10 \\ -2x - 2 & 6x - 5 \end{bmatrix} = \begin{bmatrix} -10 & y \\ -4 & 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} -10 & 8 \\ -2x - 2 & 6x - 5 \end{bmatrix} = \begin{bmatrix} -10 & y \\ -4 & 1 \end{bmatrix}$$

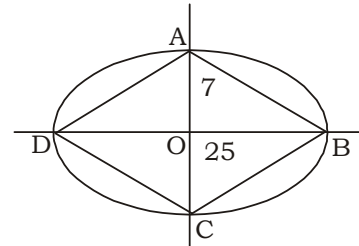
On comparing

$$-2x - 2 = -4 \text{ and } y = 8$$

$$\Rightarrow x = 1$$

$$\text{Hence } x = 1 \text{ and } y = 8$$

39. (A)



$$\text{Given that } e = \frac{24}{25}$$

$$\text{and } 2ae = 48$$

$$\Rightarrow 2a \times \frac{24}{25} = 48 \Rightarrow a = 25$$

$$\text{Now, } b^2 = a^2(1 - e^2)$$

$$\Rightarrow b^2 = 25 \times 25 \left(1 - \frac{24}{25} \times \frac{24}{25}\right)$$

$$\Rightarrow b^2 = 25 \times 25 \times \frac{49}{25 \times 25} \Rightarrow b = 7$$

$$\text{Area of } \triangle AOB = \frac{1}{2} \times OA \times OB$$

$$= \frac{1}{2} \times 7 \times 25$$

$$\text{Area of } ABCD = 4 \times \text{Area of } \triangle AOB$$

$$= 4 \times \frac{1}{2} \times 7 \times 25 = 350 \text{ sq. unit}$$

40. (D) $(\sqrt{3} - 2i)(2 + \sqrt{3}i)$

$$\Rightarrow 2\sqrt{3} - 4i + 3i - 2\sqrt{3}i^2$$

$$\Rightarrow 4\sqrt{3} - i$$

41. (C) Planes $-2x + y + 4z = 7$ and $-4x + 2y - z = 8$

$$\text{Now, } \cos\theta = \frac{(-2) \times (-4) + 1 \times 2 + 4 \times (-1)}{\sqrt{(-2)^2 + 1^2 + 4^2} \sqrt{(-4)^2 + 2^2 + (-1)^2}}$$

$$\Rightarrow \cos\theta = \frac{8 + 2 - 4}{\sqrt{21}\sqrt{21}}$$

$$\Rightarrow \cos\theta = \frac{6}{21}$$

$$\Rightarrow \cos\theta = \frac{2}{7} \Rightarrow \theta = \cos^{-1}\left(\frac{2}{7}\right)$$

42. (A) $\frac{\sin A}{\sin C} = \frac{\sin(A-B)}{\sin(B-C)}$

$$\Rightarrow \frac{\sin A}{\sin C} = \frac{\sin A \cdot \cos B - \cos A \cdot \sin B}{\sin B \cdot \cos C - \cos B \cdot \sin C}$$

$$\Rightarrow \frac{a}{c} = \frac{a \cos B - b \cos A}{b \cos C - c \cos B} \quad [\text{by Sine Rule}]$$

$$\Rightarrow ab \cos C - ac \cos B = ac \cos B - bc \cos A$$

$$\Rightarrow ab \cos C + bc \cos A = 2ac \cos B$$

$$\Rightarrow ab \times \frac{a^2 + b^2 - c^2}{2ab} + bc \times \frac{b^2 + c^2 - a^2}{2bc}$$

$$= 2ac \times \frac{a^2 + c^2 - b^2}{2ac}$$

$$\Rightarrow \frac{a^2 + b^2 - c^2}{2} + \frac{b^2 + c^2 - a^2}{2} = a^2 + c^2 - b^2$$

$$\Rightarrow b^2 = a^2 + c^2 - b^2$$

$$\Rightarrow 2b^2 = a^2 + c^2$$

Hence a^2, b^2, c^2 are in A.P.

43. (B) In the expansion of $\left(2\sqrt{x} + \frac{1}{4x^{3/2}}\right)^6$

$$T_{r+1} = {}^6C_r (2\sqrt{x})^{6-r} \left(\frac{1}{4x^{3/2}}\right)^r$$

$$T_{r+1} = {}^6C_r (2)^{6-3r} x^{\frac{6-4r}{2}}$$

Here, $\frac{6-4r}{2} = 1$

$$\Rightarrow 6-4r=2 \Rightarrow r=1$$

Coefficient of $x = {}^6C_1 (2)^3$
 $= 6 \times 8 = 48$

44. (B) $\begin{vmatrix} b+c & b^2+c^2 & k \\ c+a & c^2+a^2 & k \\ a+b & a^2+b^2 & k \end{vmatrix} = (a-b)(b-c)(c-a)$

$$\Rightarrow k \begin{vmatrix} b+c & b^2+c^2 & 1 \\ c+a & c^2+a^2 & 1 \\ a+b & a^2+b^2 & 1 \end{vmatrix} = (a-b)(b-c)(c-a)$$

$R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_1$

$$\Rightarrow k \begin{vmatrix} b+c & b^2+c^2 & 1 \\ a-b & a^2-b^2 & 0 \\ a-c & a^2-c^2 & 0 \end{vmatrix} = (a-b)(b-c)(c-a)$$

$$\Rightarrow k(a-b)(a-c) \begin{vmatrix} b+c & b^2+c^2 & 1 \\ 1 & a+b & 0 \\ 1 & a+c & 0 \end{vmatrix}$$

$$= -(a-b)(b-c)(a-c)$$

$$\Rightarrow k \begin{vmatrix} b+c & b^2+c^2 & 1 \\ 1 & a+b & 0 \\ 1 & a+c & 0 \end{vmatrix} = -(b-c)$$

$R_3 \rightarrow R_3 - R_2$

$$\Rightarrow k \begin{vmatrix} b+c & b^2+c^2 & 1 \\ 1 & a+b & 0 \\ 0 & c-b & 0 \end{vmatrix} = c-b$$

$$\Rightarrow k(c-b) \begin{vmatrix} b+c & b^2+c^2 & 1 \\ 1 & a+b & 0 \\ 0 & 1 & 0 \end{vmatrix} = (c-b)$$

$$\Rightarrow k[(b+c) \times 0 - (b^2+c^2) \times 0 + 1 \times 1] = 1$$

$$\Rightarrow k \times 1 = 1 \Rightarrow k = 1$$

45. (C) $f(x) = \sqrt{1 + \sin^2 x^2}$

$$f'(x) = \frac{1}{2} \times \frac{1}{\sqrt{1 + \sin^2 x^2}} \times 2 \sin x^2 \cdot \cos x^2 \times 2x$$

$$f'(x) = \frac{2x \sin x^2 \cdot \cos x^2}{\sqrt{1 + \sin^2 x^2}}$$

$$f'\left(\frac{\sqrt{\pi}}{2}\right) = \frac{2 \times \frac{\sqrt{\pi}}{2} \sin \frac{\pi}{4} \cdot \cos \frac{\pi}{4}}{\sqrt{1 + \sin^2 \frac{\pi}{4}}}$$

$$f'\left(\frac{\sqrt{\pi}}{2}\right) = \frac{\sqrt{\pi} \times \frac{1}{\sqrt{2}} \times \frac{1}{\sqrt{2}}}{\sqrt{1 + \frac{1}{2}}}$$

$$f'\left(\frac{\sqrt{\pi}}{2}\right) = \frac{\frac{\sqrt{\pi}}{2}}{\sqrt{\frac{3}{2}}} = \frac{\sqrt{\pi}}{\sqrt{6}}$$

46. (D) 10101

$$\begin{array}{l} \rightarrow 1 \times 2^0 = 1 \\ \rightarrow 0 \times 2^1 = 0 \\ \rightarrow 1 \times 2^2 = 4 \\ \rightarrow 0 \times 2^3 = 0 \\ \rightarrow 1 \times 2^4 = 16 \\ \hline 21 \end{array}$$

$$\begin{array}{l} 0.11 \\ \leftarrow \frac{1}{2} = 1 \times 2^{-1} \\ \leftarrow \frac{1}{4} = 1 \times 2^{-2} \\ \hline \frac{1}{2} + \frac{1}{4} = \frac{3}{4} = 0.75 \end{array}$$

Hence $(10101.11)_2 = (21.75)_{10}$

47. (A) $I = \int \frac{1}{x(x^3-1)} dx$

$$I = \int \frac{x^2}{x^3(x^3-1)} dx$$

Let $x^3 = t$

$$\Rightarrow 3x^2 dx = dt \Rightarrow x^2 dx = \frac{1}{3} dt$$

$$I = \int \frac{1}{3} \times \frac{dt}{t(t-1)}$$

$$I = \frac{1}{3} \int \left(\frac{1}{t-1} - \frac{1}{t} \right) dt$$

$$I = [\log(t-1) - \log t] + c$$

$$I = \frac{1}{3} \log \left(\frac{t-1}{t} \right) + c$$

$$I = \frac{1}{3} \log \left(\frac{x^3-1}{x^3} \right) + c$$

48. (C) Let $y = \log_{10}(5x^2-7)$
On differentiating both side w.r.t.'x'

$$\frac{dy}{dx} = \frac{1}{5x^2-7} \times 5 \times 2x$$

$$\frac{dy}{dx} = \frac{10x}{5x^2-7}$$

49. (B) $\frac{\cos 5x - 2\cos 4x + \cos 3x}{\sin 5x - \sin 3x}$

$$\Rightarrow \frac{\cos 5x + \cos 3x - 2\cos 4x}{\sin 5x - \sin 3x}$$

$$\Rightarrow \frac{2\cos 4x \cdot \cos x - 2\cos 4x}{2\cos 4x \cdot \sin x}$$

$$\Rightarrow \frac{2\cos 4x(\cos x - 1)}{2\cos 4x \cdot \sin x}$$

$$\Rightarrow \frac{-(1 - \cos x)}{\sin x}$$

$$\Rightarrow \frac{-2\sin^2 \frac{x}{2}}{2\sin \frac{x}{2} \cdot \cos \frac{x}{2}} = -\tan \frac{x}{2}$$

50. (A) **Statement I**
 $n = 12$

$$\text{The required sum} = \frac{n}{6} (n+1)(2n+1)$$

$$= \frac{12}{6} (12+1)(2 \times 12+1)$$

$$= 2 \times 13 \times 25 = 650$$

Statement I is correct.

Statement II

$$n = 7$$

$$\text{The required sum} = \left[\frac{n(n+1)}{2} \right]^2$$

$$= \left[\frac{7(7+1)}{2} \right]^2$$

$$= \left(\frac{7 \times 8}{2} \right)^2 = 784$$

Statement II is incorrect.

51. (C) The required Probability = $\frac{4}{52} = \frac{1}{13}$

52. (D) $\lim_{x \rightarrow 5} \frac{\sqrt{5x-5}}{\sqrt{2x-1}-3}$ $\left[\frac{0}{0} \right]$ form

by L-Hospital's Rule

$$\Rightarrow \lim_{x \rightarrow 5} \frac{\frac{1}{2}(5x)^{-1/2} \times 5 - 0}{\frac{1}{2}(2x-1)^{-1/2} \times 2 - 0}$$

$$\Rightarrow \lim_{x \rightarrow 5} \frac{\frac{5}{2} \times \frac{1}{\sqrt{5x}}}{\frac{1}{\sqrt{2x-1}}}$$

$$\Rightarrow \lim_{x \rightarrow 5} \frac{5\sqrt{2x-1}}{2\sqrt{5x}}$$

$$\Rightarrow \frac{5\sqrt{2 \times 5 - 1}}{2\sqrt{5 \times 5}} = \frac{5 \times 3}{2 \times 5} = \frac{3}{2}$$

53. (C) Probability of Kapil's selection $P(k) = \frac{3}{4}$

$$\text{and } P(\bar{k}) = 1 - \frac{3}{4} = \frac{1}{4}$$

$$\text{Probability of Sumit's selection } P(s) = \frac{1}{3}$$

$$P(\bar{s}) = 1 - \frac{1}{3} = \frac{2}{3}$$

Probability of one of them is selected

$$= \frac{3}{4} \times \frac{2}{3} + \frac{1}{4} \times \frac{1}{3}$$

$$= \frac{6}{12} + \frac{1}{12} = \frac{7}{12}$$

54. (C)

55. (B) Let $\vec{x} = a\hat{i} + b\hat{j} + c\hat{k}$

$$\text{Now, } (\vec{x} \cdot \hat{i}) \hat{i} = [(a\hat{i} + b\hat{j} + c\hat{k}) \cdot \hat{i}] \hat{i}$$

$$= [a] \hat{i} = a\hat{i}$$

$$\text{Similarly } (\vec{y} \cdot \hat{j}) \hat{j} = b\hat{j}$$

$$\text{and } (\vec{z} \cdot \hat{k}) \hat{k} = z\hat{k}$$

$$\text{Now, } (x \cdot \hat{i}) \hat{i} + (\vec{x} \cdot \hat{j}) \hat{j} + (\vec{x} \cdot \hat{k}) \hat{k}$$

$$\Rightarrow a\hat{i} + b\hat{j} + c\hat{k} = \vec{x}$$

56. (C) **Statement I**

For any three coplanar vectors \vec{x}, \vec{y} and \vec{z} ,

$$(\vec{x} \times \vec{y}) \cdot \vec{z} = 0$$

Statement I is correct.

Statement II

$$\text{L.H.S} = \vec{x} \cdot \{(\vec{y} + \vec{z}) \times (\vec{x} + \vec{y} + \vec{z})\}$$

$$= \vec{x} \cdot \{\vec{y} \times \vec{x} + \vec{y} \times \vec{y} + \vec{y} \times \vec{z} + \vec{z} \times \vec{x} + \vec{z} \times \vec{y} + \vec{z} \times \vec{z}\}$$

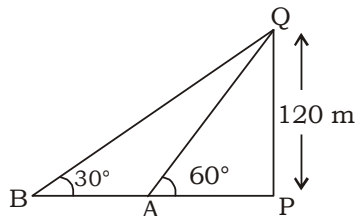
$$= \vec{x} \cdot \{\vec{y} \times \vec{x} + \vec{y} \times \vec{z} + \vec{z} \times \vec{x} - \vec{y} \times \vec{z}\}$$

$$= \vec{x} \cdot (\vec{y} \times \vec{x}) + \vec{x} \cdot (\vec{z} \times \vec{x})$$

$$= 0 + 0 = 0 = \text{R.H.S.}$$

Statement II is correct.

57. (A)



In ΔAPQ :-

$$\tan 60^\circ = \frac{PQ}{AP}$$

$$\Rightarrow \sqrt{3} = \frac{120}{AP} \Rightarrow AP = \frac{120}{\sqrt{3}}$$

In ΔBPQ :-

$$\tan 30^\circ = \frac{PQ}{BP}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{120}{AB + AP}$$

$$\Rightarrow AB + AP = 120\sqrt{3}$$

$$\Rightarrow AB + \frac{120}{\sqrt{3}} = 120\sqrt{3}$$

$$\Rightarrow AB = 120\left(\sqrt{3} - \frac{1}{\sqrt{3}}\right) \Rightarrow AB = 80\sqrt{3}$$

Distance between both trees = $80\sqrt{3}$ m

58. (B) Let $y = f(x) = \sqrt{x + \sqrt{x + \sqrt{x + \dots}}}$

$$\Rightarrow y = \sqrt{x + y}$$

On squaring

$$\Rightarrow y^2 = x + y$$

On differentiating both side w.r.t.'x'

$$\Rightarrow 2y \frac{dy}{dx} = 1 + \frac{dy}{dx}$$

$$\Rightarrow (2y - 1) \frac{dy}{dx} = 1$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{2y - 1}$$

$$\Rightarrow f'(x) = \frac{1}{2f(x) - 1}$$

59. (C) $\sin^2 \frac{\pi}{5} + \sin^2 \frac{2\pi}{5} + \sin^2 \frac{3\pi}{5} + \sin^2 \frac{4\pi}{5}$

$$\Rightarrow \sin^2 \frac{\pi}{5} + \sin^2 \frac{2\pi}{5} + \sin^2 \left(\pi - \frac{2\pi}{5}\right) +$$

$$\sin^2 \left(\pi - \frac{\pi}{5}\right)$$

$$\Rightarrow \sin^2 \frac{\pi}{5} + \sin^2 \frac{2\pi}{5} + \sin^2 \frac{2\pi}{5} + \sin^2 \frac{\pi}{5}$$

$$\Rightarrow 2 \left(\sin^2 \frac{\pi}{5} + \sin^2 \frac{2\pi}{5} \right)$$

$$\Rightarrow 2 \left[\left(\frac{\sqrt{10 - 2\sqrt{5}}}{4} \right)^2 + \left(\frac{\sqrt{10 + 2\sqrt{5}}}{4} \right)^2 \right]$$

$$\Rightarrow 2 \left[\frac{10 - 2\sqrt{5}}{16} + \frac{10 + 2\sqrt{5}}{16} \right]$$

$$\Rightarrow 2 \times \frac{20}{16} = \frac{5}{2}$$

60. (C) $\frac{(n+2)! + (n+1)(n-1)!}{(n+1)(n-1)!}$

$$\Rightarrow \frac{(n+2)(n+1)n(n-1)! + (n+1)(n-1)!}{(n+1)(n-1)!}$$

$$\Rightarrow \frac{(n+1)(n-1)![(n+2)n+1]}{(n+1)(n-1)!}$$

$$\Rightarrow n^2 + 2n + 1 = (n+1)^2$$

61. (B) $\int e^x \left[\frac{x^2 + x + 1}{(x+1)^2} \right] dx$

$$\Rightarrow \int e^x \left[\frac{x(x+1)+1}{(x+1)^2} \right] dx$$

$$\Rightarrow \int e^x \left[\frac{x}{x+1} + \frac{1}{(x+1)^2} \right] dx$$

$$\Rightarrow e^x \times \frac{x}{x+1} + c \Rightarrow \frac{x \cdot e^x}{x+1} + c$$

62. (D) In ΔABC , $\frac{1}{b+c} + \frac{1}{a+b} = \frac{3}{a+b+c}$

$$\Rightarrow \frac{a+b+b+c}{(b+c)(a+b)} = \frac{3}{a+b+c}$$

$$\Rightarrow \frac{a+2b+c}{(b+c)(a+b)} = \frac{3}{a+b+c}$$

$$\Rightarrow (a+2b+c)(a+b+c) = 3(b+c)(a+b)$$

$$\Rightarrow a^2+ab+ac+2ab+2b^2+2bc+ac+bc+c^2 = 3(ab+b^2+ca+bc)$$

$$\Rightarrow a^2+2b^2+c^2+3ab+2ac+3bc = 3ab+3b^2+3ca+3bc$$

$$\Rightarrow a^2+c^2-b^2 = ac$$

$$\Rightarrow \frac{a^2+c^2-b^2}{2ac} = \frac{1}{2}$$

$$\Rightarrow \cos B = \cos \frac{\pi}{3} \Rightarrow B = \frac{\pi}{3}$$

63. (C) A leap year = 366 days
= 52 weeks and 2 days

The required Probability = $\frac{2}{7}$

64. (C) $\cos(\tan^{-1}x) = \cos \left[\cos^{-1} \left(\frac{1}{\sqrt{1+x^2}} \right) \right]$

$$\cos(\tan^{-1}x) = \frac{1}{\sqrt{1+x^2}}$$

65. (C) $\frac{1}{ab}$, $\frac{1}{bc}$ and $\frac{1}{ca}$ are in A.P., then

$$\frac{2}{bc} = \frac{1}{ab} + \frac{1}{ca}$$

$$\Rightarrow \frac{2}{bc} = \frac{c+b}{abc} \Rightarrow 2a = b+c$$

Hence b , a and c are in A.P.

66. (B) $\sin^{-1} \left(\cos \left(\cos^{-1} \left(\sin \frac{7\pi}{4} \right) \right) \right)$

$$\Rightarrow \sin^{-1} \left(\cos \left(\cos^{-1} \left(\sin \left(2\pi - \frac{\pi}{4} \right) \right) \right) \right)$$

$$\Rightarrow \sin^{-1} \left(\cos \left(\cos^{-1} \left(-\sin \frac{\pi}{4} \right) \right) \right)$$

$$\Rightarrow \sin^{-1} \left(\cos \left(\cos^{-1} \left(-\frac{1}{\sqrt{2}} \right) \right) \right) \Rightarrow \sin^{-1} \left(-\frac{1}{\sqrt{2}} \right)$$

$$\Rightarrow \sin^{-1} \left(\sin \left(-\frac{\pi}{4} \right) \right) \Rightarrow -\frac{\pi}{4}$$

67. (D) Differential equation

$$\frac{dy}{dx} + 2xy = (\tan x) e^{-x^2}$$

On comparing with general equation

$$P = 2x \text{ and } Q = (\tan x) e^{-x^2}$$

I.F. = $e^{\int P dx}$

I.F. = $e^{\int 2x dx}$

I.F. = e^{x^2}

Solution of the differential equation

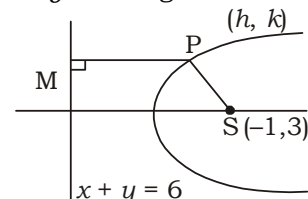
$$y \times \text{I.F.} = \int Q \times \text{I.F.} dx$$

$$\Rightarrow y \times e^{x^2} = \int (\tan x) e^{-x^2} \times e^{x^2} dx$$

$$\Rightarrow y \times e^{x^2} = \int \tan x dx$$

$$\Rightarrow y \cdot e^{x^2} = \log \sec x + c$$

68. (C)



Now, $PS = PM$

$$\Rightarrow \sqrt{(h+1)^2 + (k-3)^2} = \frac{h+k-6}{\sqrt{1^2+1^2}}$$

On squaring

$$\Rightarrow h^2 + 1 + 2h + k^2 + 9 - 6h = \frac{h^2 + k^2 + 36 + 2hk - 12k - 12h}{2}$$

On solving

$$\Rightarrow h^2 + k^2 - 2hk + 16h = 16$$

Equation of parabola

$$x^2 + y^2 - 2xy + 16x = 16$$

69. (D) We know that

$$(1+x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$$

On putting $x = 1$

$$\Rightarrow (1+1)^n = C_0 + C_1 + C_2 + \dots + C_n = 2^n$$

Hence $C_0 + C_1 + C_2 + \dots + C_n = 2^n$

70. (C) $y^{1/4} = x - \sqrt{1+x^2}$

$$\Rightarrow y = (x - \sqrt{1+x^2})^4 \quad \dots(i)$$

On differentiating both side w.r.t. 'x'

$$\Rightarrow \frac{dy}{dx} = 4(x - \sqrt{1+x^2})^3 \left[1 - \frac{1 \times 2x}{2\sqrt{1+x^2}} \right]$$

$$\Rightarrow y_1 = 4(x - \sqrt{1+x^2})^3 \left(\frac{\sqrt{1+x^2} - x}{\sqrt{1+x^2}} \right)$$

$$\Rightarrow y_1 = \frac{-4(x - \sqrt{1+x^2})^4}{\sqrt{1+x^2}}$$

$$\Rightarrow \sqrt{1+x^2} y_1 = -4y \quad \dots(ii) \text{ [from eq(i)]}$$

Again differentiating

$$\Rightarrow \sqrt{1+x^2} y_2 + y_1 \times \frac{1}{2} \times \frac{1 \times 2x}{\sqrt{1+x^2}} = -4y_1$$

$$\Rightarrow (1+x^2)y_2 + xy_1 = -4y_1\sqrt{1+x^2}$$

$$\Rightarrow (1+x^2)y_2 + xy_1 = -4 \times (-4y) \text{ [from eq(ii)]}$$

$$\Rightarrow (1+x^2)y_2 + xy_1 = 16y$$

71. (B) Given that $a = 12, b = 20, c = 16$

$$\begin{aligned} \text{Now, } \cos B &= \frac{a^2 + c^2 - b^2}{2ac} \\ \Rightarrow \cos B &= \frac{(12)^2 + (16)^2 - (20)^2}{2 \times 12 \times 16} \\ \Rightarrow \cos B &= \frac{144 + 256 - 400}{2 \times 12 \times 16} \\ \Rightarrow \cos B &= 0 \Rightarrow B = 90^\circ \\ \text{Now, } \sin A &= \sin 90 = 1 \end{aligned}$$

72. (C) $\frac{1 - 3 \tan^2 A}{3 \tan A - \tan^3 A}$

$$\Rightarrow \frac{1 - 3 \tan^2 \frac{17\pi}{4}}{3 \tan \frac{17\pi}{4} - \tan^3 \frac{17\pi}{4}} \quad \left[\because A = \frac{17\pi}{4} \right]$$

$$\Rightarrow \frac{1 - 3 \tan^2 \left(4\pi + \frac{\pi}{4} \right)}{3 \tan \left(4\pi + \frac{\pi}{4} \right) - \tan^3 \left(4\pi + \frac{\pi}{4} \right)}$$

$$\Rightarrow \frac{1 - 3 \tan^2 \frac{\pi}{4}}{3 \tan \frac{\pi}{4} - \tan^3 \frac{\pi}{4}}$$

$$\Rightarrow \frac{1 - 3 \times 1}{3 \times 1 - 1^3} = \frac{-2}{2} = -1$$

73. (B) Given that $X = \begin{bmatrix} -1 & 2 \\ 0 & -4 \end{bmatrix}, A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ and

$$B = \begin{bmatrix} 1 & -10 \\ -3 & 6 \end{bmatrix}$$

Now, $AX = B$

$$\Rightarrow \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} -1 & 2 \\ 0 & -4 \end{bmatrix} = \begin{bmatrix} 1 & -10 \\ -3 & 6 \end{bmatrix}$$

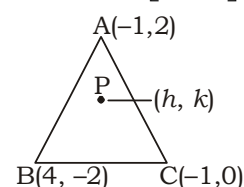
$$\Rightarrow \begin{bmatrix} -a & 2a - 4b \\ -c & 2c - 4d \end{bmatrix} = \begin{bmatrix} 1 & -10 \\ -3 & 6 \end{bmatrix}$$

On comparing

$$\begin{aligned} -a &= 1, & 2a - 4b &= -10 \\ \Rightarrow a &= -1, & 2 \times (-1) - 4b &= -10 \Rightarrow b = 2 \\ -c &= -3, & 2c - 4d &= 6 \\ \Rightarrow c &= 3, & 2 \times 3 - 4d &= 6 \Rightarrow d = 0 \end{aligned}$$

$$\text{Hence } A = \begin{bmatrix} -1 & 2 \\ 3 & 0 \end{bmatrix}$$

74. (B)



Let P is circumcentre,
then $AP = BP = CP$

Now, $AP = BP$

$$\Rightarrow \sqrt{(h+1)^2 + (k-2)^2} = \sqrt{(h-4)^2 + (k+2)^2}$$

On squaring

$$\Rightarrow h^2 + 1 + 2h + k^2 + 4 - 4k = h^2 + 16 - 8h + k^2 + 4 + 4k$$

$$\Rightarrow 10h - 8k = 15 \quad \dots(i)$$

$$\Rightarrow \sqrt{(h+1)^2 + (k-2)^2} = \sqrt{(h+1)^2 + k^2}$$

On squaring

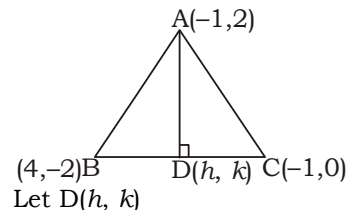
$$\begin{aligned} \Rightarrow h^2 + 1 + 2h + k^2 + 4 - 4k &= h^2 + 1 + 2h + k^2 \\ \Rightarrow 4 - 4k &= 0 \Rightarrow k = 1 \quad \dots(ii) \end{aligned}$$

from eq(i)

$$10h - 8 = 15 \Rightarrow h = \frac{23}{10}$$

$$\text{Hence circumcentre } P = \left(\frac{23}{10}, 1 \right)$$

75. (B)



$$\text{Slope of } BC = \frac{0 + 2}{-1 - 4} = \frac{-2}{5}$$

$$\text{Slope of } DC = \frac{-k}{-1 - h} = \frac{k}{1 + h}$$

$$\text{Slope of } AD = \frac{k - 2}{h + 1}$$

A.T.Q.

Slope of $BC =$ Slope of DC

$$\Rightarrow \frac{-2}{5} = \frac{k}{1 + h}$$

$$\Rightarrow 2h + 5k = -2 \quad \dots(i)$$

$$\Rightarrow \frac{-2}{5} \times \frac{k - 2}{h + 1} = -1$$

$$\Rightarrow 5h - 2k = -9 \quad \dots(ii)$$

$$\text{On solving eq(i) and eq(ii)}$$

$$h = \frac{-49}{29}, k = \frac{8}{29}$$

$$\text{Hence } H = \left(\frac{-49}{29}, \frac{8}{29} \right)$$

76. (D) Centroid of $\Delta ABC = \left(\frac{-1 + 4 - 1}{3}, \frac{2 - 2 + 0}{3} \right)$

$$= \left(\frac{2}{3}, 0 \right)$$

77. (B) $(A \cap B) \cup (B \cap C)$

78. (C) $S_n = n^2 + n - 7$

$$S_{n-1} = (n-1)^2 + (n-1) - 7$$

$$S_{n-1} = n^2 - n - 7$$

Now, $T_n = S_n - S_{n-1}$

$$\Rightarrow T_n = (n^2 + n - 7) - (n^2 - n - 7)$$

$$\Rightarrow T_n = 2n$$

$$\Rightarrow T_{21} = 2 \times 21 = 42$$

79. (C) $\log_{10}\left(\frac{3}{4}\right) - \log_{10}\left(\frac{81}{32}\right) + \log_{10}\left(\frac{27}{8}\right)$

$$\Rightarrow \log_{10}\left(\frac{\frac{3}{4} \times \frac{27}{8}}{\frac{81}{32}}\right)$$

$$\Rightarrow \log_{10}\left(\frac{81}{32} \times \frac{32}{81}\right) = \log_{10} 1 = 0$$

80. (C)

81. (D) **Statement I**

We know that

$$\cos^2\alpha + \cos^2\beta + \cos^2\gamma = 1$$

Statement I is incorrect.

Statement II

We know that

$$\cos^2\alpha + \cos^2\beta + \cos^2\gamma = 1$$

$$\Rightarrow \frac{\cos 2\alpha + 1}{2} + \frac{\cos 2\beta + 1}{2} + \frac{\cos 2\gamma + 1}{2} = 1$$

$$\Rightarrow \cos 2\alpha + 1 + \cos 2\beta + 1 + \cos 2\gamma + 1 = 2$$

$$\Rightarrow \cos 2\alpha + \cos 2\beta + \cos 2\gamma = -1$$

Statement II is incorrect.

82. (D) $9! \times C(17, 9) = k.P(17, 8)$

$$\Rightarrow 9! \times \frac{17!}{9!8!} = k \times \frac{17!}{9!}$$

$$\Rightarrow \frac{1}{8!} = k \times \frac{1}{9!}$$

$$\Rightarrow \frac{1}{8!} = \frac{k}{9 \times 8!} \Rightarrow k = 9$$

83. (D) $A = \tan^{-1}3$ and $B = \tan^{-1}2$

We know that

$$A + B + C = \pi$$

$$\Rightarrow \tan^{-1}3 + \tan^{-1}2 + c = \pi$$

$$\Rightarrow \tan^{-1}\left(\frac{3+2}{1-3 \times 2}\right) + c = \pi$$

$$\Rightarrow \tan^{-1}\left(\frac{5}{-5}\right) + c = \pi$$

$$= \frac{3\pi}{4} + c = \pi \Rightarrow c = \frac{\pi}{4}$$

84. (B) A.T.Q

$$a + 45d = 147 \quad \dots(i)$$

$$a + 146d = 46 \quad \dots(ii)$$

On solving eq(i) and eq(ii)

$$a = 192, d = -1$$

Now, Let nth term is zero

$$\Rightarrow a + (n-1)d = 0$$

$$\Rightarrow 192 + (n-1) \times (-1) = 0$$

$$\Rightarrow 192 = n-1 \Rightarrow n = 193$$

85. (B) $\log(a + \sqrt{1+a^2}) + \log\left(\frac{1}{a + \sqrt{1+a^2}}\right)$

$$\Rightarrow \log(a + \sqrt{1+a^2}) - \log(a + \sqrt{1+a^2})$$

$$\Rightarrow 0$$

86. (C) Let $\vec{a} = 3\hat{i} + \hat{j} + \hat{k}$ and $\vec{b} = 4\hat{i} + \hat{k}$

For option (C)

$$\text{Let } \vec{c} = \frac{\hat{i} + \hat{j} - 4\hat{k}}{3\sqrt{2}}$$

A.T.Q.

$$\vec{a} \cdot \vec{c} = \frac{3+1-4}{3\sqrt{2}} = 0$$

$$\text{and } \vec{b} \cdot \vec{c} = \frac{4-4}{3\sqrt{2}} = 0$$

$$\text{The required unit vector} = \frac{\hat{i} + \hat{j} - 4\hat{k}}{3\sqrt{2}}$$

87. (B) $A + B + C = \pi$

$$\Rightarrow B = \pi - (A + C)$$

Now, $\cos B = \cos(A + C)$

$$\Rightarrow \cos[\pi - (A + C)] = \cos A \cdot \cos C$$

$$\Rightarrow -\cos(A + C) = \cos A \cdot \cos C$$

$$\Rightarrow -\cos A \cdot \cos C + \sin A \cdot \sin C = \cos A \cdot \cos C$$

$$\Rightarrow \sin A \cdot \sin C = 2\cos A \cdot \cos C$$

$$\Rightarrow \tan A \cdot \tan C = 2$$

88. (B) Differential equation

$$\frac{dy}{dx} = \frac{1+y^2}{1+x^2}$$

$$\Rightarrow \frac{dy}{1+y^2} = \frac{dx}{1+x^2}$$

On integrating

$$\Rightarrow \int \frac{dy}{1+y^2} = \int \frac{dx}{1+x^2}$$

$$\Rightarrow \tan^{-1}y = \tan^{-1}x + \tan^{-1}c$$

$$\Rightarrow \tan^{-1}y - \tan^{-1}x = \tan^{-1}c$$

$$\Rightarrow \tan^{-1}\left(\frac{y-x}{1+xy}\right) = \tan^{-1}c$$

$$\Rightarrow \frac{y-x}{1+xy} = c$$

$$\Rightarrow y-x = c(1+xy)$$

89. (B) Given that $f(x) = |3x^2 - 2x - 47|$ and $g(x) = x^2$
 Now, $fog(x) = f[g(x)]$
 $\Rightarrow fog(x) = f(x^2)$
 $\Rightarrow fog(x) = |3x^4 - 2x^2 - 47|$
 $\Rightarrow fog(2) = |3 \times 2^4 - 2 \times 2^2 - 47|$
 $\Rightarrow fog(2) = |48 - 8 - 47| = 7$
90. (B) $n(E) = {}^4C_2 \times {}^3C_1 \times {}^6C_0 + {}^4C_2 \times {}^3C_0 \times {}^6C_1 + {}^4C_3 \times {}^3C_0 \times {}^6C_0$
 $n(E) = 6 \times 3 \times 1 + 6 \times 1 \times 6 + 4 \times 1 \times 1$
 $n(E) = 18 + 36 + 4 = 58$
 $n(S) = {}^{13}C_3 = 286$

The required Probability = $\frac{58}{286} = \frac{29}{143}$

91. (C) Equation
 $lx^2 - mx + m = 0$
 $\alpha + \beta = \frac{m}{l}$ and $\alpha \cdot \beta = \frac{m}{l}$

Now, $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} \Rightarrow \frac{\alpha + \beta}{\sqrt{\alpha\beta}}$

$\Rightarrow \frac{m/l}{\sqrt{m/l}} = \sqrt{\frac{m}{l}}$

Hence $\sqrt{\frac{\alpha}{\beta}} + \sqrt{\frac{\beta}{\alpha}} = \sqrt{\frac{m}{l}}$

92. (B) $I = \int_0^{\pi/2} \frac{\phi(x)}{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)} dx \quad \dots(i)$

Prop.IV $\int_0^a f(x) dx = \int_0^a f(a-x) dx$

$I = \int_0^{\pi/2} \frac{\phi\left(\frac{\pi}{2} - x\right)}{\phi\left(\frac{\pi}{2} - x\right) + \phi(x)} dx \quad \dots(ii)$

from eq(i) and eq(ii)

$2I = \int_0^{\pi/2} \frac{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)}{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)} dx$

$2I = \int_0^{\pi/2} 1 dx$

$2I = [x]_0^{\pi/2}$

$2I = \frac{\pi}{2} - 0 \Rightarrow I = \frac{\pi}{4}$

93. (C) In ΔABC , if $\angle C = 120^\circ$, $c = \sqrt{6}$, $a = 2$
 Sine Rule

$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Now, $\frac{a}{\sin A} = \frac{c}{\sin C}$

$\Rightarrow \frac{2}{\sin A} = \frac{\sqrt{6}}{\sin 120}$

$\Rightarrow \frac{2}{\sin A} = \frac{\sqrt{6}}{\sqrt{3}/2}$

$\Rightarrow \sin A = \frac{1}{\sqrt{2}} \Rightarrow A = 45^\circ$

94. (C) $\cot^{-1}(4\cot x) + \cot^{-1}\left(\frac{5+3\cos 2x}{3\sin x}\right)$

$\Rightarrow \cot^{-1}\left(\frac{4}{\tan x}\right) + \tan^{-1}\left(\frac{3\sin 2x}{5+3\cos 2x}\right)$

$\Rightarrow \tan^{-1}\left(\frac{\tan x}{4}\right) + \tan^{-1}\left(\frac{3 \times 2 \tan x}{5 + \frac{3(1 - \tan^2 x)}{1 + \tan^2 x}}\right)$

$\Rightarrow \tan^{-1}\left(\frac{\tan x}{4}\right) + \tan^{-1}\left(\frac{6 \tan x}{8 + 2 \tan^2 x}\right)$

$\Rightarrow \tan^{-1}\left[\frac{\frac{\tan x}{4} + \frac{3 \tan x}{4 + \tan^2 x}}{1 - \frac{\tan x}{4} \times \frac{3 \tan x}{4 + \tan^2 x}}\right]$

$\Rightarrow \tan^{-1}\left[\frac{4 \tan x + \tan^3 x + 12 \tan x}{16 + 4 \tan^2 x - 3 \tan^2 x}\right]$

$\Rightarrow \tan^{-1}\left[\frac{16 \tan x + \tan^3 x}{16 + \tan^2 x}\right]$

$\Rightarrow \tan^{-1}\left[\frac{\tan x(16 + \tan^2 x)}{16 + \tan^2 x}\right]$

$\Rightarrow \tan^{-1}(\tan x) = x$

95. (B) Let $y = x^7 + 7^x$
 On differentiating both side w.r.t.'x'

$\frac{dy}{dx} = 7x^6 + 7^x \log 7$

96. (C)
 97. (B)

98. (C)
$$\begin{vmatrix} a+b & 1-c & c-a-b \\ b+c & 1-a & a-b-c \\ c+a & 1-b & b-a-c \end{vmatrix}$$

$$C_3 \rightarrow C_3 + C_1$$

$$\Rightarrow \begin{vmatrix} a+b & 1-c & c \\ b+c & 1-a & a \\ c+a & 1-b & b \end{vmatrix}$$

$$C_2 \rightarrow C_2 + C_3$$

$$\Rightarrow \begin{vmatrix} a+b & 1 & c \\ b+c & 1 & a \\ c+a & 1 & b \end{vmatrix}$$

$$C_1 \rightarrow C_1 + C_3$$

$$\Rightarrow \begin{vmatrix} a+b+c & 1 & c \\ a+b+c & 1 & a \\ a+b+c & 1 & b \end{vmatrix}$$

$$\Rightarrow (a+b+c) \begin{vmatrix} 1 & 1 & c \\ 1 & 1 & a \\ 1 & 1 & b \end{vmatrix}$$

$$\Rightarrow 0 \quad [\because \text{Two columns are identical.}]$$

99. (C) $2a \sin^2 \frac{B}{2} + 2b \sin^2 \frac{A}{2} = 2a + 2b - 3c$

$$\Rightarrow 2a + 2b - 2a \sin^2 \frac{B}{2} - 2b \sin^2 \frac{A}{2} = 3c$$

$$\Rightarrow a + a - 2a \sin^2 \frac{B}{2} + b + b - 2b \sin^2 \frac{A}{2} = 3c$$

$$\Rightarrow a + a \left(1 - 2 \sin^2 \frac{B}{2}\right) + b + b \left(1 - 2 \sin^2 \frac{A}{2}\right) = 3c$$

$$\Rightarrow a + a \cos B + b + b \cos A = 3c$$

$$\Rightarrow a + a \times \frac{a^2 + c^2 - b^2}{2ac} + b + b \times \frac{b^2 + c^2 - a^2}{2bc} = 3c$$

$$\Rightarrow a + \frac{a^2 + c^2 - b^2}{2c} + b + \frac{b^2 + c^2 - a^2}{2c} = 3c$$

$$\Rightarrow a + b + \frac{2c^2}{2c} = 3c$$

$$\Rightarrow a + b + c = 3c$$

$$\Rightarrow a + b = 2c$$

Hence a, c and b are in A.P.

100. (B) Line $\frac{3x-1}{-4} = \frac{y-1}{4} = \frac{z-2}{2}$

$$\Rightarrow \frac{x - \frac{1}{3}}{-\frac{4}{3}} = \frac{y-1}{4} = \frac{z-1}{2}$$

Direction cosines

$$\left\langle \frac{-4/3}{\sqrt{\left(\frac{-4}{3}\right)^2 + 4^2 + 2^2}}, \frac{4}{\sqrt{\left(\frac{-4}{3}\right)^2 + 4^2 + 2^2}}, \frac{2}{\sqrt{\left(\frac{-4}{3}\right)^2 + 4^2 + 2^2}} \right\rangle$$

$$\Rightarrow \left\langle \frac{-4/3}{14/3}, \frac{4}{14/3}, \frac{2}{14/3} \right\rangle$$

$$\Rightarrow \left\langle \frac{-2}{7}, \frac{6}{7}, \frac{3}{7} \right\rangle$$

101. (D) In ΔABC , $a=13$ cm, $b=12$ cm and $\angle C=150^\circ$

$$\text{Area of } \Delta ABC = \frac{1}{2} ab \sin C$$

$$= \frac{1}{2} \times 13 \times 12 \sin 150$$

$$= 13 \times 6 \times \frac{1}{2} = 39 \text{ cm}^2$$

102. (B) $\frac{\log_3 4 \times \log_{16} 2 \times \log_4 9}{\log_2 8 \times \log_8 9 \times \log_9 16}$

$$\Rightarrow \frac{\log_3 2^2 \times \log_{2^4} 2 \times \log_{2^2} 3^2}{\log_2 2^3 \times \log_{2^3} 3^2 \times \log_{3^2} 2^4}$$

$$\Rightarrow \frac{2 \log_3 2 \times \frac{1}{4} \log_2 2 \times \frac{2}{2} \log_2 3}{3 \log_2 2 \times \frac{2}{3} \log_2 3 \times \frac{4}{2} \log_3 2}$$

$$\Rightarrow \frac{1}{\frac{2}{4}} = \frac{1}{8}$$

103. (A) $\lim_{x \rightarrow \infty} \frac{x^3 - 2x^2 + 3x + 1}{1 - 2x + 6x^2 - 4x^3}$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{x^3 \left(1 - \frac{2}{x} + \frac{3}{x^2} + \frac{1}{x^3}\right)}{x^3 \left(\frac{1}{x^3} - \frac{2}{x^2} + \frac{6}{x} - 4\right)}$$

$$\Rightarrow \frac{1 - 0 + 0 + 0}{0 - 0 + 0 - 4} = \frac{-1}{4}$$

104. (C) foci $(\pm ae, 0) = (\pm 2, 0)$ and $e = \frac{1}{\sqrt{2}}$

here, $ae = 2$

$$\Rightarrow a \times \frac{1}{\sqrt{2}} = 2 \Rightarrow a = 2\sqrt{2}$$

Now, $b^2 = a^2(1 - e^2)$

$$\Rightarrow b^2 = 8 \left(1 - \frac{1}{2}\right)$$

$$\Rightarrow b^2 = 8 \times \frac{1}{2} \Rightarrow b^2 = 4$$

Equation of ellipse

$$\frac{x^2}{8} + \frac{y^2}{4} = 1$$

$$\Rightarrow x^2 + 2y^2 = 8$$

105. (D) Sphere $4x^2 + 4y^2 + 4z^2 - 8x - 10z = 20$

$$\Rightarrow x^2 + y^2 + z^2 - 2x - \frac{5}{2}z - 5 = 0$$

here, $u = -1, v = 0, w = \frac{-5}{4}, d = -5$

$$\text{radius}(r) = \sqrt{u^2 + v^2 + w^2 - d}$$

$$r = \sqrt{1 + 0 + \frac{25}{16} + 5}$$

$$r = \sqrt{\frac{121}{16}} = \frac{11}{4}$$

106. (C) Given that $f(x) = \sqrt{64 - x^2} \Rightarrow f'(x) = \frac{-x}{\sqrt{64 - x^2}}$

Now, $\lim_{x \rightarrow 4} \frac{f(x) - f(4)}{x - 4} \quad \left[\frac{0}{0} \right] \text{Form}$

by L-Hospital's Rule

$$\Rightarrow \lim_{x \rightarrow 4} \frac{f'(x) - 0}{1}$$

$$\Rightarrow \lim_{x \rightarrow 4} \frac{-x}{\sqrt{64 - x^2}}$$

$$\Rightarrow \frac{-4}{\sqrt{64 - 16}}$$

$$\Rightarrow \frac{-4}{\sqrt{48}} = \frac{-1}{\sqrt{3}}$$

107. (B) $f(x) = x^{1/3}(3 - 4x)$

$$f'(x) = x^{1/3}(-4) + (3 - 4x) \times \frac{1}{3} x^{-2/3}$$

$$f'(x) = -4x^{1/3} + \frac{3 - 4x}{3x^{2/3}}$$

$$f'(x) = \frac{-12x + 3 - 4x}{3x^{2/3}}$$

$$f'(x) = \frac{3 - 16x}{3x^{2/3}}$$

For critical points

$$f'(x) = 0$$

$$\Rightarrow \frac{3 - 16x}{3x^{2/3}} = 0 \Rightarrow x = \frac{3}{16}$$

108. (C) $x\sqrt{1+y^2} + y\sqrt{1+x^2} = 0$

On differentiating both sides w.r.t. 'x'

$$\Rightarrow x \times \frac{1}{2\sqrt{1+y^2}} \times 2y \frac{dy}{dx} + \sqrt{1+y^2} \times 1 +$$

$$y \times \frac{1 \times 2x}{2\sqrt{1+x^2}} + \sqrt{1+x^2} \frac{dy}{dx} = 0$$

$$\Rightarrow \frac{xy}{\sqrt{1+y^2}} \frac{dy}{dx} + \sqrt{1+y^2} + \frac{xy}{\sqrt{1+x^2}} + \sqrt{1+x^2}$$

$$\frac{dy}{dx} = 0$$

$$\Rightarrow \frac{-x^2}{\sqrt{1+x^2}} \frac{dy}{dx} + \sqrt{1+y^2} + \frac{-y^2}{\sqrt{1+y^2}} + \sqrt{1+x^2}$$

$$\frac{dy}{dx} = 0$$

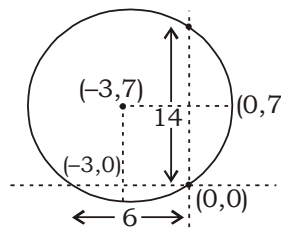
$$\Rightarrow \frac{dy}{dx} \left[\sqrt{1+x^2} - \frac{x^2}{\sqrt{1+x^2}} \right] = \frac{y^2}{\sqrt{1+y^2}} - \sqrt{1+y^2}$$

$$\Rightarrow \frac{dy}{dx} \times \frac{1}{\sqrt{1+x^2}} = \frac{-1}{\sqrt{1+y^2}}$$

$$\Rightarrow \frac{dy}{dx} = \frac{-\sqrt{1+x^2}}{\sqrt{1+y^2}}$$

$$\Rightarrow \frac{dy}{dx} = -\sqrt{\frac{1+x^2}{1+y^2}}$$

109. (C)



Intercepts on x-axis and y-axis = 6 units and 14 units

110. (A) $8 \tan \theta + 15 = 0$, where $\frac{\pi}{2} < \theta < \pi$

$$\Rightarrow \tan \theta = \frac{-15}{8}$$

here, $\sin \theta = \frac{15}{17}$, $\cos \theta = \frac{-8}{17}$, $\cot \theta = \frac{-8}{15}$

Now, $3 \cot \theta - 4 \cos \theta + \sin \theta$

$$\Rightarrow 3 \left(\frac{-8}{15} \right) - 4 \left(\frac{-8}{17} \right) + \frac{15}{17}$$

$$\Rightarrow \frac{-8}{5} + \frac{32}{17} + \frac{15}{17}$$

$$\Rightarrow \frac{-8}{5} + \frac{47}{17}$$

$$\Rightarrow \frac{-136 + 235}{85} = \frac{99}{85}$$

111. (B) $\sec 2040 = \sec(360 \times 6 - 120)$

$$\Rightarrow \sec 2040 = \sec 120$$

$$\Rightarrow \sec 2040 = \sec(90 + 30)$$

$$\Rightarrow \sec 2040 = -\sec 30 = \frac{-2}{\sqrt{3}}$$

112. (C) $y = (1+x^2)\tan^{-1}x - x$
On differentiating both sides w.r.t.'x'

$$\frac{dy}{dx} = (1+x^2) \times \frac{1}{1+x^2} + \tan^{-1}x \times (2x) - 1$$

$$\frac{dy}{dx} = 1 + 2x \tan^{-1}x - 1$$

$$\frac{dy}{dx} = 2x \tan^{-1}x$$

113. (C) $I = \int e^{x-\frac{1}{x}} \left(1 + \frac{1}{x^2}\right) dx$

Let $x - \frac{1}{x} = t$

$$\Rightarrow \left(1 + \frac{1}{x^2}\right) dx = dt$$

$$I = \int e^t dt$$

$$I = e^t + c$$

$$I = e^{x-\frac{1}{x}} + c$$

114. (D) $\frac{1}{\cos 615} + \frac{\sqrt{3}}{\sin 525}$

$$\Rightarrow \frac{1}{\cos(720-105)} + \frac{\sqrt{3}}{\sin(360+165)}$$

$$\Rightarrow \frac{1}{\cos 105} + \frac{\sqrt{3}}{\sin 165}$$

$$\Rightarrow \frac{1}{\cos(90+15)} + \frac{\sqrt{3}}{\sin(180+15)}$$

$$\Rightarrow \frac{1}{-\sin 15} + \frac{\sqrt{3}}{\sin 15}$$

$$\Rightarrow \frac{\sqrt{3}-1}{\sin 15}$$

$$\Rightarrow \frac{\sqrt{3}-1}{\frac{\sqrt{3}-1}{2\sqrt{2}}} = 2\sqrt{2}$$

115. (D) Given that $\vec{a} = -3\hat{i} + 2\hat{j} + \hat{k}$ and $\vec{b} = \hat{i} + \hat{j} - 2\hat{k}$

Now, $\vec{b} + 2\vec{a} = (\hat{i} + \hat{j} - 2\hat{k}) + 2(-3\hat{i} + 2\hat{j} + \hat{k})$

$$\Rightarrow \vec{b} + 2\vec{a} = -5\hat{i} + 5\hat{j}$$

and $2\vec{a} - 3\vec{b} = 2(-3\hat{i} + 2\hat{j} + \hat{k}) - 3(\hat{i} + \hat{j} - 2\hat{k})$

$$\Rightarrow 2\vec{a} - 3\vec{b} = -9\hat{i} + \hat{j} + 8\hat{k}$$

Now, $(\vec{b} + 2\vec{a}) \cdot (2\vec{a} - 3\vec{b}) = -5 \times (-9) + 5 \times 1 + 0$
 $= 46 + 5 = 50$

116. (A) $\sec^{-1}(-2) = \sec^{-1}\left(-\sec\frac{\pi}{3}\right)$

$$\Rightarrow \sec^{-1}(-2) = \sec^{-1}\left[\sec\left(\pi - \frac{\pi}{3}\right)\right]$$

$$\Rightarrow \sec^{-1}(-2) = \sec^{-1}\left(\sec\frac{2\pi}{3}\right) = \frac{2\pi}{3}$$

117. (B) $f(x) = \begin{cases} ax^2 - 6, & x < 1 \\ x + 7, & x \geq 1 \end{cases}$ is continuous at $x=1$,

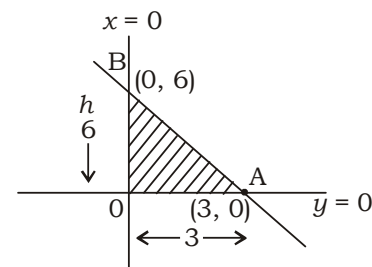
then $\lim_{x \rightarrow 1^-} f(x) = f(1)$

$$\Rightarrow \lim_{x \rightarrow 1^-} ax^2 - 6 = 1 + 7$$

$$\Rightarrow a - 6 = 8 \Rightarrow a = 14$$

118. (C)

119. (A)



The required area = $\frac{1}{2} \times OA \times OB$

$$= \frac{1}{2} \times 3 \times 6 = 9 \text{ sq. unit}$$

120. (B) $I = \int_{-1}^1 x^2 \cdot e^x dx$

$$I = 2 \int_0^1 x^2 \cdot e^x dx$$

$$I = 2 \left[x^2 \int e^x dx - \int \left\{ \frac{d}{dx}(x^2) \cdot \int e^x dx \right\} dx \right]_0^1$$

$$I = 2 \left[x^2 \cdot e^x - \int 2x \cdot e^x dx \right]_0^1$$

$$I = 2 \left[x^2 \cdot e^x - 2 \left\{ x \cdot e^x - \int 1 \cdot e^x dx \right\} \right]_0^1$$

$$I = \left[x^2 \cdot e^x - 2x \cdot e^x + 2e^x \right]_0^1$$

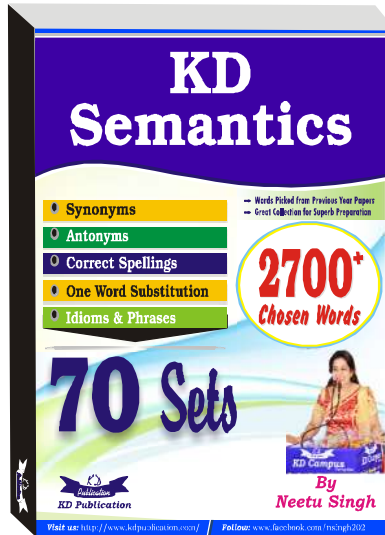
$$I = [(1 \cdot e^1 - 2 \cdot 1 \cdot e^1 + 2e^1) - (0 - 0 + 2e^0)]$$

$$I = 2[e - 2e + 2e - 2]$$

$$I = 2e - 4$$

NDA (MATHS) MOCK TEST - 154 (Answer Key)

- | | | | | | |
|---------|---------|---------|---------|----------|----------|
| 1. (C) | 21. (B) | 41. (C) | 61. (B) | 81. (D) | 101. (D) |
| 2. (B) | 22. (C) | 42. (A) | 62. (D) | 82. (D) | 102. (B) |
| 3. (A) | 23. (B) | 43. (B) | 63. (C) | 83. (D) | 103. (A) |
| 4. (D) | 24. (A) | 44. (B) | 64. (C) | 84. (B) | 104. (C) |
| 5. (D) | 25. (C) | 45. (C) | 65. (C) | 85. (B) | 105. (D) |
| 6. (C) | 26. (D) | 46. (D) | 66. (B) | 86. (C) | 106. (C) |
| 7. (D) | 27. (C) | 47. (A) | 67. (D) | 87. (B) | 107. (B) |
| 8. (B) | 28. (C) | 48. (C) | 68. (C) | 88. (B) | 108. (C) |
| 9. (D) | 29. (B) | 49. (B) | 69. (D) | 89. (B) | 109. (C) |
| 10. (B) | 30. (C) | 50. (A) | 70. (C) | 90. (B) | 110. (A) |
| 11. (C) | 31. (D) | 51. (C) | 71. (B) | 91. (C) | 111. (B) |
| 12. (C) | 32. (A) | 52. (D) | 72. (C) | 92. (B) | 112. (C) |
| 13. (B) | 33. (B) | 53. (C) | 73. (B) | 93. (C) | 113. (C) |
| 14. (C) | 34. (C) | 54. (C) | 74. (B) | 94. (C) | 114. (D) |
| 15. (B) | 35. (B) | 55. (B) | 75. (B) | 95. (B) | 115. (D) |
| 16. (C) | 36. (C) | 56. (C) | 76. (D) | 96. (C) | 116. (A) |
| 17. (D) | 37. (D) | 57. (A) | 77. (B) | 97. (B) | 117. (B) |
| 18. (C) | 38. (C) | 58. (B) | 78. (C) | 98. (C) | 118. (C) |
| 19. (C) | 39. (A) | 59. (C) | 79. (C) | 99. (C) | 119. (A) |
| 20. (D) | 40. (D) | 60. (C) | 80. (C) | 100. (B) | 120. (B) |



Note:- If your opinion differs regarding any answer, please message the mock test and question number to 8860330003

Note:- Whatsapp with Mock Test No. and Question No. at 7053606571 for any of the doubts, also share your suggestions and experience of Sunday Mock

Note:- If you face any problem regarding result or marks scored, please contact 9313111777