

**TEST NO.**  
**50**

**SSC Mains (Maths) Answer with Explanation**

1. (A)  $4^{3.5} : 2^5$   
 $= (2^2)^{3.5} : 2^5 = 2^7 : 2^5$   
 $= 2^2 : 1$   
 $= 4 : 1$
2. (D) Now,  
 Required ratio = T.S.A of one small cube :  
 T.S.A of the big cube  
 $= 6 \times (1)^2 : 6 \times (5)^2$   
 $= 1 : 25$
3. (B) Money left =  $100\% - (80\% + 6\% \text{ of } 20\%)$   
 $= 100\% - 81.2\%$   
 $= 18.8\% \text{ of total pocket money}$   
 And,  
 $18.8\% \text{ of total pocket money} = 47 \text{ paise}$   
 $= ₹ \frac{47}{100}$   
 So, Total pocket money  
 (i.e 100%) =  $₹ \frac{47}{100} \times \frac{100}{18.8} = ₹ 2.5$
4. (B) Total C.I in 2 years @ 12.5% p.a  
 $= 12.5\% + 12.5\% + 12.5\% \text{ of } 12.5\% \text{ of sum}$   
 $= 25\% + \frac{12.5}{8}\% \text{ of sum}$   
 $= \frac{212.5}{8}\% \text{ of sum}$   
 $= ₹ 510$   
 So,  
 Total S.I in 2 years @ 12.5% p.a  
 $= (2 \times 12.5\%) \text{ of the sum}$   
 $= 25\% \text{ of the sum}$   
 $= \frac{510 \times 8}{212.5} \times 25 = ₹ 480$
5. (C) Let  $x$  = initial C.P of the article.  

<u>C.P</u>	<u>S.P</u>
1 <sup>st</sup> condition $x \xrightarrow{20\% \text{ loss}}$	$0.8x$
2 <sup>nd</sup> condition $x \xrightarrow{5\% \text{ profit}}$	$0.8x + 100$
	$= 10.5x$

 $\Rightarrow 1.05x = 0.8x + 100$   
 $\Rightarrow x = \frac{100}{0.25} = 400$
6. (D) Total S.I =  $(3 \times 12\%)$  of the principal amount  
 $= 36\% \text{ of the principal amount}$
- $= ₹ 5400$   
 So, The principal amount (i.e 100%)  
 $= ₹ \frac{5400}{36} \times 100 = ₹ 15000$
7. (C) Required distance  
 $= \frac{\text{Average Speed} \times \text{Total Time}}{2}$   
 $= \frac{2 \times (5+1)(5-1)}{(5+1) + (5-1)} \times 1$   
 $= \frac{4.8}{2} \text{ km} = 2.4 \text{ km}$
8. (D) Money spent on article  
 $= 25\% \text{ of total amount}$   
 Money spent on cloths  
 $= 10\% \text{ of remaining (75\%) amount}$   
 $= 7.5\% \text{ of total amount}$   
 $= (25\% + 7.5\%) \text{ of total amount} + ₹ 531.25$   
 $= \text{Total amount} - ₹ 8000$   
 $= \text{Total (100\%) amount} - 32.5\% \text{ of total amount}$   
 $= ₹ 8000 + 531.25$   
 $= ₹ 8531.25$   
 $\Rightarrow 67.5\% \text{ of the total amount} = ₹ 8531.25$   
 So,  
 Money spent on clothes  
 i.e 7.5% of the total amount  
 $= \frac{8531.25}{67.5} \times 7.5 = ₹ 948$
9. (D) Required time =  $\frac{60 \times 40}{60 - 40}$  minutes  
 $= \frac{2400}{20}$  minutes  
 $= 120 \text{ minutes}$
10. (A)  $\frac{x^2 + y^2 + xy}{x^3 - y^3} = \frac{1}{x - y}$   
 $[\because (x^3 - y^3) = (x - y)(x^2 + y^2 + xy)]$   
 $= \frac{1}{19 - 18} = \frac{1}{1} = 1$
11. (A)  $(0.5 \times 5 + 0.25 \times 0.5 + 0.5 \times 4 + 0.5 \times 0.75)$   
 $= 2.5 + 0.125 + 2 + 0.375$   
 $= 5$

12. (D) A : B : C

$$1 : 2 : 3 \quad \left[ \text{Average} = \frac{1+2+3}{3} = 2 \right]$$

$$\therefore \text{Average} = 600 \Rightarrow 2 \cong 600$$

$$\text{So, } A : B : C$$

$$1 : 2 : 3 \\ 300 : 600 : 900$$

Now,

$$A \xrightarrow{+10\%} 300 + 30 = 330 \text{ (new value of A)}$$

$$B \xrightarrow{+10\%} 600 - 120 = 480 \text{ (new value of B)}$$

$$\text{Average} \xrightarrow{+5\%} 600 + 30 = 630 \text{ (new average)}$$

Now,

$$\Rightarrow \frac{330 + 480 + \text{new value of C}}{3} = 630$$

$$= \text{new value of C } (630 \times 3) - (330 + 480) = 1080$$

$$= \text{Increase in C} = 1080 - 900 = 180$$

13. (D)  $116 - 92 = 24$

Let  $x =$  profit when S.P = 92

$$\text{i.e. } 3x - x = 24$$

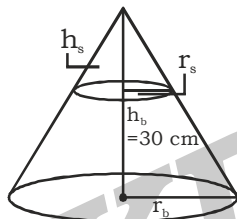
So,  $3x =$  profit when S.P = 116

$$\Rightarrow x = 12$$

$\Rightarrow$  When S.P = 92, profit = ₹ 12

$$\text{So, C.P} = 92 - 12 = ₹ 80$$

14. (D)



here,

$$\left[ \because \frac{r_b}{r_s} = \frac{h_b}{h_s} \right]$$

$$\text{Volume of smaller cone} = \frac{\text{vol. of bigger cone}}{27}$$

$$\text{i.e. } \frac{1}{3} \pi (r_s)^2 (h_s) = \frac{1}{3} \pi (r_b)^2 (h_b) / 27$$

$$\text{or, } (r_s)^2 (h_s) = \frac{(r_b)^2 (h_b)}{27}$$

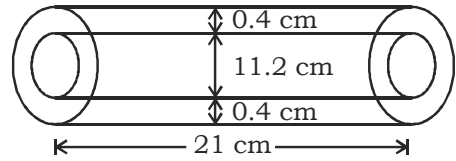
$$\Rightarrow \frac{(r_b)^2 (h_b)}{(r_s)^2 (h_s)} = 27$$

$$\text{or, } \frac{r_b \times r_b \times h_b}{r_s \times r_s \times h_s} = \frac{3 \times 3 \times 3}{1 \times 1 \times 1}$$

$$\text{or, } \frac{h_b}{h_s} = \frac{3}{1} \Rightarrow h_s = \frac{h_b}{3} = \frac{30}{3} = 10 \text{ cm}$$

$$\Rightarrow \text{The required height above the base,} \\ = (30 - 10) \text{ cm} = 20 \text{ cm}$$

15. (C)



Volume of metal = External volume of cylindrical tube - Internal volume of cylindrical tube

$$= \pi (r_{ex})^2 h - \pi (r_{in})^2 h = \pi h \{ (r_{ex})^2 - (r_{in})^2 \}$$

$$= \pi h \left\{ \left( \frac{12}{2} \right)^2 - \left( \frac{11.2}{2} \right)^2 \right\}$$

$$= \frac{22}{7} \times 21 \times (36 - 31.36)$$

$$= 22 \times 3 \times 4.64 = 306.24 \text{ cm}^3$$

16. (B)  $1 \div [1 + 1 \div \{1 + 1 \div (1 + 1 \div 2)\}]$

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + 1 \div \left( 1 + \frac{1}{2} \right) \right\} \right]$$

$$= 1 \div \left[ 1 + 1 \div \left\{ 1 + 1 \times \left( \frac{2}{3} \right) \right\} \right]$$

$$= 1 \div \left[ 1 + 1 \div \left\{ \left( \frac{5}{3} \right) \right\} \right] = 1 \div \left[ 1 + \frac{5}{3} \right]$$

$$= 1 \div \frac{8}{5} = 1 \times \frac{5}{8} = \frac{5}{8}$$

17. (B) L.C.M for 4, 6, 10 and 15 = 60

N will be in form of  $N = 60n + 2$

Now,

least six digit number of form  $60n$

(i.e. divisible by 60) = 100020

So,

$\Rightarrow$  least six digit number of form N

$$= 100020 + 2 = 100022$$

$$\Rightarrow \text{Sum of digits of N} = 1+0+0+0+2+2 = 5$$

18. (A) Present age of son =  $x$  years

Present age of father =  $3x + 3$  years

After 3 years, son =  $x + 3$  years

father =  $3x + 3 + 3$

$$= 3x + 6 \text{ years}$$

A.T.Q,

$$3x + 6 = 2(x + 3) + 10$$

$$3x + 6 = 2x + 6 + 10$$

$$3x - 2x = 10$$

$$x = 10$$

Father's present age =  $3 \times 10 + 3$

$$= 33 \text{ years}$$

19. (C) ABC  $\leftarrow$  Let the three co-prime numbers

A.T.Q,  $A \times B = 551$  and  $B \times C = 1073$

And  $19 \times 29 = 551$  and  $29 \times 37 = 1073$

$$\Rightarrow A = 19, B = 29 \text{ and } C = 37$$

$$\Rightarrow \text{Sum of three numbers} = 19 + 29 + 37 \\ = 85$$

20. (C) 

<b>₹ 500</b>	<b>Required Sum</b>
Rate of interest 12%	10%
S.I after 4 yrs 480	480
S.I is same	
$\Rightarrow \frac{500}{\text{Required Sum}} = \frac{10\%}{12\%}$	
$\Rightarrow \frac{500}{\text{Required Sum}} = \frac{5}{6}$	
$\Rightarrow \text{Required sum} = ₹ \frac{500}{5} \times 6 = ₹ 600$	
21. (B) Total ages of 40 students =  $40 \times 15 = 600$  years  
Let the average age of 10 new students =  $x$  years  
$$= \frac{600 + 10x}{50} = 15.2$$
$$= 600 + 10x = 15.2 \times 50$$
$$= 600 + 10x = 760$$
$$x = \frac{760 - 600}{10} = \frac{160}{10} = 16 \text{ years}$$
22. (B)  $T_1 = \frac{24}{6} = 4$  hours,  $T_2 = \frac{24}{8} = 3$  hours  
 $T_3 = \frac{24}{12} = 2$  hours  
Average speed =  $\frac{24 + 24 + 24}{4 + 3 + 2} = \frac{72}{9} = 8$  km/h
23. (B) Radius of the shot put ball = 7cm  
Height of the cylinder =  $\frac{7}{3}$  cm  
Volume of the shot put = Volume of the cylinder  
$$\frac{4}{3} \pi \times 7^3 = \pi \times R^2 \times \frac{7}{3}$$
$$R^2 = \frac{\frac{4}{3} \pi \times 7^3 \times \frac{3}{7}}{\pi}$$
$$R = \sqrt{4 \times 7^2} = 2 \times 7 = 14 \text{ cm}$$
$$D = 2R = 2 \times 14 = 28 \text{ cm}$$
24. (D)  $h = 1 + \frac{25}{100} \text{ m} = \frac{5}{4} \text{ m}$   
Total area of the wet surface = Area of the cistern without top  
$$= 2[lb + bh + lh] - lb$$
$$= 2 \left[ 6 \times 4 + 4 \times \frac{5}{4} + 6 \times \frac{5}{4} \right] - 24$$
$$= 2 \left[ 24 + 5 + \frac{30}{4} \right] - 24$$
- $$= 2 \left[ \frac{29 \times 4 + 30}{4} \right] - 24$$
$$= 2 \times \frac{146}{4} - 24 = 73 - 24 = 49 \text{ m}^2.$$
25. (C)  $(\sqrt[3]{3.5} + \sqrt[3]{2.5}) \left\{ (\sqrt[3]{3.5})^2 - \sqrt[3]{8.75} + (\sqrt[3]{2.5})^2 \right\}$   
$$= (\sqrt[3]{3.5})^3 + (\sqrt[3]{2.5})^3$$
  
[by using  $(a + b)(a^2 - ab + b^2) = a^3 + b^3$ ]  
$$= 3.5 + 2.5 = 6$$
26. (A) Total CP = CP + repairing charge  
$$= 1200 + 200 = ₹ 1400$$
  
S.P = ₹ 1680  
$$\% \text{ of profit} = \frac{(1680 - 1400) \times 100}{\text{CP}}$$
$$= \frac{280 \times 100}{1400} = 20\%$$
27. (D) Let  $x$  = the larger number and  $y$  = the smaller number  
Now,  
$$x - y = 2395 \quad \dots(i)$$
  
and  $\frac{x}{y}$ ; Quotient = 7 and remainder = 25  
$$\Rightarrow x = 7y + 25 \quad \dots(ii)$$
  
Now on putting value of  $y$  from (i) in (ii) we get,  
$$x = 7(x - 2395) + 25$$
$$x = 7x - 16765 + 25$$
$$6x = 16765 - 25$$
$$\Rightarrow x = \frac{16740}{6} = 2790$$
28. (A)  $\sqrt[3]{4} + \sqrt[3]{16} + 1 = \sqrt[3]{2 \times 2} + \sqrt[3]{2 \times 8} + 1$   
$$= (\sqrt[3]{2} \times \sqrt[3]{2}) + (2 \times \sqrt[3]{2} \times 1) + (1 \times 1)$$
$$= (\sqrt[3]{2})^2 + (2 \times \sqrt[3]{2} \times 1) + (1)^2$$
$$= (\sqrt[3]{2} + 1)^2$$
  
So, square root of  $(\sqrt[3]{4} + \sqrt[3]{16} + 1)$   
i.e  $(\sqrt[3]{4} + \sqrt[3]{16} + 1) = \sqrt[3]{2} + 1$
29. (C) 
$$\frac{0.7 \times 0.7 \times 0.7 + 0.3 \times 0.3 \times 0.3 \times 0.7 \times 3}{0.7 \times 0.7 + 0.3 \times 0.3 + 0.42}$$
$$= \frac{0.7 \times 0.7 \times 0.7 + 0.3 \times 0.3 \times 0.3 \times 3 \times 0.7 \times 0.3 \times 1}{0.7 \times 0.7 + 0.3 \times 0.3 + 2 \times 0.7 \times 0.3}$$
$$= \frac{(0.7)^2 + (0.3)^2 + 0.3 \times 0.7 \times 0.3 \times (0.7 + 0.3)}{(0.7)^2 + (0.3)^2 + 2 \times 0.7 \times 0.3}$$
$$= \frac{(0.7 + 0.3)^2}{(0.7 + 0.3)^2} = \frac{1^3}{1^2} = \frac{1}{1} = 1$$

30. (B)  $A + C = \frac{22}{37}$  part

$$\Rightarrow B = 1 - \frac{22}{37} \text{ part} = \frac{15}{37} \text{ part}$$

And,

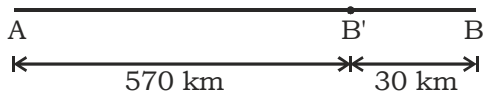
$$B + C = \frac{21}{37} \text{ part}$$

$$\text{or } \frac{15}{27} + C = \frac{21}{37} \Rightarrow C = \frac{21}{37} - \frac{15}{37} = \frac{6}{37} \text{ part}$$

So,

$$\text{Wage of C} = \frac{6}{37} \times 9250 = ₹ 1500$$

31. (A)  $\overleftarrow{\hspace{10em}} \xrightarrow{\hspace{10em}}$  600 km  $\overrightarrow{\hspace{10em}}$



Distance covered by B before movement of A i.e. Distance covered by B in 20 minutes

$$= \left( 90 \times \frac{20}{60} \right) \text{ km} = 30 \text{ km}$$

$\Rightarrow$  When train from station A starts to move; the other train will be at B' and distance between A & B (600 - 30) km = 570 km

Now,

$$\begin{aligned} \text{Relative speed of trains} &= (100 + 90) \text{ km/hr} \\ &= 190 \text{ km/hr} \end{aligned}$$

So, Time taken by each train to reach

$$\text{each other} = \left( \frac{570}{190} \right) \text{ hr} = 3 \text{ hours}$$

And in 3 hours, distance travelled by A = (100 × 3) km = 300 kms

$\Rightarrow$  Both train will cross each other at a distance 300 kms and from A i.e at the exact middle point of A and B.

32. (C) Let x = no. of girls

So,

$$\begin{aligned} 600 \times 11 \text{ years } 9 \text{ months} &= x \times 11 \text{ years} + (600 - x) \times 12 \text{ years} \\ \Rightarrow 7050 \text{ years} &= (11x + 7200 - 12x) \text{ years} \\ \Rightarrow x &= 7200 - 7050 = 150 \end{aligned}$$

33. (D) 1<sup>st</sup> no. : 2<sup>nd</sup> no. and 2<sup>nd</sup> no. : 3<sup>rd</sup> no.

$$= 3 : 2 \qquad \qquad \qquad 3 : 2$$

$$\Rightarrow 1^{\text{st}} \text{ no.} : 2^{\text{nd}} \text{ no.} : 3^{\text{rd}} \text{ no.}$$

$$= 9 : 6 : 4$$

So, Let the no, are 9x, 6x and 4x

A.T.Q,  $(9x)^2 + (6x)^2 + (4x)^2 + 532$

$$\Rightarrow 133x^2 = 532$$

$$\Rightarrow x = 2$$

So, the 2nd no. i.e  $6x = 6 \times 2 = 12$

34. (B) We know that,  $5^2 + 12^2 = 13^2$  ....(i)

$$5^{\sqrt{x}} + 12^{\sqrt{x}} = 13^{\sqrt{x}} \quad \dots\text{(ii)}$$

from equation (i) and (ii)

$$\sqrt{x} = 2 \Rightarrow x = 4$$

35. (C) 20% discount on L.P - 25% discount on L.P = ₹ 500

$$\Rightarrow 80\% \text{ value of L.P} - 75\% \text{ value of L.P} = ₹ 500$$

$$\Rightarrow 5\% \text{ value of L.P} = ₹ 500$$

$$\Rightarrow \text{L.P (i.e 100\%)} = ₹ \frac{500 \times 100}{5} = ₹ 10000$$

So, Tarun bought the TV at 80% of L.P

$$= ₹ \frac{80}{100} \times 10000 = ₹ 8000$$

36. (B) SI@ 3% p.a for 4 years = 12% of sum

SI@ 2% p.a for 5 years = 10% of sum

A.T.Q,

$$(12\% - 10\%) \text{ of sum} = ₹ 150$$

$$\Rightarrow 2\% = 150$$

$$\Rightarrow \text{sum} = \frac{150 \times 100}{2} = ₹ 7500$$

37. (C) 

<b>S.I</b>	<b>C.I</b>
For 1 <sup>st</sup> year ₹ 135	₹ 135
For 2 <sup>nd</sup> years ₹ 135	₹ 162 = 135 + 27

Now,

if r = rate of interest per annum

$$\Rightarrow r \% \text{ of } 135 = 27$$

$$\Rightarrow r = \frac{27 \times 100}{135} = 20$$

Also,

$$\Rightarrow 20\% \text{ of the sum} = 135$$

$$\Rightarrow \text{sum} = \frac{135 \times 100}{20} = ₹ 675$$

38. (B) A.T.Q,

$$P \left( 1 + \frac{20}{100} \right)^t > 2P$$

(where P → Principal and t → required no. of years)

$$\text{or } \left( 1 + \frac{1}{5} \right)^t > 2 \quad \text{or } \left( \frac{6}{5} \right)^t > 2$$

Now,

$$\left( \frac{6}{5} \right)^t < 2, \left( \frac{6}{5} \right)^2 < 2, \left( \frac{6}{5} \right)^3 < 2 \text{ but } \left( \frac{6}{5} \right)^4 > 2$$

$$\Rightarrow \text{Required least no. of complete years} = 4 \text{ years}$$

39. (B) Let  $x$  hour = time taken by pipe A alone to empty the pool  
 $2x$  hours = time taken by pipe B alone to empty the pool  
 So, Time taken by pipes A and B together to empty the pool

$$= \frac{x \times 2x}{x + 2x} \text{ hours}$$

$$= \frac{2x^2}{3x} \text{ hours} = \frac{2}{3}x \text{ hours}$$

$\Rightarrow$  Time taken by pipe C alone to empty the pool =  $\left(\frac{2}{3}x \times 2\right)$  hours =  $\frac{4}{3}x$  hours

$\Rightarrow$  Part of the pool which will be empty when A, B and C work together,

$$= \left(\frac{1}{x} + \frac{1}{2x} + \frac{3}{4x}\right) \text{ part}$$

$$= \left(\frac{4+2+3}{4x}\right) \text{ part} = \frac{9}{4x} \text{ part}$$

$\Rightarrow$  Total time taken by A, B and C working together to empty the pool

$$= \frac{4x}{9} = 400 \text{ minutes}$$

[ $\therefore$  6 hours 40 minutes = 400 minutes]

$$\Rightarrow x = \frac{400 \times 9}{4} \text{ minutes}$$

$$= 900 \text{ minutes} = 15 \text{ hours}$$

40. (C) -24, -20, -16.....  
 Let  $n$  = required no. of terms  
 Now,

$$S_n = \frac{n}{2} \{2a + (n-1)d\}$$

$$\text{i.e. } 180 = \frac{n}{2} \{2 \times (-24) + (n-1)4\}$$

$$\text{or, } 180 = \frac{n}{2} \{-48 + 4n - 4\}$$

$$\text{or, } 360 = 4n^2 - 52n$$

$$\text{or, } 4n^2 - 52n - 360 = 0$$

$$\Rightarrow n = 18$$

41. (D)  $a^2d^2 + b^2c^2 - 2abcd + a^2c^2 + b^2d^2 + 2abcd$   
 $= a^2(c^2 + d^2) + b^2(c^2 + d^2)$   
 $= (a^2 + b^2)(c^2 + d^2)$   
 $= 2 \times 1 = 2$

42. (A)  $\frac{(K-1)}{(2-K)} = \frac{1}{-3} = \frac{-2}{1}$

$$\text{or, } -3(K-1) = 2-K$$

$$\text{or, } -3K + 3 = 2 - K$$

$$\text{or, } -3K + K = 2 - 3$$

$$\Rightarrow -2k = -1$$

$$\Rightarrow K = \frac{1}{2}$$

43. (D)  $(x^2 + 5x + 10)^{-1} = \frac{1}{(x^2 + 5x + 10)}$

$\frac{1}{(x^2 + 5x + 10)}$  will be maximum when  $x^2 + 5x + 10$  is minimum and maximum

$$\text{value of } x^2 + 5x + 10 = -\left(\frac{5^2 - 4 \times 1 \times 10}{4}\right)$$

$$= \frac{15}{4}$$

$$\text{So, Required maximum value} = \frac{1}{\frac{15}{4}} = \frac{4}{15}$$

44. (D)  $P = \sqrt{\frac{1 - \sin x}{1 + \sin x}} \Rightarrow P = \frac{1 - \sin x}{\cos x}$

$$\text{and } Q = \frac{1 - \sin x}{\cos x}$$

$$R = \frac{\cos x}{1 + \sin x} \times \frac{1 - \sin x}{1 - \sin x}$$

$$= \frac{\cos x(1 - \sin x)}{\cos^2 x}$$

$$\Rightarrow R = 1 - \sin x$$

$$P = Q = R$$

45. (D)  $\sin \theta + \sin^2 \theta + \sin^3 \theta = 1$

$$\Rightarrow \sin \theta + \sin^3 \theta = \cos^2 \theta$$

$$\Rightarrow \sin \theta(1 + \sin^2 \theta) = \cos^2 \theta$$

$$\Rightarrow \sin \theta(2 - \cos^2 \theta) = \cos^2 \theta$$

$$\Rightarrow \sqrt{1 - \cos^2 \theta}(2 - \cos^2 \theta) = \cos^2 \theta$$

$$\Rightarrow (1 - \cos^2 \theta)[4 + \cos^4 \theta - 4 \cos^2 \theta] = \cos^4 \theta$$

$$\Rightarrow 4 + \cos^4 \theta - 4 \cos^2 \theta - 4 \cos^2 \theta - \cos^6 \theta + 4 \cos^4 \theta = \cos^4 \theta$$

$$\Rightarrow -\cos^6 \theta + 4 \cos^4 \theta - 8 \cos^2 \theta + 4 = 0$$

$$\Rightarrow + \cos^6 \theta - 4 \cos^4 \theta + 8 \cos^2 \theta = 4$$

46. (B)  $\sec^2 \theta - (1 + \sqrt{3}) \tan \theta + \sqrt{3} - 1 = 0$

$$\Rightarrow 1 + \tan^2 \theta - \tan \theta - \sqrt{3} \tan \theta + \sqrt{3} - 1 = 0$$

$$\Rightarrow \tan^2 \theta - \sqrt{3} \tan \theta - \tan \theta + \sqrt{3} = 0$$

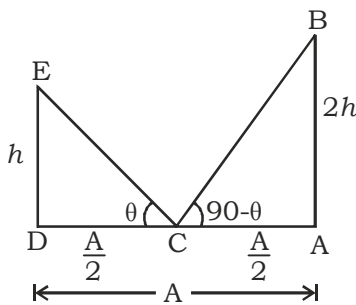
$$\Rightarrow \tan \theta(\tan \theta - \sqrt{3}) - 1(\tan \theta - \sqrt{3}) = 0$$

$$\Rightarrow (\tan \theta - \sqrt{3})(\tan \theta - 1) = 0$$

$$\Rightarrow \tan \theta - \sqrt{3} = 0$$

$$\Rightarrow \tan \theta = \sqrt{3}$$

47. (D)



In  $\triangle ECD$

$$\tan \theta = \frac{h}{\frac{A}{2}} = \frac{2h}{A} \quad \dots(i)$$

In  $\triangle ACB$

$$\tan(90 - \theta) = \frac{2h}{A} \times 2$$

$$\cos \theta = \frac{4 - h}{A}$$

$$\tan \theta = \frac{A}{4h} \quad \dots(ii)$$

From equ<sup>n</sup> (i) and (ii)

$$\frac{2h}{A} = \frac{A}{4h^2}$$

$$8h^2 = A^2$$

$$h^2 = \frac{A^2}{8} = h = \frac{A}{2\sqrt{2}}$$

48. (D)  $2 \sin\left(\frac{\pi x}{2}\right) = x^2 + \frac{1}{x^2}$

$$\Rightarrow 2 \sin\left(\frac{\pi x}{2}\right) = \left(x^2 + \frac{1}{x^2}\right)^2 + 2$$

$$[\because a^2 + b^2 = (a - b)^2 + 2ab]$$

$$\Rightarrow \left(x - \frac{1}{x}\right)^2 = 2 \left\{ \sin\left(\frac{\pi x}{2}\right) - 1 \right\}$$

$$\Rightarrow \left(x - \frac{1}{x}\right) = \sqrt{2} \times 0 \quad \left[ \sin \frac{\pi}{2} = 1 \right]$$

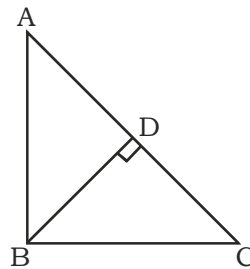
$$= 0 \quad \text{Also, } \left[ 1 = \sin \frac{\pi x}{2} \right]$$

49. (D)  $\frac{\text{Per}(\triangle ABC)}{\text{Per}(\triangle DEF)} = \frac{AB}{DE}$

$$\frac{\text{Per}(\triangle ABC)}{25} = \frac{9.1}{6.5}$$

$$\text{Per}(\triangle ABC) = 35$$

50. (B)



$$\triangle ADB \cong \triangle ABC$$

$$\Rightarrow \frac{AD}{AB} = \frac{AB}{AC}$$

$$\Rightarrow AB^2 = AD \times AC$$

51. (D) Sum of all interior angles =  $2 \times$  sum of all exterior angles

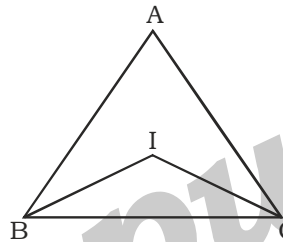
$$\Rightarrow (n - 2) \times 180^\circ = 2 \times 360^\circ$$

$$\Rightarrow (n - 2) \times 180^\circ = 720^\circ$$

$$\Rightarrow (n - 2) = 4 \Rightarrow n = 6$$

$$\Rightarrow \text{Required no. of sides of the polygon} = 6$$

52. (B)



$$\angle ABC = 65^\circ$$

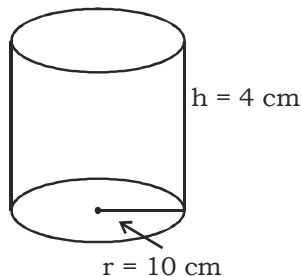
$$\Rightarrow \angle IBC = \frac{\angle ABC}{2} = 32.5^\circ$$

$$\text{Also, } \angle ACB = 55^\circ$$

$$\Rightarrow \angle ICB = \frac{\angle ACB}{2} = 27.5^\circ$$

$$\Rightarrow \angle BIC = 180^\circ - (\angle IBC + \angle ICB) = 180^\circ - 60^\circ = 120^\circ$$

53. (A)



Let radius is increased by  $x$  cm

$$\text{New volume of cylinder} = \pi(10 + x)^2 \times 4$$

Again,

Let the height is increased by  $x$  cm

$$\text{New volume of cylinder} = \pi \times 10^2 \times (4 + x)$$

$$\Rightarrow \pi(10 + x)^2 \times 4 = \pi \times 10^2 \times (4 + x)$$

$$\Rightarrow (10 + x)^2 \times 4 = 100(4 + x)$$

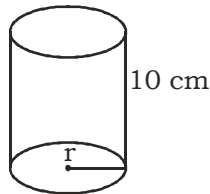
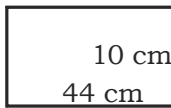
$$\Rightarrow (10 + x)^2 = 25(4 + x)$$

$$\Rightarrow 100 + x^2 + 20x = 100 + 25x$$

$$\Rightarrow x^2 - 5x = 0 \Rightarrow x(x - 5) = 0$$

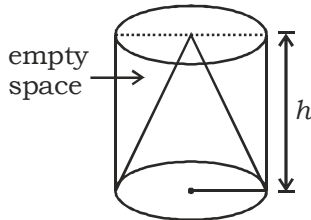
$$\Rightarrow x = 5 \text{ cm}$$

54. (B)



$$\begin{aligned} \text{Volume of the cylinder} &= \pi r^2 h & \Rightarrow 2\pi r &= 44 \text{ cm} \\ &= \pi \times 7^2 \times 10 & \Rightarrow r &= \frac{44 \times 7}{22 \times 2} \text{ cm} \\ &= \frac{22}{7} \times 49 \times 10 & \Rightarrow r &= 7 \text{ cm} \\ &= 1540 \text{ m}^3. \end{aligned}$$

55. (C)



$$\begin{aligned} \text{Volume of water needed to fill the empty space} \\ &= \text{Volume of cylinder} - \text{Volume of cone} \\ &= \pi r^2 h - \frac{1}{3} \pi r^2 h = \frac{2}{3} \pi r^2 h \\ &= 2 \times \left( \frac{1}{3} \pi r^2 h \right) \\ &= 2 \times 27 \pi \text{ cm}^3 \\ &= 54 \pi \text{ cm}^3 \end{aligned}$$

56. (C) T.S.A of prism = C.S.A + 2 × Area of base

$$\begin{aligned} \Rightarrow 608 &= \text{Perimeter of base} \times \text{height} + 2 \times \text{Area of base} \\ \Rightarrow 608 &= 4x \times 15 + 2 \times x^2 \\ &\quad (\text{where } x = \text{side of square}) \\ \Rightarrow x^3 + 30x - 304 &= 0 \\ \Rightarrow (x - 8)(x + 38) &= 0 \\ \Rightarrow x &= 8 \\ \Rightarrow \text{Volume of prism} &= \text{Area of base} \times \text{height} \\ &= 8 \times 8 \times 15 = 960 \text{ cm}^3 \end{aligned}$$

57. (B) Volume of water due to 2 cm rain on a square km land

$$\begin{aligned} &= 1 \text{ km} \times 1 \text{ km} \times 2 \text{ cm} \\ &= 1000 \text{ m} \times 1000 \text{ m} \times \frac{2}{100} \text{ m} \\ &= 20000 \text{ m}^3 \end{aligned}$$

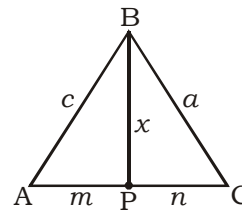
$$\begin{aligned} \Rightarrow 50\% \text{ of volume of rain drops} \\ &= 10000 \text{ m}^3 \end{aligned}$$

Now,

Required level by which the water level in the pool will be increased

$$= \frac{10000 \text{ m}^3}{100 \text{ m} \times 10 \text{ m}} = 10 \text{ m}$$

58. (A)



A.T.Q,

$$AB + BC = 22 \text{ cm}$$

$$AC = 12 \text{ cm}$$

$$\text{Let } BC = a$$

$$AB = c$$

$$AP = m \text{ and } PC = n$$

In  $\triangle ABP$ ,

$$c - m < x < c + m \quad \dots(i)$$

$$a - n < x < a + n \quad \dots(ii)$$

In  $\triangle BPC$

Adding equation (i) and (ii)

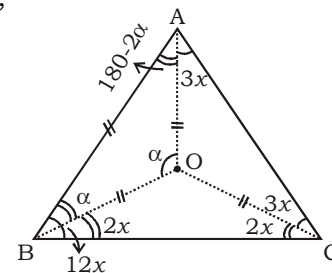
$$(c + a) - (m + n) < 2x < (c + a) + (m + n)$$

$$22 - 12 < 2x < 22 + 12$$

$$5 < x < 17$$

$$\text{Smallest integer value} = 6 \text{ cm}$$

59. (B) ATQ,



In  $\triangle ABC$

$$12x + 180 - 2\alpha + 3x + 5x = 180$$

$$\Rightarrow 20x = 2\alpha$$

$$\Rightarrow 10x = \alpha$$

In  $\triangle OBC$ ,  $\angle B = 2x$

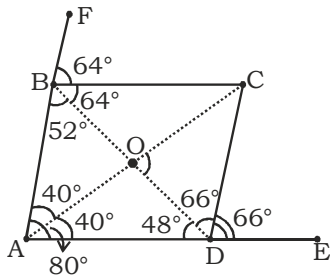
So,  $\triangle ABO$

becomes an equilateral triangle

$$10x = 60^\circ$$

$$x = 6^\circ$$

60. (D)



AD is extended through a point E and AB is extended to a point F  
So,  $\angle ABF = 64^\circ$  and  $\angle ADE = 66^\circ$   
Point C is exterior angle bisector and line AC is angle bisector of  $\angle A$

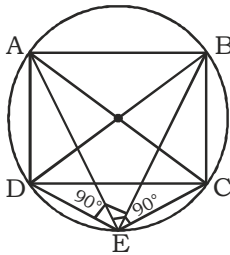
In  $\triangle ACD$

$$\angle C = 180^\circ - 40^\circ - 114^\circ = 26^\circ$$

Now, In  $\triangle COD$

$$= 180^\circ - 66^\circ - 26^\circ = 88^\circ$$

61. (A)



$$\Rightarrow AE^2 + BE^2 + CE^2 + DE^2$$

In  $\triangle AEC$  and  $\triangle DEB$ ,

$$AC^2 = AE^2 + EC^2 \quad \dots(i)$$

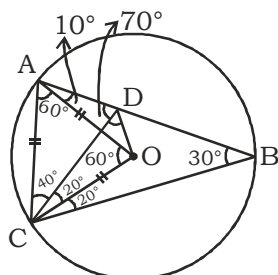
$$BD^2 = BE^2 + DE^2 \quad \dots(ii)$$

Adding equation (i) and (ii)

$$AC^2 + BD^2 = AE^2 + EC^2 + BE^2 + DE^2$$

$$\Rightarrow (8\sqrt{2})^2 + (8\sqrt{2})^2 = AE^2 + EC^2 + BE^2 + DE^2 \\ = 256 \text{ cm}$$

62. (A)



In  $\triangle AOC$

$$\angle O = 60^\circ, \angle O = 60^\circ \text{ and } \angle C = 60^\circ$$

( $\because$  OA = OC = radius)

In  $\triangle CDB$

$$\angle ADC = \angle DCB + \angle DBC = 70^\circ$$

In  $\triangle ADC$

$$\angle A = 180^\circ - (40^\circ + 70^\circ) = 70^\circ$$

Now, in  $\triangle ADO$

$$\angle A = 10^\circ$$

In  $\triangle ADC$

$$\therefore \angle A = 70^\circ \text{ and } \angle D = 70^\circ$$

$$\therefore AC = DC$$

$$\therefore OC = AC$$

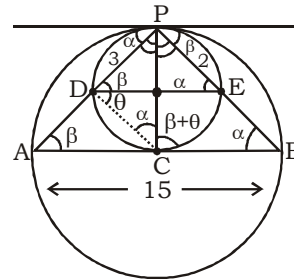
$$\therefore AC = DC = OC$$

So,  $\triangle DOC$  become a Isosceles

Triangle  $\angle DCO = 20^\circ$

$$\text{Now, } \angle D = \angle O = 80^\circ$$

63. (D)



Draw a tangent at point P

Using alternate theorem for smaller circle

If  $\angle P = \alpha$  then  $\angle E = \alpha$  for another side of point P,  $\angle P = \beta$ , then  $\angle D = \beta$

Similarly for larger circle

If  $\angle P = \alpha$  then  $\angle B = \alpha$ , for another side of point P  $\angle P = \beta$  then  $\angle A = \beta$

$\triangle PDE$  and  $\triangle PAB$  become similar triangles

$$\Rightarrow \frac{PD}{PA} = \frac{DE}{AB} = \frac{PE}{PB} \quad \dots(i)$$

Draw a line between points P and C and between points D and C,

Using same arc property

$$\angle PED = \angle PCD$$

By alternate segment

$$\angle PDC = \angle PCB$$

Now,  $\angle DPC = \angle CPB$

Hence, PC becomes an angle bisector  $\angle A$

$$\frac{AC}{BC} = \frac{PA}{PB}$$

From equation (i)

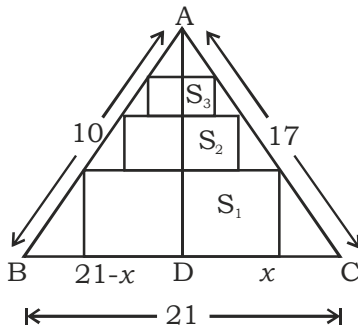
$$\Rightarrow \frac{AC}{BC} = \frac{PD}{PE} = \frac{x}{15-x} = \frac{3}{2}$$

$$\Rightarrow 2x = 45 - 3x$$

$$\Rightarrow AC = x = 9 \text{ cm}$$



64. (C)



$$S_n = \frac{b \times h^n}{(b+h)^n}$$

Let AD = h

$$h^2 = 100 - (21-x)^2 \quad \dots(i)$$

$$h^2 = 17^2 - x^2 \quad \dots(ii)$$

From equation (i) and (ii)

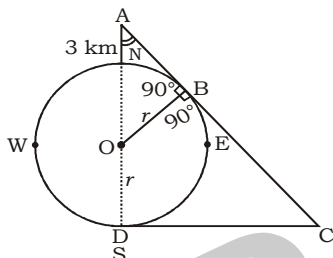
$$\Rightarrow 100 - 441 - x^2 + 42x = 289 - x^2$$

$$\Rightarrow x = 15 \text{ cm}$$

$$\Rightarrow h = 8 \text{ cm}$$

$$S_3 = \frac{21 \times 8^3}{(21+8)^3} = \frac{21 \times 8^3}{29^3}$$

65. (A)



Let, radius r

In  $\triangle ABO$

$$(3+r)^2 - r^2 = AB^2$$

$$\Rightarrow AB = \sqrt{(3+r)^2 - r^2}$$

$\triangle ABO$  and  $\triangle ADC$  are similar triangles

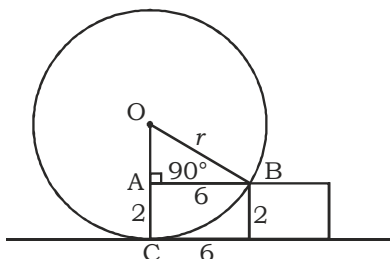
$$\Rightarrow \frac{r}{9} = \frac{\sqrt{(3+r)^2 - r^2}}{3+2r}$$

By options

$$\text{Put } r = \frac{9}{2}$$

Diameter = 9 cm

66. (A) ATQ,



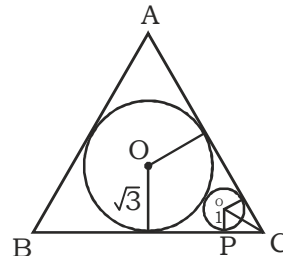
Let OC = r, AO = r - 2 and OB = r

$$r^2 = (r-2)^2 + 36$$

$$\Rightarrow r^2 = r^2 + 4 - 4r + 36$$

$$\Rightarrow r = 10 \text{ cm}$$

67. (C)



$$\Rightarrow r = \frac{6}{2\sqrt{3}} = \sqrt{3}$$

Radius of  $O_1$  circle

$$r = \frac{\sqrt{3}}{3} = \frac{1}{\sqrt{3}}$$

$O_1C$  is a angle bisector of  $\angle C$

Area of  $\triangle O_1PC$

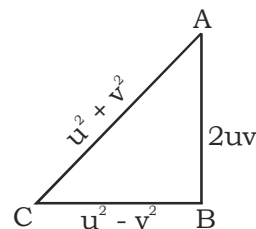
$$= \frac{1}{2} \times \frac{1}{\sqrt{3}} \times 1 \times 2 = \frac{1}{\sqrt{3}}$$

Area of shaded region

$$= \frac{1}{\sqrt{3}} - \frac{\pi r^2}{360} \times 120^\circ$$

$$= \frac{1}{\sqrt{3}} - \frac{\pi}{9}$$

68. (B)



$$AB = \sqrt{(u^2 + v^2)^2 - (u^2 - v^2)^2} = 2uv$$

$$\Rightarrow \frac{1}{2} 2uv \times (u^2 - v^2) = 2016$$

$$\Rightarrow uv(u-v)(u+v) = 2016$$

$$16 \times 126$$

$$32 \times 63$$

$$u \times v(u-v)(u+v) = 16 \times 2 \times 9 \times 7$$

$$u = 9, v = 7$$

$$AB = 2 \times 9 \times 7 = 126$$

$$BC = u^2 - v^2 = 81 - 49 = 32$$

$$AC = u^2 + v^2 = 81 + 49 = 130$$

$$\text{Perimeter of } \triangle ABC = 130 + 32 + 126 = 288 \text{ units}$$

69. (B) A.T.Q,  
Area of 4 - walls  
=  $2h(l + b)$   
=  $2 \times 2.5(6 + 4) \times 5$   
Two rooms have one square window each,  
Now remaining area  
 $\Rightarrow 250 - 2.5 \times 2.5 \times 2 = 237.5$   
Number of cans required =  $\frac{237.5}{20}$   
= 11.87 = 12

70. (B) A.T.Q,  
Let three term of A.P is are  
18K - d, 18K, 18K + d  
End of one year  $\rightarrow 45K \times 1.1 = 49.5K$   
Amount repaid  $\rightarrow \frac{18K - d}{31.5K + d}$   
End of two years  $\rightarrow (31.5K + d) \times 1.1$   
(34.65K + 1.1d)  
Amount repaid  $\rightarrow \frac{18K}{16.65K + 1.1d}$   
End of three years  $\rightarrow (16.65K + 1.1d) \times 1.1$   
(16.65K + 1.1d)  $\times 1.1 = 18K + d$   
 $\Rightarrow 18.315K + 1.21d = 18K + d$   
 $\Rightarrow 0.315K = -0.21d$   
Put K = 1000  
315 = -0.21d  
d = -1500  
18K - d                      18K                      18K + d  
18000 + 1500    18000                      18000 - 1500  
₹ 19,500                      ₹ 18,000                      ₹ 16,500

71. (A) ATQ, 3 years interval  
 $\frac{5000}{4000} = \frac{5}{4}$   
9 years  $\rightarrow$  ₹ 5000  
12 years  $\rightarrow$  ₹  $5000 \times \frac{5}{4}$   
15 years  $\rightarrow$  ₹  $5000 \times \frac{5}{4} \times \frac{5}{4} = ₹ 7812.5$   
Amount = ₹ 7812.5  
For principal  
6 years  $\rightarrow$  ₹ 4000  
3 years  $\rightarrow$  ₹  $4000 \times \frac{4}{5}$   
0 year  $\rightarrow$  ₹  $4000 \times \frac{4}{5} \times \frac{4}{5} = ₹ 2560$

Principal = ₹ 2560  
Amount = ₹ 7812.5  
72. (B) ATQ,  $\sin\theta + \sin\phi = a$ ,  $\cos\theta + \cos\phi = b$   
putting the value  $\theta = 90^\circ$  and  $\phi = 30^\circ$   
 $a = 1 + \frac{1}{2} = \frac{3}{2}$ ,  $b = \frac{\sqrt{3}}{2}$

$$\tan\left(\frac{\theta - \phi}{2}\right) = \tan 30^\circ = \frac{1}{\sqrt{3}}$$

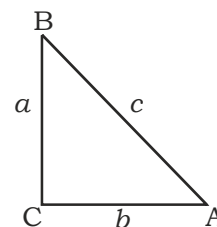
By options,

$$(B) \Rightarrow \frac{\sqrt{4 - a^2 - b^2}}{a^2 + b^2} = \sqrt{\frac{4 - \frac{9}{4} - \frac{3}{4}}{\frac{9}{4} + \frac{3}{4}}} = \frac{1}{\sqrt{3}}$$

73. (B) ATQ,  $\frac{\sec 8A - 1}{\sec 4A - 1} = \frac{1 - \cos 8A}{1 - \cos 4A} \times \frac{\cos 4A}{\cos 8A}$   
 $= \frac{2 \sin^2 4A}{2 \sin^2 2A} \times \frac{\cos 4A}{\cos 8A}$   
 $= \frac{2 \sin 4A \cdot \cos 4A \cdot \sin 4A}{2 \sin^2 2A \cdot \cos 8A}$   
 $= \frac{\sin 8A \times 2 \sin 2A \cos 2A}{\cos 8A \times 2 \sin^2 2A}$   
 $= \tan 8A \cdot \frac{\cos 2A}{\sin 2A} = \frac{\tan 8A}{\tan 2A}$

74. (D) A.T.Q,  
Let the roots of equation  $\alpha$  and  $\beta$   
 $\alpha + \beta = \tan A + \tan B = \frac{a}{b} + \frac{b}{a} = \frac{a^2 + b^2}{ab}$

$$\alpha \beta = \tan A \cdot \tan B = \frac{a}{b} \cdot \frac{b}{a} = 1$$



Then equation,

$$x^2 - (\alpha + \beta)x + \alpha\beta = 0$$

$$x^2 - \left(\frac{a^2 + b^2}{ab}\right)x + 1 = 0$$

$$abx^2 - (a^2 + b^2)x + ab = 0$$

$$abx^2 - c^2x + ab = 0 \quad (\because a^2 + b^2 = c^2)$$

75. (A)  $\tan 5x - \frac{\tan 3x - \tan 2x}{1 - \tan 3x \tan 2x}$   
 $= \tan 5x - \frac{\tan 3x \tan 2x - \tan 3x + \tan 2x}{1 - \tan 3x \tan 2x}$   
 $= \tan 5x \tan 3x \tan 2x = \tan 5x - \tan 3x - \tan 2x$

76. (A)  $\frac{3 - \tan^2 A}{1 - 3 \tan^2 A} = k \Rightarrow \tan^2 A = \frac{k - 3}{3k - 1}$   
 $= \operatorname{cosec} A (3 \sin A - 4 \sin^3 A) = (3 - 4 \sin^2 A)$

$$\Rightarrow 3 - \frac{4}{\operatorname{cosec}^2 A} = 3 - \frac{4}{1 + \cot^2 A}$$

$$\Rightarrow 3 - \frac{4}{1 + \frac{3k-1}{k-3}} = \frac{2k}{k-1}$$

$$\Rightarrow \sin^2 A = \frac{1}{\operatorname{cosec}^2 A} = \frac{1}{1 + \cot^2 A} = \frac{k-3}{4(k-1)}$$

$$0 \leq \sin^2 A \leq 1$$

$$0 \leq \frac{k-3}{4(k-1)} \leq 1 \Rightarrow k \geq \frac{1}{3} \text{ or } k \geq 3$$

77. (D)  $m+n = a(\cos \alpha + \sin \alpha)(\cos^2 \alpha - \cos \alpha \sin \alpha + \sin^2 \alpha)$   
 $+ 3 \cos \alpha \sin \alpha (2 \cos \alpha + \sin \alpha)$   
 $= a(\cos \alpha + \sin \alpha)(1 + 2 \cos \alpha \sin \alpha)$

$$= a(\cos \alpha + \sin \alpha)^3$$

$$m-n = a(\cos \alpha - \sin \alpha)(\cos^2 \alpha + \cos \alpha \sin \alpha + \sin^2 \alpha)$$

$$- 3 \cos \alpha \sin \alpha (\cos \alpha - \sin \alpha)$$

$$= a(\cos \alpha - \sin \alpha)(1 - 2 \sin \alpha \cos \alpha)$$

$$= a(\cos \alpha - \sin \alpha)^3$$

$$= (m+n)^{2/3} + (m-n)^{2/3}$$

$$= a^{2/3}(1 + 2 \sin \alpha \cos \alpha) + a^{2/3}(1 - 2 \sin \alpha \cos \alpha)$$

$$= 2a^{2/3}$$

78. (D)  $\cos(\theta - \alpha), \cos \theta, \cos(\theta + \alpha)$  in h.p.  
 Then,

$$\Rightarrow \cos \theta = \frac{2 \cos(\theta - \alpha) \cdot \cos(\theta + \alpha)}{\cos(\theta - \alpha) + \cos(\theta + \alpha)}$$

$$\Rightarrow \cos \theta = \frac{\cos 2\theta + \cos 2\alpha}{2 \cos \theta \cdot \cos \alpha}$$

$$\Rightarrow 2 \cos^2 \theta \cdot \cos \alpha = 2 \cos^2 \theta - 1 + \cos 2\alpha$$

$$\Rightarrow 2 \cos^2 \theta (\cos \alpha - 1) = -1 + 1 - 2 \sin^2 \alpha$$

$$\Rightarrow 2 \cos^2 \theta \left[ 1 - 2 \sin^2 \frac{\alpha}{2} - 1 \right] = -2 \sin^2 \alpha$$

$$\Rightarrow 2 \cos^2 \theta \left( -2 \sin^2 \frac{\alpha}{2} \right) = -2.4 \sin^2 \frac{\alpha}{2} \cdot \cos^2 \frac{\alpha}{2}$$

$$\Rightarrow \cos^2 \theta = 2 \cos^2 \frac{\alpha}{2}$$

$$\Rightarrow \cos^2 \theta \cdot \sec^2 \frac{\alpha}{2} = 2$$

$$\Rightarrow \cos \theta \cdot \sec \frac{\alpha}{2} = \pm \sqrt{2}$$

79. (D)  $\sin A + \sin B = x$   
 $\sin^2 A + \cos^2 A + 2 \sin A \cdot \cos A = x^2$   
 $2 \sin A \cdot \cos A = x^2 - 1$   
 we know that,  
 $\sin^6 A + \cos^6 A = 1 - 3 \sin^2 A \cdot \cos^2 A$

$$\frac{1}{4} (4 - 3(x^2 - 1)^2) = 1 - \left( \frac{x^2 - 1}{2} \right)^2$$

$$1 - \frac{3}{4} (x^2 - 1)^2 = 1 - \frac{3}{4} (x^2 - 1)^2$$

L.H.S = R.H.S

Hence, for all values of  $x$  are true

But  $\sin A + \cos A = x$

$$\text{So, } -\sqrt{2} \leq x \leq \sqrt{2} \Rightarrow x^2 \leq 2$$

80. (A)

	Person I	Person II
MRP	→ ₹ 28000	₹ 20000 + ₹ 8000
Discount	₹ 2800	₹ 2400 + ₹ 640
		₹ 3040

Difference between selling price  
 $= ₹ 3040 - ₹ 2800 = ₹ 240$

81. (D) A.T.Q,

A	:	B	:	C	
SP	8	:	9	:	5
Profit%	8	:	7	:	14

8 units → 14.28%

$$\downarrow \frac{1}{7} \text{ CP} = 7 \text{ units}$$

$$\text{SP} = 8 \text{ units}$$

7 units → 12.50%

$$\downarrow \frac{1}{8} \text{ SP} = 9 \text{ units}$$

$$\text{CP} = 8 \text{ units}$$

14 units → 25%

$$\downarrow \frac{1}{4} \text{ CP} = 4 \text{ units}$$

$$\text{SP} = 5 \text{ units}$$

A : B : C  
 CP - 7 : 8 : 4  
 Total CP = 19 units  
 Total SP = 22 units

$$\text{Profit \%} = \frac{3}{19} \times 100 = 15 \frac{15}{19} \%$$

82. (C) Alcohol      Water

$$\begin{array}{cc|l} 5 & 9 & \times 1 \\ 2 & 5 & \times 2 \\ \hline \text{Now, New ratio is-} \\ \text{Alcohol} & \text{Water} \\ 1\left(\frac{5}{4}\right) & 9 & \\ & 10 & \end{array}$$

Here, mixture to be taken out =  $\frac{1}{5}$

Now,  $\frac{1}{5}$  unit = 5 litres

Then, total quantity = 1 unit  
=  $5 \times 5 = 25$  litres

83. (C) A.T.Q,

$$1M = 2C$$

and,

$$(4M + 5W + 6C) \times 15 = (2M + 3W + 2C) \times 31$$

$$\Rightarrow (7M + 5W) \times 15 = (3M + 3W) \times 31$$

On solving, we get

$$4M = 6W$$

Then, the ratio of capacity of man, woman and child =  $6 : 4 : 3$

Let 1 man, 1 woman and 1 child can complete the work in  $x$  days.

Then,

$$(6 \times 4 + 4 \times 5 + 6 \times 3) \times 15$$

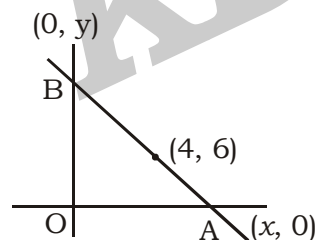
$$= (6 + 4 + 3) \times x$$

$$\Rightarrow 62 \times 15 = 13x$$

$$\Rightarrow x = \frac{930}{13} = 71 \frac{7}{13} \text{ days}$$

$\therefore$  Required number of days =  $71 \frac{7}{13}$  days

84. (B) Let the coordinates of A and B be  $(x, 0)$  and  $(0, y)$  respectively.



Now, using mid point formula, we get,

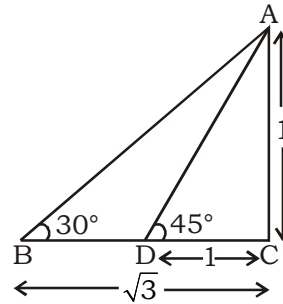
$$\frac{x+0}{2} = 4 \Rightarrow x = 8$$

$$\text{and, } \frac{y+0}{2} = 6 \Rightarrow y = 12$$

Then, area of  $\Delta OAB = \frac{1}{2} \times x \times y$

$$= \frac{1}{2} \times 8 \times 12 = 48 \text{ sq. units}$$

85. (A) A.T.Q,



$$BD = 20 \text{ m}$$

Now,

$$(\sqrt{3} - 1) \text{ units} = 20 \text{ m}$$

Then, height of the lamp post

$$1 \text{ unit} = \frac{20}{\sqrt{3} - 1} \text{ m} = 10(\sqrt{3} + 1) \text{ m}$$

$\therefore$  Height of the lamp post =  $10(\sqrt{3} + 1) \text{ m}$

86. (C) Total age of couple at the time of marriage =  $23 \times 2 = 46$  years

and, total age of family at the time birth of first child =  $16 \times 3 = 48$  years

and, total age of family at the time of birth of second child =  $15 \times 4 = 60$  years

$$\text{Here, age of the first child} = \frac{60 - 48}{3}$$

$$= 4 \text{ years}$$

Now,

$$\text{total age of family} = 20 \times 4 = 80 \text{ years}$$

$$\text{then, age of the first child} = 4 + \frac{80 - 60}{4}$$

$$= 4 + 5 = 9 \text{ years}$$

87. (A) A.T.Q,

	upstream	downstream
Time	3	1
Speed	1	3

$$\text{Speed of man in still water} = \frac{1+3}{2} = 2 \text{ units}$$

$$\text{and, speed of current} = \frac{3-1}{2} = 1 \text{ unit}$$

Then,

$$\text{Now, speed of man (2 units)} = \frac{23}{3} \text{ kmph}$$

$$\text{Then, speed of current (1 unit)}$$

$$= \frac{23}{3} \times \frac{1}{2} = \frac{23}{6} = 3 \frac{5}{6} \text{ kmph}$$

88. (B) Let length, breadth and height of the cuboid be  $4x$ ,  $2x$  and  $x$  respectively.  
Then, volume of the cuboid  
 $= 4x \times 2x \times x = 8x^3$   
After changes, the dimensions of the cuboid becomes  $2x$ ,  $4x$  and  $\frac{x}{2}$  respectively.  
Then,

$$\text{Volume of the cuboid} = 2x \times 4x \times \frac{x}{2} = 4x^3$$

$\therefore$  Required percentage change

$$= \frac{8x^3 - 4x^3}{8x^3} \times 100\% = 50\%$$

89. (D) A.T.Q,

$$x^2 - \sqrt{3}x - 1 = 0$$

$$\Rightarrow x - \frac{1}{x} = \sqrt{3} \dots\dots\dots (i)$$

We know that,

$$\left(x + \frac{1}{x}\right)^2 - \left(x - \frac{1}{x}\right)^2 = 4$$

Then,

$$x + \frac{1}{x} = \sqrt{7} \dots\dots\dots (ii)$$

Multiply equation (i) and (ii), we get

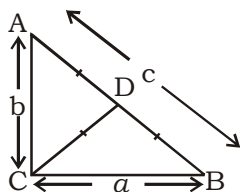
$$x^2 - \frac{1}{x^2} = \sqrt{21}$$

Taking cube both sides, we get

$$x^6 - \frac{1}{x^6} - 3\left(x^2 - \frac{1}{x^2}\right) = 21\sqrt{21}$$

$$\Rightarrow x^6 - \frac{1}{x^6} = 24\sqrt{21}$$

90. (D) We know that,



Circumradius of a right angle triangle is equal to half of its hypotenuse.

Then,

$$c = 52 \times 2 = 104 \text{ cm}$$

Now,

$$\text{perimeter of ABC} = 112 \times 2$$

$$\Rightarrow a + b + c = 224 \text{ cm}$$

$$\Rightarrow a + b = 120 \text{ cm}$$

and,

$$(a + b)^2 = 120^2$$

$$\Rightarrow a^2 + b^2 + 2ab = 120^2$$

$$\Rightarrow 2ab = 120^2 - c^2$$

$$\Rightarrow 2ab = 120^2 - 104^2$$

$$\Rightarrow 2ab = 16 \times 224$$

Then,

$$\text{Area of ABC} = \frac{1}{2} ab$$

$$= \frac{16 \times 224}{4} = 896 \text{ cm}^2$$

91. (B) Graduate male population of state

$$A = \left(24 \times \frac{16}{100} \times \frac{7}{12}\right) \text{ lakh} = 2.24 \text{ lakh}$$

XII std male population of state A

$$= \left(32 \times \frac{15}{100} \times \frac{7}{16}\right) \text{ lakh} = 2.1 \text{ lakh}$$

$\therefore$  Required difference =  $(2.24 - 2.1)$  lakh = 14000

92. (D) Graduate female population of state

$$E = 24 \times \frac{20}{100} \times \frac{7}{16} = 2.1 \text{ lakh}$$

XII std femle population of state

$$D = 32 \times \frac{12}{100} \times \frac{7}{12} = 2.24 \text{ lakh}$$

$\therefore$  Required ratio =  $2.1 : 2.24$   
 $= 210 : 225 = 15 : 16$

93. (C) Graduate female population of state

$$C = 24 \times \frac{15}{100} \times \frac{4}{9} = 1.6 \text{ lakh}$$

XII std female population of state

$$C = 32 \times \frac{18}{100} \times \frac{5}{9} = 3.2 \text{ lakh}$$

$\therefore$  Required percentage

$$= \frac{1.6}{3.2} \times 100\% = 50\%$$

94. (A) XII std pass male population of state

$$C = 32 \times \frac{18}{100} \times \frac{4}{9} = 2.56 \text{ lakh}$$

$\therefore$  Required percentage

$$= \frac{2.56}{32} \times 100\% = 8\%$$

95. (D) Graduate male population of state

$$E = 24 \times \frac{20}{100} \times \frac{9}{16} = 2.7 \text{ lakh}$$

XII std pass female population of state

$$E = 32 \times \frac{19}{100} \times \frac{10}{19} = 3.2 \text{ lakh}$$

∴ Required ratio = 27 : 32

96. (C) Total numbers of obese men in 2007

$$66000 \times 35\% = 23100$$

Total number of obese women in

$$2007 = 54000 \times 25\% = 13500$$

Total numbers of obese children in 2007

$$16000 \times 12.5\% = 2000$$

Required average

$$= (23100 + 13500 + 2000) \div 3$$

$$= 38600 \div 3 = 12867$$

97. (B) Required percentage

$$= \frac{78000 \times 37.5\%}{78000 \times 62.5\%} \times 100 = 60\%$$

98. (D) Required ratio

$$= \frac{60000 \times 20\%}{70000 \times 27.5\%} \times 100 = 48 : 77$$

99. (A) No. of obese women in 2006

$$= 20\% \text{ of } 60000 = 12000$$

Numbers of obese children in 2006

$$= 25\% \text{ of } 12000 = 3000$$

Numbers of obese men in

$$2006 = 32.5\% \text{ of } 63000 = 20475$$

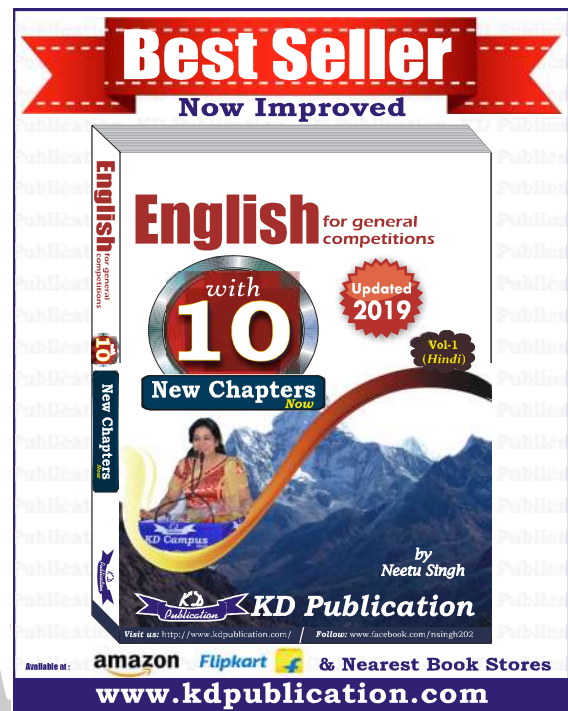
$$\text{Required difference} = 20475 - (12000 + 3000) = 20475 - 15000 = 5475$$

100. (D) Number of children not suffering from

obesity in 2005 = 90% of 21000 = 18900

Number of children not in 2004 = 85% of = 15000

Total of these two equals to 31650.



**SSC TIER II (MATHS) MOCK TEST - 50 (ANSWER KEY)**

1. (A)	11. (A)	21. (B)	31. (A)	41. (D)	51. (D)	61. (A)	71. (A)	81. (D)	91. (B)
2. (D)	12. (D)	22. (B)	32. (C)	42. (A)	52. (B)	62. (A)	72. (B)	82. (C)	92. (D)
3. (B)	13. (D)	23. (B)	33. (D)	43. (D)	53. (A)	63. (D)	73. (B)	83. (C)	93. (C)
4. (B)	14. (D)	24. (D)	34. (B)	44. (D)	54. (B)	64. (C)	74. (D)	84. (B)	94. (A)
5. (C)	15. (C)	25. (C)	35. (C)	45. (D)	55. (C)	65. (A)	75. (A)	85. (A)	95. (D)
6. (D)	16. (B)	26. (A)	36. (B)	46. (B)	56. (C)	66. (A)	76. (A)	86. (C)	96. (C)
7. (C)	17. (B)	27. (D)	37. (C)	47. (D)	57. (B)	67. (C)	77. (D)	87. (A)	97. (B)
8. (D)	18. (A)	28. (A)	38. (B)	48. (D)	58. (A)	68. (B)	78. (D)	88. (B)	98. (D)
9. (D)	19. (C)	29. (C)	39. (B)	49. (D)	59. (B)	69. (B)	79. (D)	89. (D)	99. (A)
10. (A)	20. (C)	30. (B)	40. (C)	50. (B)	60. (D)	70. (B)	80. (A)	90. (D)	100. (D)

**Note:- If your opinion differs regarding any answer, please message the mock test and question number to 8860330003**

**Note:- Whatsapp with Mock Test No. and Question No. at 7053606571 for any of the doubts. Join the group and you may also share your suggestions and experience of Sunday Mock**

**Note:- If you face any problem regarding result or marks scored, please contact 9313111777**