

TEST NO.
51

SSC Mains (Maths) Answer with Explanation

1. (D) Total number of marbles kept in 50th box,
= sum of factors of 50
= $1 + 2 + 5 + 10 + 25 + 50 = 93$
2. (C) A.T.Q,
 $\therefore (x^2 - y^2) + (y^2 - z^2) + (z^2 - x^2) = 0$
 $\therefore (x^2 - y^2)^3 + (y^2 - z^2)^3 + (z^2 - x^2)^3$
= $3(x^2 - y^2)(y^2 - z^2)(z^2 - x^2)$
 $\therefore (x - y) + (y - z) + (z - x) = 0$
 $\therefore (x - y)^3 + (y - z)^3 + (z - x)^3$
= $3(x - y)(y - z)(z - x)$
$$\Rightarrow \frac{(x^2 - y^2)^3 + (y^2 - z^2)^3 + (z^2 - x^2)^3}{(x - y)^3 + (y - z)^3 + (z - x)^3}$$

= $\frac{3(x^2 + y^2)(y^2 - z^2)(z^2 - x^2)}{3(x - y) + (y - z)(z - x)}$
= $\frac{3(x + y)(x - y)(y + z)(y - z)(z + x)(z - x)}{3(x + y)(y - z)(z - x)}$
= $(x + y)(y + z)(z + x)$
3. (A) Let the two digits number be $10y + x$ where $x > y$
 $\therefore 10x + y - 10y - x = 63$
 $\Rightarrow 9x - 9y = 63$
 $\Rightarrow x - y = 7$
 $\therefore x = 7, 8, 9$ and $y = 0, 1, 2$
 \therefore possible values of x are 7, 8, 9
4. (A) For every $n \geq 4$;
 $n!$ will be divisible by 8
 \Rightarrow remainder will be zero
[becomes for $n \geq 4$, 8 will be a factor of $n!$]
So, remainder of $1! + 2! + 3! + 4! + \dots + 100!$ will be equal to the remainder of $1! + 2! + 3!$ only
 $1! + 2! + 3! = 1 + 2 + 3$
and $\frac{9}{8}$; $R = 1$
5. (D) H.C.F = A and L.C.M = B
 $\Rightarrow A \times B = x \times y$
So, $A^3 + B^3 = (A + B)^3 - 3AB(A + B)$
= $(x + y)^3 - 3xy(x + y)$
= $x^3 + y^3 + 3xy(x + y) - 3xy(x + y)$
= $x^3 + y^3$
6. (A) $(x)^{\frac{1}{2}} = (y)^{\frac{1}{3}} \Rightarrow (x)^{\frac{1}{1} \times 3} = (y)^{\frac{1}{1} \times 2} = (x)^3 = (y)^2$
7. (C) Required average age of 2 persons

- $$= \frac{30 + 34 + (8 \times 3)}{2} = 44 \text{ years}$$
8. (A) Required average age just before the birth of the youngest member
$$= \frac{(10 \times 20) - (10 \times 10)}{10 - 1} = \frac{100}{9} = 11.11 \text{ years}$$
 9. (A) A.T.Q,
$$x = \frac{\sqrt{240}}{\sqrt{5} + \sqrt{3}} = \frac{\sqrt{20}\sqrt{12}}{\sqrt{5} + \sqrt{3}}$$

$$\frac{x}{\sqrt{20}} = \frac{\sqrt{12}}{\sqrt{5} + \sqrt{3}} = \frac{2\sqrt{3}}{\sqrt{5} + \sqrt{3}}$$

(Using componendo and dividendo)
$$\frac{x + \sqrt{20}}{x - \sqrt{20}} = \frac{2\sqrt{3} + \sqrt{5} + \sqrt{3}}{2\sqrt{3} - \sqrt{5} - \sqrt{3}}$$

$$\frac{x + \sqrt{20}}{x - \sqrt{20}} = \frac{3\sqrt{3} + \sqrt{5}}{\sqrt{3} - \sqrt{5}} \dots (i)$$

$$\frac{x}{\sqrt{12}} = \frac{\sqrt{20}}{\sqrt{5} + \sqrt{3}}$$

(Using componendo and dividendo)
$$\frac{x + \sqrt{12}}{x - \sqrt{12}} = \frac{2\sqrt{5} + \sqrt{5} + \sqrt{3}}{2\sqrt{5} - \sqrt{5} - \sqrt{3}}$$

$$\frac{x + \sqrt{12}}{x - \sqrt{12}} = \frac{3\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}} \dots (ii)$$

Adding equation (i) and (ii)
$$\frac{x + \sqrt{20}}{x - \sqrt{20}} + \frac{x + \sqrt{12}}{x - \sqrt{12}} = \frac{3\sqrt{3} + \sqrt{5}}{\sqrt{3} - \sqrt{5}} + \frac{3\sqrt{5} + \sqrt{3}}{\sqrt{5} - \sqrt{3}}$$

$$= \frac{3\sqrt{3} + \sqrt{5} - 3\sqrt{5} - \sqrt{3}}{\sqrt{3} - \sqrt{5}}$$

$$= \frac{2\sqrt{3} - 2\sqrt{5}}{\sqrt{3} - \sqrt{5}} = \frac{2(\sqrt{3} - \sqrt{5})}{(\sqrt{3} - \sqrt{5})} = 2$$
 10. (A) Average speed = $\frac{\text{Total distance covered}}{\text{Total time taken}}$
$$= \frac{(6 + 8 + 40) \text{ km}}{(15 + 15 + 15) \text{ min}} = \frac{54 \text{ km}}{45 \text{ min}} = \frac{54 \text{ km}}{60 \text{ hr}}$$

= 72 km/hr

11. (C) Age of the captain
 $= (11 \times 30) - \{(5 \times 29) + (5 \times 27)\}$
 $= (330 - 280) \text{ years} = 50 \text{ years}$
12. (B) $(2m + 4b) \times 10 = (4m + 5b) \times 6$
 $\Rightarrow 20m + 40b = 24m + 30b$
 $\Rightarrow 4m = 10b \Rightarrow 2m = 5b$
 So, $5b = 2 \times 40$
 $\Rightarrow b = \frac{2 \times 40}{5} = 16$
 \therefore Required ratio = $40 : 16 = 5 : 2$
13. (B) **In case I.**
 Let the number of shirts of brand B be x .
 Let the cost of a shirt of brand B be ₹ 1
 \therefore Original cost = $4 \times 2 + x = (8 + x)$
In case II.
 $4 + 2x = (8 + x) \times \frac{140}{100} = (8 + x) \frac{7}{5}$
 $\Rightarrow 20 + 10x = 56 + 7x$
 $\Rightarrow 10x - 7x = 56 - 20 = 36$
 $\Rightarrow 3x = 36 \Rightarrow x = 12$
 \therefore Required ratio = $4 : 12 = 1 : 3$
14. (C) Half the sum = 18
 \Rightarrow total sum = 36
 \Rightarrow Nos. will be 6, 12 and 18
 So, ratio of squares = $6^2 : 12^2 : 18^2$
 $= 36 : 144 : 324$
15. (B) A.T.Q,
 $\frac{N}{6} = \frac{R}{4} = \frac{S}{5}$
 $\Rightarrow N : R : S$
 $= 6 : 4 : \frac{5}{2}$
 $= 12 : 8 : 5$
 \Rightarrow Neelam's share
 $= \frac{12}{(12 + 8 + 5)} \times 2250 = ₹ 1080$
16. (A) S.P at 20% profit = ₹ 9/ litres
 \Rightarrow Cost of mixture = $\frac{9}{120} \times 100$
 $= ₹ 7.5/\text{litres}$
 Now, let the ratio of milk and water in the mixture = $x : y$
 $\Rightarrow \frac{(10 \times x) + (0 \times y)}{x + y} = 7.5$
 $\Rightarrow 10x = 7.5(x + y)$
 $\Rightarrow 2.5x + 7.5y$
 $\Rightarrow x = 3y$
 $\Rightarrow x : y = 3 : 1$
17. (D) Ratio of equivalent capitals of A, B and C for 1 month,
 $= (40500 \times 6 + 45000 \times 6) : (45000 \times 12)$
 $: (60000 \times 6 + 45000 \times 6)$
 $= (405 + 450) : (450 \times 2) : (600 + 450)$
 $= 855 : 900 : 1050$
 $= 171 : 180 : 210$
 $= 57 : 60 : 70$
 Sum the ratio = $57 + 60 + 70 = 187$
 Required difference = $\frac{70 - 57}{187} = 56100$
 $= \frac{13}{187} \times 56100 = ₹ 3900$
18. (A) Let the cost price of 1 orange = ₹ 1
 \therefore C.P of 1 banana = ₹ $\frac{3}{4}$
 and C.P of 1 apple = ₹ $\frac{3}{2}$
 New price:
 1 orange = ₹ 1.1
 1 banana = $\frac{3}{4} \times \frac{110}{100} = ₹ 0.825$
 1 apple = $\frac{3}{2} \times \frac{110}{100} = ₹ 1.65$
 \therefore Original price of (4 bananas + 2 apples + 3 oranges)
 $= ₹ (3 + 3 + 3) = ₹ 9$
 $= ₹ (3.3 + 3.3 + 3.3) = 9.9$
 \therefore Percentage increase
 $= \frac{9.9 - 9}{9} \times 100 = 10\%$
19. (A) Let the number be x
 \Rightarrow % change
 $= \frac{\text{original result} - \text{changed result}}{\text{original result}} \times 100\%$
 $= \frac{5x - \frac{x}{5}}{5x} \times 100\% = \frac{25x - x}{25x} \times 100\%$
 $= \frac{24x}{25x} \times 100\% = 96\%$
20. (C) 20% decrease in price
 \Rightarrow 25% increase in consumption
 (when expenditure is constant)
 \Rightarrow increased amount of sugar = 25% of 20kg
 $= 5 \text{ kg}$
 \Rightarrow Total amount now of sugar = $(20 + 5) \text{ kg}$
 $= 25 \text{ kg}$

21. (C) Votes got by Candidate A
- $$= (100 - 10)\% \text{ of } \frac{4}{5} \text{ of total voters}$$
- $$= 90\% \text{ of } \frac{4}{5} \text{ of total voters}$$
- $$= \frac{9}{10} \times \frac{4}{5} \text{ of total voters}$$
- $$= \frac{18}{25} \text{ of total voters}$$
- $$= 216 \text{ voters} \quad \dots(i)$$
- Now, votes got by Candidate B
- $$= (100 - 20)\% \text{ of } \left(1 - \frac{4}{5}\right) \text{ th of the total voters}$$
- $$= 80\% \text{ of } \frac{1}{5} \text{ th of total voters}$$
- $$= \frac{4}{5} \times \frac{1}{5} \text{ of total voters}$$
- $$= \frac{4}{25} \text{ of total voters}$$
- $$= \frac{216}{18} \times 4 = 48 \text{ voters}$$

- So, total number of votes polled
 = (216+48) votes = 264 votes
22. (D) $\cos x = \frac{2 \cos y - 1}{2 - \cos y}$
- Let $y = 60^\circ$
- $$\cos x = \frac{2 \times \frac{1}{2} - 1}{2 - \frac{1}{2}}$$
- $$\Rightarrow x = 90^\circ$$
- Then,
- $$\tan\left(\frac{x}{2}\right) \cot\left(\frac{y}{2}\right) = \tan 45^\circ \cot 30^\circ = \sqrt{3}$$

23. (C) If the C.P of wrist watch be ₹ x then
 C.P of wall clock = ₹ (390 - x)
- $$\text{So, } \frac{x \times 10}{100} + \frac{(390 - x) \times 15}{100} = 51.50$$
- $$\Rightarrow 10x + 5850 - 15x = 5150$$
- $$\Rightarrow 5x = 5850 - 5150 = 700$$
- $$\Rightarrow x = \frac{700}{5} = ₹ 140$$

- $$\therefore \text{C.P of wall clock} = 390 - 140 = ₹ 250$$
- $$\therefore \text{Required difference} = 250 - 140 = ₹ 110$$
24. (A) $\therefore (40 - 20)\% = ₹ 1$

- $$\text{So, } 120\% = \frac{1}{20} \times 120 = ₹ 6$$
25. (B) Required Marked price
- $$= 210 \times \frac{120}{100} \times \frac{100}{(100 - 12.5)}$$
- $$= 210 \times \frac{120}{87.5} = ₹ 288$$

26. (D) Let the C.P = x
- So, S.P in 1st case = $1.05x$
 now, C.P in 2nd case = $0.95x$
 and S.P in 2nd case = $1.05x - 2$
- Now, A.T.Q,
- $$0.95x \times 1.1 = 1.05x - 2$$
- $$\text{or, } 1.045x = 1.05x - 2$$
- $$\Rightarrow 1.05x - 1.045x = 2$$
- $$\Rightarrow 0.005x = 2$$
- $$\Rightarrow x = \frac{2}{0.005} = ₹ 400$$

27. (C) Discount on ₹ 36000 = $\frac{36000 \times 7}{100} = ₹ 2520$
- $$\text{Discount on first ₹ 20,000} = \frac{20000 \times 8}{100} = ₹ 1600$$
- $$\text{Discount on next ₹ 10,000} = \frac{10,000 \times 5}{100} = ₹ 500$$
- $$\therefore \text{Discount on remaining ₹ 6,0000} = 2520 - (1600 + 500) ₹ 420$$
- $$\therefore \text{Required percent} = \frac{420 \times 100}{6000} = 7\%$$

28. (A) A.T.Q,
- $$\sin^2 \alpha + \sin^2 \beta + \cos^2 \gamma = 3$$
- Let $\alpha = \beta = 90^\circ$ and $\gamma = 0^\circ$
- $$\tan\left(\frac{\alpha + \beta + \gamma}{4}\right) + \cot\left(\frac{\alpha + \beta + \gamma}{4}\right)$$
- $$= \tan\left(\frac{180^\circ}{4}\right) + \cot\left(\frac{180^\circ}{4}\right)$$
- $$= \tan 45^\circ + \cot 45^\circ$$
- $$= 1 + 1 = 2$$

29. (D) A.T.Q,

$$4\cos 20^\circ - \sqrt{3} \cot 20^\circ = 4 \cos 20^\circ -$$

$$\sqrt{3} \frac{\cos 20^\circ}{\sin 20^\circ}$$

$$= \frac{4 \sin 20^\circ \cos 20^\circ - \sqrt{3} \cos 20^\circ}{\sin 20^\circ}$$

$$= \frac{2.2 \sin 20^\circ \cos 20^\circ - \sqrt{3} \cos 20^\circ}{\sin 20^\circ}$$

$$= \frac{2 \sin 40^\circ - \sqrt{3} \cos 20^\circ}{\sin 20^\circ}$$

$$= \frac{2 \left[\sin 40^\circ - \frac{\sqrt{3}}{2} \cos 20^\circ \right]}{\sin 20^\circ}$$

$$= \frac{2 [\sin 40^\circ - \sin 60^\circ \cos 20^\circ]}{\sin 20^\circ}$$

$$= \frac{2 \sin 40^\circ - 2 \sin 60^\circ \cos 20^\circ}{\sin 20^\circ}$$

$$= \frac{2 \sin 40^\circ - \sin 80^\circ - \sin 40^\circ}{\sin 20^\circ}$$

$$= \frac{\sin 40^\circ - \sin 80^\circ}{\sin 20^\circ}$$

$$= \frac{2 \cos 60^\circ \cdot (-\sin 20^\circ)}{\sin 20^\circ} = -1$$

30. (D) Let x be the required annual payment
So, also, $r = 10\%$ p.a and $t = 3$ years

$$\left[1 \xrightarrow{+10\%} 1.1 \right]$$

$$\text{So, } (1 + 1.1 + 1.21)x = 3310 \times (1.1)^3$$

$$\text{or, } 3.31x = 3310 \times 1.331$$

$$x = \frac{3310 \times 1.331}{3.31} = ₹ 1331$$

31. (C) $A = P \left(1 + \frac{R}{100} \right)^T$

$$\Rightarrow 3 = 1 \left(1 + \frac{R}{100} \right)^3$$

On squaring both sides,

$$9 = 1 \left(1 + \frac{R}{100} \right)^6$$

32. (A) Cash price of refrigerator

$$= 1500 + \left(1020 \times \frac{10}{11} \right) + \left(1003 + \frac{100}{121} \right) + \left(990 \times \frac{1000}{1331} \right)$$

$$= 1500 + \left\{ \frac{(10200 \times 121) + (100300 \times 11) + 990000}{1331} \right\}$$

$$= 1500 + \left(\frac{1234200 + 1103300 + 990000}{1331} \right)$$

$$= 1500 + \frac{3327500}{1331}$$

$$= 1500 + 2500 = ₹4000$$

33. (D) When B works normally then days taken by B to complete the work

$$= \frac{20 \times 12}{20 - 12} \text{ days} = 30 \text{ days}$$

Now, If B does the work only half a day daily,

\Rightarrow B will take twice the total days to complete the whole work alone

\Rightarrow Now number of days taken by B,

$$= (30 \times 2) \text{ days} = 60 \text{ days}$$

So, Now days taken by (A + B) together

$$\text{to do the whole work} = \frac{20 \times 60}{20 + 60} = 15 \text{ days}$$

34. (A) A.T.Q,

$$u_n = \cos^n \delta + \sin^n \delta$$

$$2u_6 - 3u_4 + 2 = 2(\cos^6 \delta + \sin^6 \delta) - 3(\cos^4 \delta + \sin^4 \delta) + 2$$

$$\text{Let } \delta = 0^\circ$$

$$2 - 3 + 2 = 1$$

35. (C) Let days taken by A to do the whole work = x days

So, days taken by B to do the whole work = $(x - 5)$ days

and, days taken by C to do the whole work = $(x - 9)$ days

Now, A.T.Q,

Days taken by (A + B) together to do the whole work = Days taken by C alone to do the whole work

$$\Rightarrow \frac{x(x - 5)}{x + (x - 5)} = x - 9$$

$$\text{or, } x^2 - 5x = (x - 9)(2x - 5)$$

$$\text{or, } x^2 - 5x = 2x^2 - 5x - 18x + 45$$

$$\text{or, } x^2 - 18x + 45 = 0$$

$$\text{or, } x^2 - 15x - 3x + 45 = 0$$

$$\text{or, } x(x - 15) - 3(x - 15) = 0$$

$$\text{or } (x - 3)(x - 15) = 0 \Rightarrow x = 3 \text{ or } 15$$

but $x = 3$ is not possible as $x - 5$ or $x - 9$ will become negative.

So, $x = 15$ days

36. (B) Time $\propto \frac{1}{\text{cross-sectional area of the pipe}}$

$$\text{Time} \propto \frac{1}{\frac{\pi}{4}d^2}$$

$$\text{Time} \propto \frac{1}{d^2}$$

$$\therefore \frac{t_2}{t_1} = \frac{(d_1)^2}{(d_2)^2}$$

$$\text{So, } t_2 = t_1 \left(\frac{d_1}{d_2} \right)^2$$

$$t_1 = 40 \text{ minutes, } d_1 = d, d_2 = 2d$$

$$\therefore t_2 = 40 \left(\frac{d}{2d} \right)^2$$

$$t_2 = 40 \left(\frac{1}{2} \right)^2$$

$$t_2 = 10 \text{ minutes}$$

\Rightarrow time taken by a pipe of diameter $2d$ for doing the same job = 10 minutes

37. (C) Let the capacity of the tank be x gallons. Quantity of water filled in the tank in 1 minutes when all the pipes A, B and C

$$\text{are opened simultaneously} = \frac{x}{20} + \frac{x}{24} - 3$$

$$\text{According to the question, } \frac{x}{20} + \frac{x}{24} - 3$$

$$= \frac{x}{15}$$

$$\Rightarrow \frac{x}{20} + \frac{x}{24} - \frac{x}{15} = 3$$

$$\Rightarrow \frac{6x + 5x - 8x}{120} = 3$$

$$\Rightarrow 3x = 3 \times 120$$

$$\Rightarrow x = \frac{3 \times 120}{3} = 120 \text{ gallons}$$

38. (A) A.T.Q,

$$\sec^2 \theta = \frac{4xy}{(x+y)^2}$$

$$\cos^2 \theta = \frac{(x+y)^2}{4xy}$$

$$0 \leq \cos^2 \theta \leq 1$$

$$\frac{(x+y)^2}{4xy} \leq 1$$

$$\frac{(x+y)^2}{4xy} \leq 1$$

$$(x+y)^2 \leq 4xy \Rightarrow x^2 + y^2 + 2xy - 4xy \leq 0$$

$$(x-y)^2 \leq 0$$

We know that square of any number can not be negative possible.

$$\text{So, } (x-y)^2 = 0$$

$$x = y$$

39. (D) In the race between Sonu and Monu. Distance travelled by Sonu and Monu in same time = 600 metres and (600 - 60) metres = 600 metres and 540 metres \Rightarrow In the same time,

Ratio of distance travelled by Sonu and Monu = 10 : 9

Similarly,

In the same time

Ratio of distance travelled by Monu and Bablu = 500 : (500 - 25)

$$= 500 : 475$$

$$= 20 : 19$$

So, In the same time,

Ratio of distance travelled by Sonu, Monu and Bablu.

$$= 10 \times 20 : 9 \times 20 : 9 \times 19$$

$$= 200 : 180 : 171$$

\Rightarrow When Sonu travels 200m, Bablu will travel 171 m.

\Rightarrow In 400 m race between Sonu and Bablu required number of metres by which Sonu will win the race,

$$= 400\text{m} - 342\text{m} = 58\text{m}$$

40. (A) Let x = length of the faster train in (in metres),

$$\text{So, } 36 \text{ seconds} = \frac{x}{(40-20)\text{kmph}}$$

$$\Rightarrow x = 36 \text{ second} \times 20 \times \frac{5}{18} \text{ m/sec}$$

$$= 200 \text{ metres}$$

41. (A) Speed of boat in still water = $\frac{S_{\text{down}} + S_{\text{up}}}{2}$

$$= \frac{x+y}{2} = 0.5(x+y)$$

42. (C) Expression,
 $= 4 + 44 + 444 + \dots$ to n terms
 $= 4(1 + 11 + 111 + \dots)$ to n terms
 $= \frac{4}{9}(9 + 99 + 999 + \dots)$ to n terms
 $= \frac{4}{9}[(10 - 1) + (100 - 1) + (1000 - 1) + \dots]$
to n terms]
 $= \frac{4}{9}[(10 + 10^2 + 10^3 + \dots)$ to n terms] $- n]$
 $= \frac{4}{9}[10(1 + 10 + 10^2 + \dots)$ to n terms] $- n]$
 $= \frac{40}{9} \left(\frac{10^n - 1}{9} \right) - \frac{4}{9}n$

$[\therefore 1 + 10 + 10^2 + \dots$ to n terms $= \frac{10^n - 1}{9}]$
 $= \frac{40}{81}(10^n - 1) - \frac{4}{9}n$

43. (A) $a^4 + b^4 = a^4 + b^4 + 2a^2b^2 - 2a^2b^2$
 $= (a^2 + b^2)^2 - (ab\sqrt{2})^2$
 $= (a^2 + b^2 + ab\sqrt{2})(a^2 + b^2 - ab\sqrt{2})$
 $\Rightarrow \frac{a^4 + b^4}{a^2 - ab\sqrt{2} + b^2}$
 $= \frac{(a^2 + b^2 + ab\sqrt{2})(a^2 + b^2 - ab\sqrt{2})}{a^2 - ab\sqrt{2} + b^2}$
 $= a^2 + b^2 - ab\sqrt{2} = x - y$
 $\Rightarrow x = a^2 + b^2$
 $x^2 = a^4 + b^4 + 2a^2b^2$
 $y^2 = 2a^2b^2$
 $\Rightarrow x^2 - y^2 = a^4 + b^4$
 $\frac{a^4 + b^4}{a^2 - ab\sqrt{2} + b^2} = \frac{x^2 - y^2}{x - y} = x + y$

44. (D) $(x - a)(x - b) = 1 \Rightarrow (x - b) = \frac{1}{(x - a)}$
 $(x - a - 5) = \frac{1}{(x - a)}$ ($\because a + 5 = b$)
 $(x - a) - \frac{1}{(x - a)} = 5$
(Taking cube both sides)
 $(x - a)^3 - \frac{1}{(x - a)^3} - 3(5) = 125$
 $(x - a)^3 - \frac{1}{(x - a)^3} = 140$

45. (C) Let x be the required number and a be its first part

so, $(x - a)$ will be its second part,
Now, A.T.Q,
 $0.8a = 0.6(x - a) + 3$
or, $0.8a + 0.6a = 0.6x + 3$
or, $1.4a = 0.6x + 3$
 $\Rightarrow a = \frac{0.6x + 3}{1.4}$ (i)

Also,
 $0.9a + 6 = 0.8(x - a)$
or, $0.9a + 0.8a = 0.8x - 6$
or, $1.7 = 0.8x - 6$
 $\Rightarrow a = \frac{0.8x - 6}{1.7}$ (ii)

From equation (i) and (ii),
 $\frac{0.6x + 3}{1.4} = \frac{0.8x - 6}{1.7}$
 $\Rightarrow 1.02x + 5.1 = 1.12x - 8.4$
 $\Rightarrow 0.1x = 13.5$
 $\Rightarrow x = \frac{13.5}{0.1} = 135$

46. (B) Adding 1 in all terms,
 $\left(\frac{a^2 - bc}{a^2 + bc} + 1 \right) \left(\frac{b^2 - ac}{b^2 + ac} + 1 \right) + \left(\frac{c^2 - ab}{c^2 + ab} + 1 \right)$
 $= 1 + 1 + 1 + 1$
 $\left(\frac{2a^2}{a^2 + bc} \right) \left(\frac{2b^2}{b^2 + ac} \right) + \left(\frac{2c^2}{c^2 + ab} \right) = 4$
 $\frac{a^2}{a^2 + bc} + \frac{b^2}{b^2 + ac} + \frac{c^2}{c^2 + ab} = 2$

47. (A) A.T.Q
 $18.75\% = \frac{3}{16}$

	CP	+3	SP
I-article	16		19
II-article	22		19
		-3	

Loss percentage on second-II article
 $= \frac{3}{22} \times 100 = 13.63\%$

48. (B) A.T.Q,
Let $x = \sqrt{x^2 - x + 1}$
 $\Rightarrow x + \frac{1}{x} = 2 - x^2$
Minimum value of $x + \frac{1}{x} = 2$
 $\Rightarrow x + \frac{1}{x} \geq 2 = 2 - x^2 \geq 2$
 $\Rightarrow 0 \geq x^2, x^2 \leq 0$
It is possible, when $x = 0$
that why the value of x equal to 1 possible

49. (C) A.T.Q,
 $x^2 - 2(k-1)x + (2k+1) = 0$
 For equal roots $D = 0 \Rightarrow b^2 - 4ac = 0$
 $\therefore [-2(k-1)]^2 - 4(1)(2k+1) = 0$
 $4(k^2 + 1 - 2k) - 4(2k+1) = 0$
 $4k^2 + -8k - 8k - 4 = 0$
 $4k^2 - 16k = 0$
 $4k - 16 = 0$
 $4k = 16 \Rightarrow k = 4$

50. (A) C.P of each book sold by publisher

$$= ₹ \frac{70,000}{2000 - 400} = ₹ 43.75$$

S.P of each book sold by publisher
 $= (100 - 30)\% \text{ of } ₹ 75 = ₹ 52.5$

$$\text{So, \% gain} = \frac{52.5 - 43.75}{43.75} \times 100\%$$

(\therefore S.P > C.P)
 $= 20\% \text{ gain}$

51. (D) $x = a = 1, y = b = 2, z = c = 3$

$$= \frac{1-4}{3(-1)} + \frac{4-9}{5(-1)} + \frac{9-1}{4(2)}$$

$$= \frac{-3}{-3} + \frac{-5}{-5} + \frac{8}{8} = 1+1+1 = 3$$

52. (C) $15\sin^3\alpha + 20\cos^3\alpha = 12$

$$\Rightarrow \frac{15}{12}\sin^3\alpha + \frac{20}{12}\cos^3\alpha = 1$$

$$\left(\frac{5}{4}\sin\alpha\right)\sin^2\alpha + \left(\frac{5}{3}\cos\alpha\right)\cos^2\alpha = 1$$

$$\downarrow \qquad \downarrow$$

$$1 \qquad 1$$

To making in the form of $\sin^2\alpha + \cos^2\alpha = 1$

We put the value of

$$\frac{5}{4}\sin\alpha = 1 \text{ and } \frac{5}{3}\cos\alpha = 1$$

$$\text{Now, } \sin\alpha = \frac{4}{5} \text{ and } \cos\alpha = \frac{3}{5}$$

Hence,

$$\Rightarrow 10\sin\alpha + 15\cos\alpha = 10 \times \frac{4}{5} + 15 \times \frac{3}{5}$$

$$= 8 + 9 = 17$$

53. (B) Required ratio = $(15 \times 22) : (11 \times 25)$
 $= 330 : 275 = 6 : 5$

54. (D) Let ₹ x = quarterly payment

given, $r = 16\%$ per annum

So, rate of interest per quarter

$$= \frac{16}{4} = 4\% \text{ per quarter}$$

Also,

No. of quarters in 2 years = 4×2

$$= 8 \text{ quarter}$$

So, $8x + (7+6+4+3+2+1) \times 4\% \text{ of } x = 2280$

$$\text{or, } 8x + \left(\frac{7 \times 8}{2}\right) 4\% \text{ of } x = 2280$$

$$\left[\because 1+2+3+\dots+n = \frac{n(n+1)}{2}\right]$$

$$\text{or, } 8x + 112\% \text{ of } x = 2280$$

$$\text{or } 800\% \text{ of } x + 112\% \text{ of } x = 2280$$

$$\Rightarrow 912\% \text{ of } x = 2280$$

$$\text{So, } x = \frac{2280 \times 100}{912} = ₹ 250$$

55. (A) $\sin 6^\circ \sin 42^\circ \sin 66^\circ \sin 78^\circ = ?$

$$\frac{\sin 6^\circ \sin 54^\circ \sin 66^\circ \sin 42^\circ \sin 78^\circ}{\sin 54^\circ}$$

$$= \frac{\left(\frac{1}{4} \sin 18^\circ\right) \cdot \sin 42^\circ \cdot \sin 78^\circ}{\sin 54^\circ}$$

$$= \frac{1}{4} \times \frac{1}{4} \sin 54^\circ \cdot \frac{1}{\sin 54^\circ} = \frac{1}{16}$$

56. (A) $9\cos^2x - 6\sin x \cdot \cos x + \sin^2x + (\sin^2x + \cos^2x)$

$$\downarrow$$

$$1$$

$$= (3\cos x - \sin x)^2 + 1$$

$$\downarrow$$

$$0$$

[\because Minimum value of $10 + x^2 = 10$]

Then minimum value = 1

For maximum value

$$(3\cos x - \sin x)^2 + 1 = (\sqrt{3^2 + 1})^2 + 1 = 11$$

Hence, maximum value = 11

minimum value = 1

57. (A) Let time taken by B in completing the work = x days

\therefore Time taken by A $(x - 10)$ days

$$\therefore \frac{1}{x} + \frac{1}{x-10} = \frac{1}{12}$$

$$\Rightarrow \frac{x-10+x}{x(x-10)} = \frac{1}{12}$$

$$\Rightarrow 24x - 120 = x^2 - 10x$$

$$\Rightarrow x^2 - 34x + 120 = 0$$

$$\Rightarrow x^2 - 30x - 4x + 120 = 0$$

$$\Rightarrow x(x-30) - 4x(x-30) = 0$$

$$\Rightarrow (x-4)(x-30) = 0$$

$$\Rightarrow x-30 \text{ because } x \neq 4$$

58. (B) $5\alpha + 4\alpha = 90^\circ$

$$\alpha = 10^\circ$$

$$2\sin 30^\circ - \sqrt{3} \tan 30^\circ = 2 \times \frac{1}{2} - \sqrt{3} \times \frac{1}{\sqrt{3}} = 0$$

59. (B) Let speed of car = x km/hr
Here, Distance covered by the car in 27 minutes = Distance covered by the sound in (28 minutes 30 seconds - 27 minutes)

$$\Rightarrow x \text{ km/hr} \times \left(\frac{27}{60}\right) \text{ hr}$$

$$= \left(330 \times \frac{18}{5} \text{ km/hr}\right) \times \left(\frac{1.5}{60} \text{ hr}\right)$$

$$\Rightarrow x = 330 \times \frac{18}{5} \times \frac{1.5}{60} \times \frac{60}{27} = 66$$

$$\Rightarrow \text{speed of car} = 66 \text{ km/hr}$$

- 60 (B) $\sin x + \cos x = c$
Squaring both sides
 $\sin^2 x + \cos^2 x + 2\sin x \cdot \cos x = c^2$

$$\sin x \cdot \cos x = \frac{c^2 - 1}{2}$$

We know that,
 $\sin^6 x + \cos^6 x = 1 - 3\sin^2 x \cdot \cos^2 x$

$$= 1 - 3\left(\frac{c^2 - 1}{2}\right)^2$$

$$= 1 - 3\left(\frac{c^4 + 1 - 2c^2}{4}\right) = \frac{1 + 6c^2 - 3c^4}{4}$$

61. (C) $A(\lambda, 2 - 2\lambda)$, $B(-\lambda + 1, 2\lambda)$ and $C(-4 - \lambda, 6 - 2\lambda)$
Area of ΔABC ,

$$\Delta = \frac{1}{2}(x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2))$$

$$\{\lambda(2\lambda - 6 + 2\lambda) + (-\lambda + 1)(6 - 2\lambda - 2 + 2\lambda)\}$$

$$+ (-4 - \lambda)(2 - 2\lambda - 2\lambda)$$

$$140 = (4\lambda^2 - 6\lambda + 4 - 4\lambda - 8 + 16\lambda - 2\lambda + 4\lambda^2)$$

$$140 = 8\lambda^2 + 4\lambda - 4$$

$$2\lambda^2 + \lambda - 36 = 0$$

$$2\lambda^2 + 9\lambda - 8\lambda - 36 = 0$$

$$\lambda(2\lambda + 9) - 4(2\lambda + 9) = 0$$

$$(\lambda - 4)(2\lambda + 9) = 0$$

$$\lambda = 4, \frac{-9}{2}$$

The integer value of λ is 4

62. (A) Quality

$$B \leq A$$

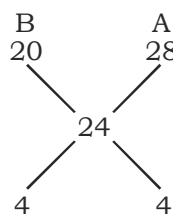
$$x \quad x + 8$$

$$11 \text{ units} \longrightarrow ₹ 264$$

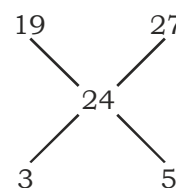
$$10 \text{ units} \longrightarrow ₹ 240$$

$$\text{CP of paint are} = ₹ 240$$

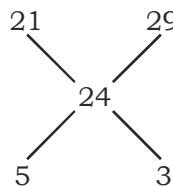
Case - I



Case-II



Case - III



In cases (II) and (III)

$B > A$

So, case - (I) is true

63. (D) Let 'a' and 'b' are those two numbers.

$$\Rightarrow a^2 + b^2 = 97$$

$$\Rightarrow a^2 + b^2 - 2ab = 97 - 2ab$$

$$\Rightarrow (a - b)^2 = 97 - 2ab$$

We know that $(a - b)^2 \geq 0$

$$\Rightarrow 97 - 2ab \geq 0$$

$$\Rightarrow ab \leq 48.5$$

Hence, $ab \neq 0$

64. (D) $S = 7 \times 11 + 11 \times 15 + 15 \times 19 + \dots + 95 \times 99$

Nth term of the series can be written as

$$T_n = (4n + 3) \times (4n + 7)$$

Last term, $(4n + 3) = 95$ i.e $n = 23$

$$\sum_{n=0}^{n=23} (4n + 3) \times (4n + 7)$$

$$\Rightarrow \sum_{n=0}^{n=23} 16n^2 + 40n + 21$$

$$23 \times 24 \times 47 \quad 23 \times 24$$

$$\Rightarrow 16 \times 23 \times 4 \times 47 + 40 \times 23 \times 12 + 21$$

$$\Rightarrow 80245$$

65. (D) It is given that $N^N = 2^{160}$

We can rewrite the equation as

$$N^N = (2^5)^{160/5} = 32^{32}$$

$$\Rightarrow N = 32$$

$$N^2 + 2^N = 32^2 + 2^{32} = 2^{10} \times (1 + 2^{22})$$

Hence, we can say that $N^2 + 2^N$ can be divided by 2^{10}

Therefore, $X_{max} = 10$

66. (C) Let 't' pm the time when the tank is the emptied everyday. Let 'a' and 'b' be the litres/hr filled by pump A and pump B respectively,

On Monday, A alone completed filling the tank at 8 pm. Therefore we can say that pump A worked for $(8 - t)$ hours. Hence, the volume of the tank = $a \times (8 - t)$ litres
Similarly, on Tuesday, B alone completed filling the tank at 6 pm.

Therefore we can say that pump B worked for $(6 - t)$ hours. Hence the volume of the tank = $b \times (6 - t)$ litres

On Wednesday, A alone worked till 5pm, and then B worked alone from 5 pm to 7 pm to fill the tank. Therefore we can say that pump A worked for $(5 - t)$ hours and pump B worked for 2 hours. Hence the volume of the tank = $a \times (5 - t) + 2b$ litres

We can say that $a(8 - t) = b \times (6 - t) = a \times (5 - t) + 2b$

$$a \times (8 - t) = a \times (5 - t) + 2b$$

$$\Rightarrow 3a = 2b \quad \dots(i)$$

$$a \times (8 - t) = b \times (6 - t)$$

Using equation (i), we can say that

$$a \times (8 - t) = \frac{3a}{2} \times (6 - t)$$

$$t = 2$$

Therefore, we can say that the tank gets emptied at 2 pm daily. We can see that A takes 6 hours and pump B takes 4 hours alone.

Hence, working together both can fill the tank in = $\{6 \times 4\} / \{6 + 4\} = 2.4$ hours or 2 hours and 24 minutes.

The pumps started filling the tank at 2:00pm. Hence the tank will be filled by 4 : 24 pm

67. (B) Let 'a', 'b' and 'c' be the contraction of salt in solutions A, B and C respectively.

It is given that three salt solutions A, B, C are mixed in the proportion 1 : 2 : 3, then the resulting solution has strength 20%

$$a + 2b + 3c$$

$$\Rightarrow 1 + 2 + 3 = 20$$

$$\Rightarrow a + 2b + 3c = 120 \quad \dots(i)$$

If instead the proportion is 3 : 2 : 1, then the resulting solution has strength 30%

$$3a + 2b + c$$

$$\Rightarrow 1 + 2 + 3 = 30$$

$$\Rightarrow 3a + 2b + c = 180 \quad \dots(ii)$$

From equation (i) and (ii), we can say that

$$\Rightarrow b + 2c = 45$$

$$\Rightarrow b = 45 - 2c$$

Also, on subtracting (i) and (ii) we get

$$a - c = 30$$

$$\Rightarrow a = 30 + c$$

In solution D, B and C are mixed in the ratio 2 : 7

So, the concentration of salt in

$$D = \frac{2b + 7c}{9} = \frac{90 - 4c + 7c}{9} = \frac{90 + 3c}{9}$$

$$\text{Required ratio} = 9a = 9(30+c) = 1 : 3$$

68. (A) A.T.Q,

Let the CP of table = T

CP of chair = C

$$T \times \frac{25}{3}\% = C \times \frac{25}{2}$$

$$\Rightarrow \frac{T}{C} = \frac{3}{2} \quad \dots(i)$$

$$T \times \frac{25}{2}\% - C \times \frac{25}{3}\% = 25$$

$$3T - 2C = ₹ 600 \quad \dots(ii)$$

Putting the value of T in equation (ii),

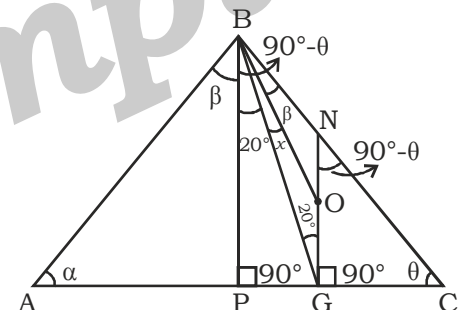
$$3 \times \frac{3}{2}C - 2C = ₹ 600$$

$$\Rightarrow \frac{9}{2}C - 2C = ₹ 600$$

$$\Rightarrow \frac{5C}{2} = ₹ 600$$

$$C = ₹ 240$$

69. (A) A.T.Q,



$$\angle \alpha - \angle \theta = 33^\circ$$

Draw an altitude from B on side AC, OG parallel to BP.

In ΔBGO and ΔPBG ,

$$\angle G = \angle B = 20^\circ$$

Line OG extended to side AC

$$\angle GNC = 90^\circ - \theta$$

In ΔPBC and ΔGNC

$$\angle N = \angle B = 90^\circ - \theta$$

Now, In ΔPBC ,

$$20^\circ + x^\circ + \beta = 90^\circ - \theta \quad \dots(i)$$

In ΔABP ,

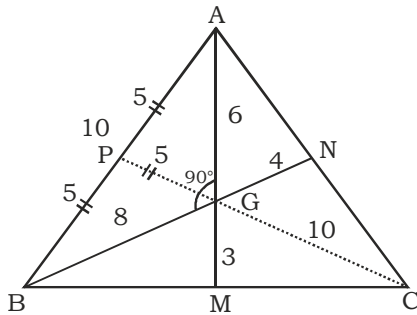
$$\alpha + \beta = 90^\circ \quad \dots(ii)$$

From equation (i) and (ii),

$$20^\circ + x^\circ + 90 - \alpha = 90^\circ - \theta$$

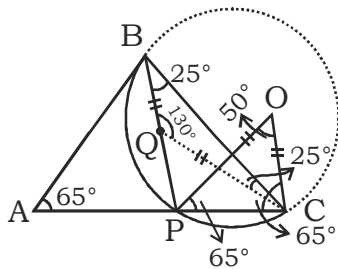
$$\Rightarrow x^\circ = \alpha - \theta - 20^\circ = 33^\circ - 20^\circ = 13^\circ$$

70. (B) A.T.Q,



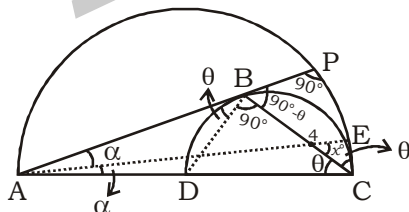
Draw a line from G on side AB
 \therefore GP is angle bisector of $\angle G$
 \therefore AP = BP = GP = 5 cm
 \therefore G is centroid and CP is median ,
 1 unit = 5 cm
 2 units = 10 cm

71. (B) A.T.Q,



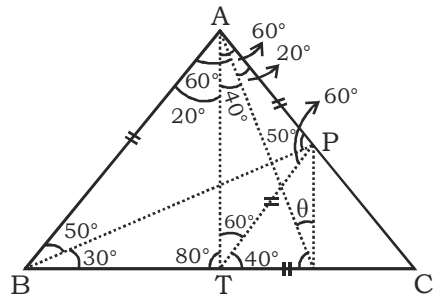
Draw a line from Q to C
 In $\triangle ABC$,
 $\therefore \angle C = 65^\circ$
 $\therefore \angle Q = 2\angle A = 130^\circ$
 Draw a circle from O
 $\angle PBC = 25^\circ, \angle POC = 50^\circ$
 $OC = OP = \text{radius}$
 So, In $\triangle OPC$,
 $\angle P = \angle C = 65^\circ$

72. (A) A.T.Q,

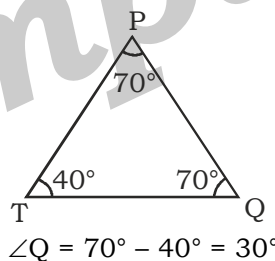


\therefore AE is angle bisector of $\angle A$
 So in $\triangle PAE$ and $\triangle EAC$.
 Draw lines from B to D and P to C
 $\triangle ABD = \theta$
 Now, in $\triangle BPC = 90^\circ - \theta$
 In $\triangle APC$
 $2\alpha + 2\theta + 90^\circ = 180^\circ$
 $\alpha + \theta = 45^\circ$
 $x = 45^\circ$
 $\therefore x$ is the sum of interior angle,

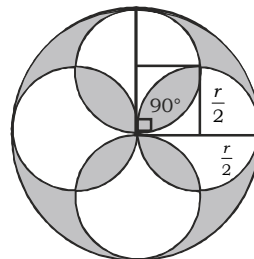
73. (C) A.T.Q,



In $\triangle APB \angle P = 50^\circ$
 and $\angle B = 50^\circ$
 So, sides
 $AB = AP$
 Now, In $\triangle AQB$,
 $\angle Q = 40^\circ$
 Draw a line AT
 $\angle T = 80^\circ$
 In $\triangle ABT$,
 $\angle A = 20^\circ$
 $AB = AP = AT = TQ$
 In $\triangle ATC$
 $\angle A = 20^\circ$ and in $\triangle AQT$
 $\angle A = 40^\circ$
 Now In $\triangle PTQ$
 $PT = TQ$



74. (C) A.T.Q,



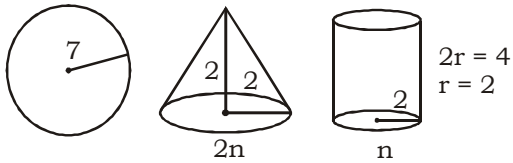
$$= \frac{\pi}{4} r^2 - \frac{\pi}{4} r^2 + \frac{4}{7} \times \frac{r^2}{4} = \frac{4}{7} \times \frac{r^2}{4}$$

$$\text{Area of lif} = \frac{4}{7} \times \text{side}^2$$

$$= \frac{4}{7} \times \frac{225}{4} \times 8$$

$$= \frac{8}{7} \times 225$$

75. (C) A.T.Q,



$$\frac{4}{3}\pi r^3 = \frac{1}{3}\pi r^2 h + \pi r^2 h$$

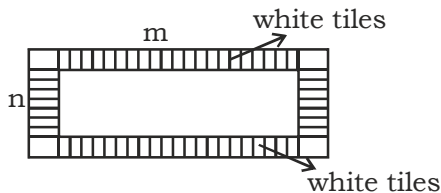
$$\frac{4}{3}\pi \times 343 = \frac{1}{3}\pi \times 2 \times 2 \times 2 \times 2n + \pi \times 2 \times 2 \times 4 \times n$$

$$\Rightarrow 16n = 343$$

$$n = 21.43$$

Hence maximum numbers of cones = 42

76. (B) A.T.Q,



$$m + m + (n - 2) \times 2$$

$$= 2m + 2(n - 2)$$

$$\text{white tiles} = 2[m + n - 2]$$

$$\text{Total tiles} = m \times n$$

$$\text{Red tiles} = m \times n - 2[m + n - 2]$$

$$\Rightarrow 2(m + n - 2) = m \times n - 2[m + n - 2]$$

$$\Rightarrow 4(m + n - 2) = m \times n$$

$$\Rightarrow m \times n - 4m - 4n + 8 = 0$$

$$m(n - 4) - 4(n - 4) = 8$$

$$(n - 4)(m - 4) = 8$$

Possible cases

$$m > n$$

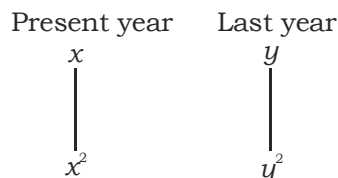
$$4 \times 2, \quad 8 \times 1$$

Case - I Case-II

$$m - 4 = 4 \quad m - 4 = 8$$

$$m = 8 \quad m = 12$$

77. (B) A.T.Q,



$$x^2 - y^2 = 131$$

$$(x + y)(x - y) = 131$$

$$x + y = 131$$

$$x - y = 1$$

$$x = 66$$

Total Potatoes produce farmer
 this year = 4356

78. (A) A.T.Q,

$$\text{Let CP of a cycles} = 100x$$

$$\text{MRP} = 120x$$

Case - I

Cash value 1% \longrightarrow Discount

$$\text{SP} = 108x$$

$$\text{Profit} = 8\%$$

Case - II

Credit sales,

5% \longrightarrow Discount

$$\text{SP} = 144x$$

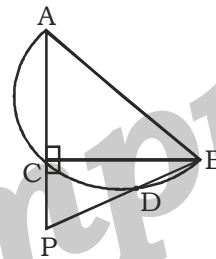
$$\text{Profit} = 14\%$$

$$\frac{45 \times 100x \times 8}{100} + \frac{15 \times 100x \times 14}{100} = ₹ 11400$$

$$\Rightarrow x = ₹ 20$$

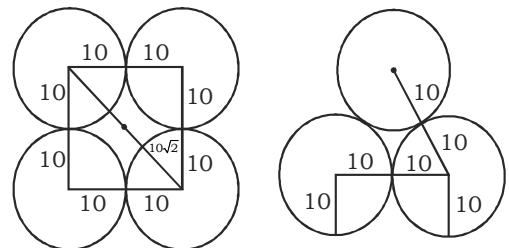
Hence, cost price of a cycles is ₹ 2000

79. (A) A.T.Q,



$$\begin{aligned} AB^2 &= AC^2 + BC^2 \\ &= AC \times AC + BP^2 - PC^2 \\ &= AC \times (AP - PC) + BP^2 - PC^2 \\ &= AC \times AP - AC \times PC + BP^2 - PC^2 \\ &= AC \times AP - PC(AC + PC) + BP^2 \\ &= AC \times AP - PC \times AP + BP^2 \\ &= AC \times AP - PD \times PB + PB^2 \quad (PC \times PA = PD \times PB) \\ &= AC \times AP + PB(PB - PD) \\ &= AC \times AP + PB \times BD \end{aligned}$$

80. (B) A.T.Q,

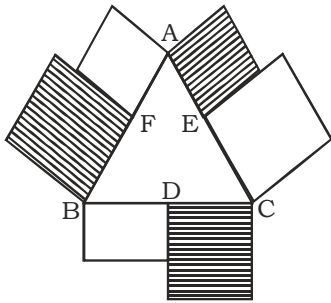


$$= \sqrt{400 - 200} = \sqrt{200} = 10\sqrt{2}$$

\therefore Two sphere are already lies below

$$= 10\sqrt{2} + 10$$

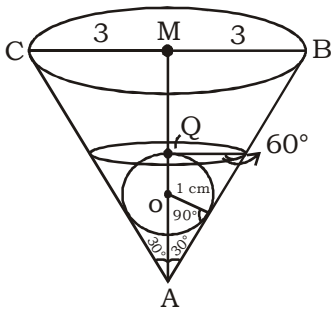
81. (D) A.T.Q,



$$AF^2 + BD^2 + CE^2 = DF^2 + DC^2 + AE^2$$

$$DF^2 + DC^2 + AE^2 = 4 + 25 + 49 = 78 \text{ cm}^2$$

82. (A) A.T.Q,



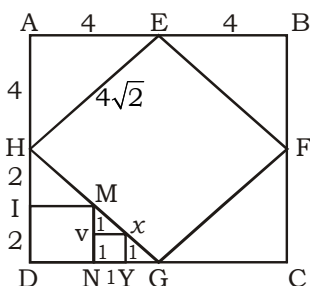
$\therefore BC = 6 \text{ cm}$
 $AB = 6 \text{ cm}$
 $AC = 6 \text{ cm}$
 So it is an equilateral triangle,
 Draw an altitude AM,
 $AO = 2 \text{ cm}, AQ = 3 \text{ cm}$

$$= \frac{1}{3} \pi r^2 h - \frac{4}{3} \pi r^3$$

$$= \frac{1}{3} \times \pi \times 3 \times 3 - \frac{4}{3} \pi \times 1$$

$$= \frac{5\pi}{3} \text{ cm}^3$$

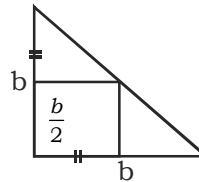
83. (A) A.T.Q,



ABCD : NMID

EFGH : VXYN

$$\text{side} = \frac{b \times h}{b + h}$$

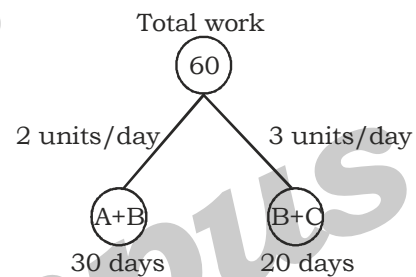


$$\text{side} = \frac{b \times b}{2b} = \frac{b}{2}$$

ABCD : NMID = 64 : 4 = 16 : 1

EFGH : VXYN = $(4\sqrt{2})^2 : 1 = 32 : 1$

84. (D)



According to the question.

$\Rightarrow A + B \dots\dots\dots 30 \text{ days}$
 $\Rightarrow B + C \dots\dots\dots 20 \text{ days}$
 $\Rightarrow A \dots\dots\dots 5$
 $\Rightarrow B \dots\dots\dots 5 + 10$
 $\Rightarrow C \dots\dots\dots 10 + 8 \text{ days}$
 $\Rightarrow \text{work done by } (A + B) \text{ in } 5 \text{ days} = 2 \times 5 = 10 \text{ work}$
 $\Rightarrow \text{Work done by } (B + C) \text{ in } 5 \text{ days} = 10 \times 3 = 30 \text{ work}$
 $\Rightarrow \text{Total work} \dots\dots\dots 40 \text{ work}$
 $\Rightarrow \text{Remaining work} = 60 - 40 = 20 \text{ work}$
 $\Rightarrow \text{Here we find that C does remaining } 20 \text{ work in } 8 \text{ days}$

$$\Rightarrow \text{C's efficiency} = \frac{\text{work}}{\text{Day}}$$

$$= \frac{20 \text{ work}}{8 \text{ Day}} = \frac{5}{2}$$

$$\Rightarrow \text{C's efficiency} = \frac{5}{2} \text{ work per day}$$

$\Rightarrow \text{Therefore time taken by C alone to complete the work} = \frac{60}{5} \times 2 = 24 \text{ days}$

85. (D) $X^{2018} Y^{2017} = \frac{1}{2}$

$x^{2016} y^{2019} = 8$

$\frac{x^2}{y^2} = \frac{1}{16} \Rightarrow \frac{x}{y} = \frac{1}{4}$

$x = \frac{1}{2}$ and $y = 2$

$x^2 + y^3 = \left(\frac{1}{2}\right)^2 + 2^3 = \frac{33}{4}$

86. (A) A.T.Q,

Let total work is = 16 (R + G)

Total work done by Ramesh and Ganesh before sick = 7 (R + G)

After sick 30% efficiency fell by

$\Rightarrow 16 (R + G) = 7 (R + G) + 10 (7R + G)$

$\Rightarrow R = 0.5 G$ (i)

Total amount of work left when Ramesh got, sick = 16 (R + G) - 7(R + G) = 9(R + G)

= 9 (0.5G + G) = 13.5 G

Time taken by Ganesh to finish the

remaining work = $\frac{13.5G}{G} = 13.5$ days

87. (A) A.T.Q,

Before Appeal

Amal = 11k

Bimal = 14 k

After appeal = 11k + x

= 14k + x

11k + x = 47(i)

14k + x = 56(ii)

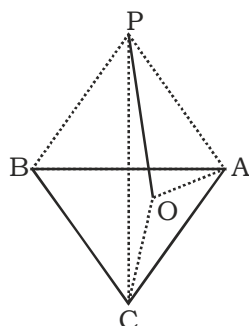
From equation (i) and (ii),

k = 3

x = 14

Bimal's ratio = $\frac{14 \times 3 + 14}{14 \times 3} = \frac{4}{3}$

88. (B) Let O be the centre of the equilateral ΔABC and OP the tower of height H. Then each of the ΔPAB , ΔPBC and ΔPCA equilateral. Thus PA = PB = PC = a. Therefore from right-angle triangle POA, we have,



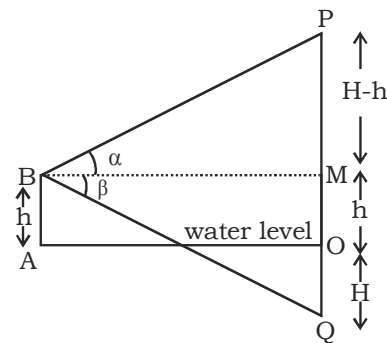
$PA^2 = PO^2 + OA^2$

$\Rightarrow a^2 = h^2 + \left(\frac{a}{2} \sec 30^\circ\right)^2$

= $h^2 + \frac{a^2}{4} \cdot \frac{4}{3} = h^2 + \frac{a^2}{3}$

$\Rightarrow \frac{2}{3} a^2 = h^2 \Rightarrow 2a^2 = 3h^2$

89. (D) Let P be the cloud at height H above the level of the water. In the lake Q is its image.



$\therefore OQ = OP = H$

B is a point at a height AB = h, above the water, Angle of elevation of P and depression of Q from B are α and β respectively

In ΔPBM ,

$\tan \alpha = \frac{H-h}{BM}$

$\therefore MB = (H-h) \cot \alpha$ (i)

In ΔQMB ,

$\tan \beta = \frac{QM}{BM}$

$\therefore BM = (H+h) \cot \beta$ (ii)

From equation (i) and (ii),

$(H-h) \cot \alpha = (H+h) \cot \beta$

$\Rightarrow H(\cot \alpha - \cot \beta) = h(\cot \alpha + \cot \beta)$

$\therefore H = \frac{h(\cot \alpha + \cot \beta)}{\cot \alpha - \cot \beta}$

90. (B) A.T.Q,

Let Tea A \longrightarrow a kg

Tea B \longrightarrow b kg

Case - I

$\frac{3a+2b}{5} = 40 \times \frac{10}{11}$

$3a+2b = \frac{2000}{11}$ (i)

Case - II

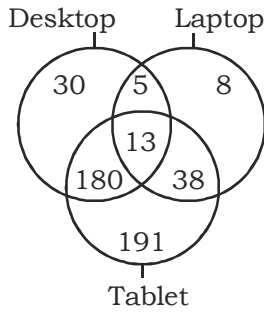
$\frac{2a+2b}{5} = 40 \times \frac{20}{21}$

$2a+2b = \frac{4000}{21}$ (ii)

$$b = \frac{3200}{77}, a = \frac{7600}{77 \times 3}$$

$$\frac{a}{b} = \frac{7600}{3200 \times 3} = \frac{19}{24}$$

91. (D) Use figure from 91 to 95



92. (A)
 93. (C)
 94. (B)
 95. (B)

96. (C) Average sales of grade

$$1 = \frac{(20 + 40 + 50 + 60)}{4} = 42.5 \text{ tonnes}$$

Average sales of grade

$$2 = \frac{(40 + 60 + 20 + 110)}{4} = 57.5 \text{ tonnes}$$

$$\text{Difference} = 57.5 - 42.5 = 15 \text{ tonnes}$$

97. (A) Total income of companies
 $A = (75000 \times 20) + (60000 \times 40)$
 $= ₹ 3900000$

Total income of companies
 $C = (75000 \times 50) + (60000 \times 20)$
 $= ₹ 4950000$

Difference = ₹ 1050000 = ₹ 1.05 million.

98. (D) 3 companies = A, B and D. See the table below.

	Grade 1 company (tonnes)	Grade 2 (tonnes)
A	20	40
B	40	60
C	50	20
D	60	110

99. (D) Net time of company

$$A = (75000 \times 20) + (40 \times 6000)$$

$$= ₹ 3900000$$

Grade 1 constitutes 38.46%

$$\frac{150000}{3900000} \times 100 = 38.46\%$$

100. (D) Total production by company

$$D = 60 + 110 = 170 \text{ tonnes}$$

Total production by company

$$B = 40 + 60 = 100 \text{ tonnes}$$

Total production by company D is 170 % that of company.

SSC TIER II (MATHS) MOCK TEST - 51 (ANSWER KEY)

1. (D)	11. (C)	21. (C)	31. (C)	41. (A)	51. (D)	61. (C)	71. (B)	81. (D)	91. (D)
2. (C)	12. (B)	22. (D)	32. (A)	42. (C)	52. (C)	62. (A)	72. (A)	82. (A)	92. (A)
3. (A)	13. (B)	23. (C)	33. (D)	43. (A)	53. (B)	63. (D)	73. (C)	83. (A)	93. (C)
4. (A)	14. (C)	24. (A)	34. (A)	44. (D)	54. (D)	64. (B)	74. (C)	84. (D)	94. (B)
5. (D)	15. (B)	25. (B)	35. (C)	45. (C)	55. (A)	65. (D)	75. (B)	85. (D)	95. (B)
6. (A)	16. (A)	26. (D)	36. (B)	46. (B)	56. (A)	66. (C)	76. (B)	86. (A)	96. (C)
7. (C)	17. (D)	27. (C)	37. (C)	47. (A)	57. (A)	67. (B)	77. (B)	87. (A)	97. (A)
8. (A)	18. (A)	28. (A)	38. (A)	48. (B)	58. (B)	68. (A)	78. (A)	88. (B)	98. (D)
9. (A)	19. (A)	29. (D)	39. (D)	49. (C)	59. (B)	69. (A)	79. (A)	89. (D)	99. (D)
10. (A)	20. (C)	30. (D)	40. (A)	50. (A)	60. (B)	70. (B)	80. (B)	90. (B)	100. (D)

Note:- If your opinion differs regarding any answer, please message the mock test and question number to 8860330003

Note:- Whatsapp with Mock Test No. and Question No. at 7053606571 for any of the doubts. Join the group and you may also share your suggestions and experience of Sunday Mock

Note:- If you face any problem regarding result or marks scored, please contact 9313111777