## 52 SSC Mains (Maths) Answer with Explanation

1. (D) $(a-1) \sqrt{2}+3=b \sqrt{2}+a$

$$
\begin{aligned}
& \Rightarrow a=3, a-1=b \\
& \Rightarrow 3-1: b \Rightarrow b=2 \\
& \therefore a+b=3+2=5
\end{aligned}
$$

2. (B) $\mathrm{OP}=2$
$O Q=\frac{3}{2}$


$$
\begin{aligned}
\therefore \mathrm{PQ} & =\sqrt{\mathrm{OP}^{2}+\mathrm{OQ}^{2}} \\
& =\sqrt{2^{2}+\left(\frac{3}{2}\right)^{2}} \\
& =\sqrt{4+\frac{4}{9}} \\
& =\sqrt{\frac{16+9}{4}}=\sqrt{\frac{25}{4}}=\frac{5}{2}=2.5 \mathrm{~cm}
\end{aligned}
$$

3. (A) A.T.Q,


Putting $x=0$ in $9 x-12 y=108$, we get, $y=-9$
Putting $\mathrm{y}=0$ in $9 x-12 y=108$,
we get, $x=12$
$\therefore \mathrm{OA}=12, \mathrm{OB}=9$
$\mathrm{AB}=\sqrt{\mathrm{OA}^{2}+\mathrm{OB}^{2}}$

$$
\begin{aligned}
& =\sqrt{12^{2}+9^{2}} \\
& =\sqrt{144+81}=\sqrt{225}=15 \text { units }
\end{aligned}
$$

4. (A) $\left(x+\frac{1}{x}\right)^{2}$
$\Rightarrow x+\frac{1}{x}=\sqrt{3}$
On cubing both sides,
$x^{3}+\frac{1}{x^{3}}+3\left(x+\frac{1}{x}\right)=3 \sqrt{3}$
$\Rightarrow x^{3}+\frac{1}{x^{3}}=3 \sqrt{3}-3 \sqrt{3}=0$
$\Rightarrow x^{6}+1=0$
$\therefore x^{206}+x^{200}+x^{90}+x^{84}+x^{18}+x^{12}+x^{6}+1$
$=x^{200}\left(x^{6}+1\right)+x^{84}\left(x^{6}+1\right)+x^{12}\left(x^{6}+1\right)+\left(x^{6}+1\right)=0$
5. (A) $\frac{\sqrt{7}}{\sqrt{16+6 \sqrt{7}}-\sqrt{16-6 \sqrt{7}}}$

$$
=\frac{\sqrt{7}}{\sqrt{9+7+2 \times 3 \times \sqrt{7}}-\sqrt{9+7-2 \times 3 \times \sqrt{7}}}
$$

$$
\sqrt{7}
$$

$$
\sqrt{(3)^{2}+(\sqrt{7})^{2}+2 \times 3 \times \sqrt{7}}-\sqrt{(3)^{2}+(\sqrt{7})^{2}-2 \times 3 \times \sqrt{7}}
$$

$$
=\frac{\sqrt{7}}{\sqrt{(3+\sqrt{7})^{2}}-\sqrt{(3-\sqrt{7})^{2}}}
$$

$$
=\frac{\sqrt{7}}{(3+\sqrt{7})-(3-\sqrt{7})}=\frac{\sqrt{7}}{2 \sqrt{7}}=\frac{1}{2}
$$

6. (B) $a \otimes b=a+b$ when, $a$ and $b$ both positive $a \otimes b=\sqrt{a^{2}+b^{2}}$ for any another value Then expression,
$\frac{10-4}{\sqrt{9+16}}=\frac{6}{5}$
7. (A) A.T.Q,

Internal side $=8 \mathrm{~cm}$

$\therefore \triangle \mathrm{OMN}$ is an equilateral triangle
$\mathrm{AO}=\frac{\sqrt{3}}{2} \times 8=4 \sqrt{3}$
$\mathrm{OA}=4 \sqrt{3}$
$O B=6 \sqrt{3}$
OB become height of the larger hexagon
$\frac{\sqrt{3}}{2} a=6 \sqrt{3}$
$\mathrm{a}=12$
side $=12 \mathrm{~cm}$
Area of shaded region
$=\frac{\sqrt{3}}{4}(12)^{2} \times 6-\frac{\sqrt{3}}{4} \times(8)^{2} \times 6$
$=\frac{\sqrt{3}}{4} \times 6[144-64]=120 \sqrt{3}$
8. (B) A.T.Q,


Intial age of Bigger son $=14$ years
Smaller son $=12$ years
$=\mathrm{B}\left(1+\frac{1}{20}\right)^{4}=\mathrm{S}\left(1+\frac{1}{20}\right)^{6}$
$\frac{B}{S}=\frac{441}{400}$
841 units $\rightarrow ₹ 120000$
400 units $\rightarrow ₹ 57074.9$
9. (C) ATQ,


He has to pay ₹ 7202 at the end of third year to clear the loan
10. (A) A.T.Q,


Here, $h=$ height of tower $A B$
$\tan \theta=\frac{h}{a}$
$\tan \left(90^{\circ}-\theta\right)=\frac{h}{b}$
or, $\cot \theta=\frac{h}{b}$
$\Rightarrow \tan \theta=\frac{b}{h}$
From equation (i) and (ii)
$\frac{h}{a}=\frac{b}{h} \Rightarrow h=\sqrt{a b}$
11. (A) Here,
$3^{50}=\left(3^{5}\right)^{10}=243^{10}$,
$4^{40}=\left(4^{4}\right)^{10}=256^{10}$,
$5^{30}=\left(5^{3}\right)^{10}=125^{10}$,
and,
$6^{20}=\left(6^{4}\right)^{10}=36^{10}$,
$\therefore$ Greatest number $=256^{10}=4^{40}$
12. (C) A.T.Q,
$1 \mathrm{M}=2 \mathrm{C}$
and,
$(4 \mathrm{M}+5 \mathrm{~W}+6 \mathrm{C}) \times 15=(2 \mathrm{M}+3 \mathrm{~W}+2 \mathrm{C}) \times 31$
$\Rightarrow(7 \mathrm{M}+5 \mathrm{~W}) \times 15=(3 \mathrm{M}+3 \mathrm{~W}) \times 31$
On solving, we get
$4 \mathrm{M}=6 \mathrm{~W}$
Then, the ratio of capacity of man, woman and child $=6: 4: 3$
Let 1 man, 1 woman and 1 child can complete the work in $x$ days.
Then,
$(6 \times 4+4 \times 5+6 \times 3) \times 15$
$=(6+4+3) \times x$
$\Rightarrow 62 \times 15=13 x$
$\Rightarrow x=\frac{930}{13}=71 \frac{7}{13}$ days
$\therefore$ Required number of days $=71 \frac{7}{13}$ days
13. (B) Let the investments of the personbe $P$ $\mathrm{P}_{2}$ and $\mathrm{P}_{3}$
A.T.Q,
$P_{1}\left[\frac{r_{1} t_{1}}{100}+1\right]=P_{2}\left[\frac{r_{2} t_{2}}{100}+1\right]=P_{3}\left[\frac{r_{3} t_{3}}{100}+1\right]$
$\Rightarrow P_{1}\left[\frac{6 \times 5}{100}+1\right]=P_{2}\left[\frac{8 \times 5}{100}+1\right]=P_{3}\left[\frac{10 \times 6}{100}+1\right]$
$\Rightarrow 13 \mathrm{P}_{1}=14 \mathrm{P}_{2}=16 \mathrm{P}_{3}$
Then,
$P_{1}: P_{2}: P_{3}=14 \times 16: 13 \times 16: 13 \times 14$
= 112: 104: 91
$\therefore$ Required ratio $=112: 104: 91$
14. (B) Let the total profit be $2 x$.

Now the amount which B gets
as allowance $=12 \times 150=₹ 1800$
Now,
The profit shared between A and B
$=\frac{2 x-1800}{2}=x-900$
Now, the amount which B pays to A
$=50,000 \times \frac{10}{100}=₹ 5000$
A.T.Q,
$\frac{x-900+5000}{x-900-5000+1800}=\frac{3}{2}$
$\Rightarrow \frac{x+4100}{x-4100}=\frac{3}{2}$
$\Rightarrow 2 x+2 \times 4100=3 x-3 \times 4100$
$\Rightarrow x=5 \times 4100$
$\Rightarrow x=20500$
Then,
Total profit
$=2 x=2 \times 20500=₹ 41000$
15. (A) Angles of triangle,
$\Rightarrow(a-d)^{\circ}, a^{\circ},(a+d)^{\circ}$
$\therefore a-d+a+a+d=180^{\circ}$
$\Rightarrow 3 a=180^{\circ} \Rightarrow \quad a=60$
$\therefore \frac{a-d}{a+d}=\frac{60}{\pi}=\frac{60}{180}=\frac{1}{3}$
$\Rightarrow \frac{60-d}{60+d}=\frac{1}{3}$
$\Rightarrow 180-3 d=60+d$
$\Rightarrow 4 d=120^{\circ} \Rightarrow \quad d=30^{\circ}$
$a-d=60^{\circ}-30^{\circ}=30^{\circ}$
$a=60^{\circ}$
$a+d=60^{\circ}+30^{\circ}=90^{\circ}$
So, Angles of triangle are $30^{\circ}, 60^{\circ}$ and $90^{\circ}$
16. (A) In the given figure after leaving the point A, balloon reaches point B vertically upward in 1.5 min


Here, $\mathrm{O} \rightarrow$ the observer
So, $\angle \mathrm{BOA}=60^{\circ}$ (observer)
$\Rightarrow \tan 60^{\circ}=\frac{\mathrm{AB}}{\mathrm{OA}}$
$\Rightarrow \mathrm{AB}=\mathrm{OA} \tan 60^{\circ}$

$$
=200 \times \sqrt{3}
$$

So, speed of the balloon

$$
\begin{aligned}
& =\frac{\text { Distance }}{\text { Time }} \\
& =\frac{\mathrm{AB}}{\text { time to reach from A to B }} \\
& =\frac{200 \sqrt{3} \mathrm{~m}}{1.5 \times 60}=3.87 \mathrm{~m} / \mathrm{sec}
\end{aligned}
$$

17. (C) A.T.Q,


Here,
$\mathrm{AB} \rightarrow$ height of the house
and CD $\rightarrow$ height of the window
So, $\angle \mathrm{ADB}=90^{\circ}$
Also,
here line AD makes an angle $\theta^{\circ}$ with the vertical line DE.
$\Rightarrow \angle \mathrm{ADE}=\theta^{\circ}$ also,
$\Rightarrow \angle \mathrm{BDC}=90^{\circ}-\theta^{\circ}$
In $\triangle B C D$,
$\tan \left(90^{\circ}-\theta\right)=\frac{B C}{C D}=\frac{d}{C D}$ or, $\cot \theta=\frac{d}{C D}$
$\Rightarrow \mathrm{CD}=\frac{\mathrm{d}}{\cot \theta}=d \tan \theta$
Also,
In $\triangle \mathrm{ADE}$,
$\tan \theta=\frac{\mathrm{AE}}{\mathrm{DE}}=\frac{\mathrm{d}}{\mathrm{DE}} \Rightarrow \mathrm{DE}=\frac{\mathrm{d}}{\tan \theta}=d \cot \theta$
So, the height of the house,
$\mathrm{AB}=\mathrm{CD}+\mathrm{DE}$
$=d(\tan \theta+\cot \theta)$
$=d\left(\frac{\sin \theta}{\cos \theta}+\frac{\cos \theta}{\sin \theta}\right)=d\left(\frac{1}{\cos \theta \times \sin \theta}\right)$
$=d \sec \theta \operatorname{cosec} \theta$
18. (A) A.T.Q,


Let $A B C$ is a $\Delta$ and $a, b$ and $c$ are the lengths of $B C, C A$ and $A B$ respectively.
$\because \sin A: \sin B: \sin C=1: 1: \sqrt{2}$

## By sine formula:

$\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
$\Rightarrow a: b=\sin A: \sin B$ and $b: c=\sin B: \sin C$
$\Rightarrow a: b: c=1: 1: \sqrt{2}$
Let $a=x, b=x$ and $c=\sqrt{2} x$

$$
\begin{aligned}
c^{2}:\left(a^{2}+b^{2}\right) & =(\sqrt{2} x)^{2}:\left(x^{2}+x^{2}\right) \\
& =2 x^{2}: 2 x^{2}=1: 1
\end{aligned}
$$

19. (B) In $\triangle A C D$ and $\triangle A B C$,
$\angle \mathrm{CDA}=\angle \mathrm{CAB}=90^{\circ}$
$\because \angle \mathrm{C}$ is common.
$\triangle \mathrm{ACD} \sqcup \triangle \mathrm{ABC}$

$\therefore \frac{\triangle \mathrm{ACD}}{\triangle \mathrm{ABC}}=\frac{\mathrm{AC}^{2}}{\mathrm{BC}^{2}}$
$\Rightarrow \frac{10}{40}=\frac{9^{2}}{\mathrm{BC}^{2}}$
$\Rightarrow \mathrm{BC}^{2}=4 \times 9^{2}$
$\therefore \mathrm{BC}=2 \times 9=18 \mathrm{~cm}$
20. (B) A.T.Q,


$$
\begin{aligned}
\mathrm{OD} & =\sqrt{15^{2}-12^{2}} \\
& =\sqrt{225-144} \\
& =\sqrt{81}=9
\end{aligned}
$$

$$
\begin{aligned}
& \mathrm{OD}=\sqrt{13^{2}-12^{2}} \\
& \quad=\sqrt{169-144}=\sqrt{25}=5 \mathrm{~cm} \\
& \therefore \mathrm{OO}^{\prime}=9+5=14 \mathrm{~cm}
\end{aligned}
$$

21. (B) ATQ,

$\mathrm{DE} / / \mathrm{BC}$
$\angle \mathrm{ADE}=\angle \mathrm{ABC}$
$\angle \mathrm{AED}=\angle \mathrm{ACB}$
$\therefore \triangle \mathrm{ADE} \sqcup \triangle \mathrm{ABC}$
$\therefore \frac{\square \mathrm{BDEC}}{\triangle \mathrm{ADE}}=\frac{1}{1}$
$\Rightarrow \frac{\square \mathrm{BDEC}}{\triangle \mathrm{ADE}}+1=1+1$
$\Rightarrow \frac{\Delta \mathrm{ABC}}{\Delta \mathrm{ADE}}=2=\frac{\mathrm{AB}^{2}}{\mathrm{AD}^{2}}$
$\Rightarrow \frac{\mathrm{AB}}{\mathrm{AD}}=\sqrt{2} \Rightarrow \frac{\mathrm{AB}}{\mathrm{AD}}-1=\sqrt{2}-1$
$\Rightarrow \frac{\mathrm{AD}}{\mathrm{BD}}=\frac{1}{\sqrt{2}-1}$
$\mathrm{AD}: \mathrm{BD}=1: \sqrt{2}-1$
22. (B) A.T.Q,

$\mathrm{XZ}=r+9$ and $\mathrm{YZ}=r+2$
$\therefore \mathrm{XY}^{2}=\mathrm{XZ}^{2}+\mathrm{ZY}^{2}$
$\Rightarrow 17^{2}=(r+9)^{2}+(r+2)^{2}$
$\Rightarrow 289=r^{2}+18 r+81+r^{2}+4 r+4$
$\Rightarrow 2 r^{2}+22 r+85-289=0$
$\Rightarrow 2 r^{2}+22 r-204=0$
$\Rightarrow r^{2}+11 r-102=0$
$\Rightarrow r^{2}+17 r-6 r-102=0$
$\Rightarrow r(r+17)-6(r+17)=0$
$\Rightarrow(r-6)(r+17)=0$
$\Rightarrow r=6 \mathrm{~cm}$
23. (A) A.T.Q,


Length of transverse tangent
$=\sqrt{X Y^{2}-\left(r_{1}+r_{2}\right)}$
$\Rightarrow 8=\sqrt{\mathrm{XY}^{2}-9^{2}}$
$\Rightarrow 64=\mathrm{XY}^{2}-81$
$\Rightarrow X Y^{2}=64+81=145$
$\Rightarrow X Y=\sqrt{145}$
24. (C) $\because \mathrm{AB}$ is diameter
$\Rightarrow \angle \mathrm{ADB}=90^{\circ}$
also $\mathrm{DO} \perp \mathrm{AB}$ at ' $\mathrm{O}^{\prime}$ the centre of the circle,
$\therefore \triangle \mathrm{ADO} \cong \triangle \mathrm{BDO}$ (by SAS cong. Rule)
$\Rightarrow \mathrm{AD}=\mathrm{DB} \quad$ (by CPCT)
$\therefore \angle \mathrm{DAB}=\angle \mathrm{ABD}=45^{\circ}$
But $\angle \mathrm{ACD}=\angle \mathrm{ABD}$ (angles in the same segment of a circle)
$=45^{\circ}$
25. (A) $\angle \mathrm{CAD}=\angle \mathrm{CBD}$ (Angles in the same segment of a circle)
$=60^{\circ}$
Now $\angle \mathrm{BAD}=\angle \mathrm{BAC}+\angle \mathrm{CAD}$

$$
=30+60^{\circ}=90^{\circ}
$$

Now $\angle \mathrm{BAD}+\angle \mathrm{BCD}=180^{\circ}$
( $\therefore \square \mathrm{ABCD}$ is cyclic)
$\Rightarrow 90^{\circ}+\angle \mathrm{BCD}=180^{\circ}$
$\Rightarrow \angle \mathrm{BCD}=180^{\circ}-90^{\circ}=90^{\circ}$
26. (A) Perimeter of the rope
$=3 \times\left(\frac{1}{3}\right.$ of circumference of a circle +
$3 \times$ diameter of a circle)
$=3 \times \frac{1}{3} \times 2 \pi+3 \times 2$
$=2 \pi+6$
27. (A) A.T.Q,
$\because \mathrm{DC}|\mid \mathrm{AB}$ (given)
$\Rightarrow \triangle \mathrm{AOB} \sim \triangle \mathrm{COD}$ (by AA similarity)
$\Rightarrow \frac{\operatorname{ar}(\triangle \mathrm{AOB})}{\operatorname{ar}(\Delta \mathrm{COD})}=\frac{\mathrm{AB}^{2}}{\mathrm{DC}^{2}}$
$=\frac{(3 \mathrm{DC})^{2}}{\mathrm{DC}^{2}}=\frac{9 \mathrm{DC}^{2}}{\mathrm{DC}^{2}}=\frac{9}{1}=9: 1$
28. (B) In the given figure, $\triangle \mathrm{ABC}$ is a right angle triangle, where $\angle \mathrm{B}=90^{\circ}$
$\mathrm{AE}, \mathrm{BD}$ and CF are the 3 medians
Now, $\mathrm{AB}=12 \mathrm{~cm}, \mathrm{BC}=9 \mathrm{~cm}$ and $\mathrm{AC}=15 \mathrm{~cm}$
$\mathrm{BD}=\frac{1}{2} \mathrm{AC} \Rightarrow \mathrm{BD}^{2}=\frac{1}{4} \mathrm{AC}^{2 \mid}$
$\Rightarrow \mathrm{AE}^{2}+\mathrm{CF}^{2}=\frac{5}{4} \mathrm{AC}^{2}$
Also,
$\Rightarrow \mathrm{BD}^{2}+\mathrm{AE}^{2}+\mathrm{CF}^{2}=\left(\frac{1}{4}+\frac{5}{4}\right) \mathrm{AC}^{2}$
$=\frac{6}{4} \mathrm{AC}^{2}=\frac{6}{4} \times 225=337.5 \mathrm{~cm}$
29. (A) A.T.Q,

|  | Red | Yellow |  |
| ---: | :---: | :---: | :--- |
| Total | 5 | 4 | $\times 10$ |
| Upper half | 3 | 2 | $\times 9$ |

New Ratio becomes

|  | Red | Yellow |
| :--- | :--- | :--- |
| Total | 50 | 40 |
| Upper half | 27 | 18 |
| lower half | 23 | 22 |
| Then, |  |  |
| Required ratio $=23: 22$ |  |  |

30. (A) $\mathrm{d}_{\mathrm{m}}$ : diameter of the moon
$d_{e}$ : diameter of the earth

## Case - I

$\because \mathrm{d}_{\mathrm{m}}=\frac{1}{4} \mathrm{~d}_{\mathrm{e}}$
Let $r$ unit be the radius of the earth.
then, $\mathrm{d}_{\mathrm{m}}=\frac{1}{4} 2 r=\frac{r}{2}$ unit
$\mathrm{R}_{\mathrm{m}}$ : radius of the moon $=\frac{\mathrm{r}}{2 \times 2}=\frac{r}{4}$ unit
$\frac{V_{e}}{V_{m}}=\frac{\frac{4}{3} \pi r^{3}}{\frac{4}{3} \pi\left(\frac{r}{4}\right)^{3}}=64: 1$
31. (B) Perimeter $=2(l+b)$

$$
\mathrm{P}=2(l+w)
$$

$\frac{P}{2}-w=l$
Its area $=l \times b$
$k=\left(\frac{P}{2}-w\right) \times w_{\mathrm{s}}$
$\Rightarrow 2 k=P w-2 w^{2}$
$\Rightarrow 2 w^{2}-\mathrm{P} w+2 k=0$
32. (C) Volume of the ice-cream in cylindrical container $=\pi r^{2} h=\frac{22}{7} \times 6 \times 6 \times 15 \mathrm{~cm}^{3}$
Let rcm be the radius of the cone its height $=4 r \mathrm{~cm}$
Volume of 1 cone with hemispherical top
$=\frac{1}{3} \pi r^{2} h+\frac{2}{3} \pi r^{3}$
$=\frac{1}{3} \pi r^{2} \times 4 r+\frac{2}{3} \pi r^{3}$
$=\frac{4}{3} \pi r^{3}+\frac{2}{3} \pi r^{3}$
$=\frac{6}{3} \pi r^{3}=2 \pi r^{3}$
Volume of 10 such cones $=10 \times 2 \pi r^{3} \mathrm{~cm}^{3}$
A.T.Q,
$\frac{22}{7} \times 6 \times 6 \times 15=10 \times 2 \pi r^{3}$
$\frac{22}{7} \times 6 \times 6 \times 15=10 \times 2 \times \frac{22}{7} \times r^{3}$
$\Rightarrow r^{3}=\frac{6 \times 6 \times 15}{10 \times 5}=\frac{6 \times 6 \times 6}{2 \times 2 \times 2}$
$\Rightarrow r=\frac{6}{2} \mathrm{~cm}=3 \mathrm{~cm}$
33. (D) Time $=3: 18: 07-1: 55: 08$

$$
=1: 22: 59
$$

Total number of swith on

$$
\begin{aligned}
& =\frac{1 \times 3600+22 \times 60+59}{13} \\
& =384
\end{aligned}
$$

34. (A) Area of rectangular field $=\frac{1000}{1} \times 4 \mathrm{~m}^{2}$

$$
=4000 \mathrm{~m}^{2}
$$

$\because$ breadth $=50 \mathrm{~m}$
$\therefore$ Length $=\frac{4000}{50}=80 \mathrm{~m}$
New length of field $=(80+20) \mathrm{m}=100 \mathrm{~m}$
New area $=100 \times 50=5000$ sq.m
$\therefore$ Required expenditure $=₹\left(5000 \times \frac{1}{4}\right)$

$$
\text { = ₹ } 1250
$$

35. (C) Increase in water level
$=\frac{\text { Volume of sphere }}{\text { Area of base of cylinder }}$
$=\frac{\frac{4}{3} \pi r^{2}}{\pi r^{2}}=\frac{4}{3} r=\frac{4}{3} \times 3.5=\frac{14}{3} \mathrm{~cm}$.
$\therefore$ Required water level
$=7-\frac{14}{3}=\frac{7}{3} \mathrm{~cm}$.
36. (A) Curbed surface of cylinder $=2 \pi r h$

## Case - II

Radius $=\frac{1}{3} r:$ height $=6 h$
Curved surface $=2 \pi \times \frac{1}{3} r \times 6 h$
$=(2 \pi \mathrm{rh}) \times 2$
$\therefore$ Increase will be twice.
37. (A) Total cost price of 80 dozen

Bananas at ₹ 10 per dozen

$$
\text { = ₹ } 800
$$

12 dozen got rotten and its selling price is,

$$
\begin{aligned}
& =₹ 12 \times 6 \\
& =₹ 72
\end{aligned}
$$

Remaining dozens sell it 14 per dozen $=₹ 14 \times 68$
Total selling price $=1024$
Profit $\%=\frac{1024-800}{800} \times 100=28 \%$
38. (A) A.T.Q,
$2\left[2016^{2}-2015^{2}+2014^{2}-2013^{2}\right.$
$\left.+\ldots \ldots .+2^{2}-1^{2}\right]$
$=2[(2016+2015)(2016-2015)+(2014$
$+2013)(2014-2013) \ldots \ldots(2+1)(2-1)$
$=2[2016+2015+2014+2013+\ldots \ldots .+1]$
$=2 \times \frac{2016 \times 2017}{2}=2016 \times 2017$
Now, $2016 \times 2017=2016^{2}+2016$
$\therefore$ The number which must be subtracted
to make it a perfect square $=2016$
39. (C) S.I for 2 years $=\frac{16000 \times 15 \times 2}{100}=4800$

Principal for C.I $=16000+4800=20800$
C.I Rate $\rightarrow 12 \%=\frac{12}{100}=\frac{3}{25}$

Compound Interest for $1^{\text {st }}$ year
$=20800 \times \frac{3}{25}=2496$
C.I for $2^{\text {nd }}$ year $=20800 \times \frac{3}{25}+2496 \times \frac{3}{25}$
$=2496+299.52=2795.52$
Total interest after 4 years $=4800+2496$

+ 2796.52 = 10091.52

40. (C) Let 1 kg tea $=₹ 1$

20 kg tea $=₹ 20$


Profit $=\frac{21-18}{18} \times 100=16.66 \%$
41. (A) A.T.Q,


Area of the minor segment
$=$ sector area OABO - area of $\triangle \mathrm{OAB}$
$=\frac{3.14 \times 10 \times 10 \times 90^{\circ}}{360^{\circ}}-\frac{1}{2} \times 10 \times 10$
$=\frac{314}{4}-50=78.5-50=28.5 \mathrm{~cm}^{2}$
Area of the major segment
$=$ area of circle - area of minor segment
$=3.14 \times 10 \times 10-28.5$
$=314-28.5=205.5 \mathrm{~cm}^{2}$
42. (C) A.T.Q,


Total area of the square field
$=(44 \times 44) \mathrm{m}^{2}=1936 \mathrm{~m}^{3}$
At the rate of ₹ 1 per sq. metre, the total cost would be ₹ 1936 ,
but the total cost = ₹ 3536
Difference = ₹ 3536 - ₹ $1936=₹ 1600$
$\Rightarrow ₹ 1600$ would be the extra cost on the flower bed and as the extra cost on the flower bed is ₹ 1 per sq. metre
$\Rightarrow$ Area of flower bed $=1600$ sq. metres
$\Rightarrow$ Side of flower bed $=\sqrt{1600} \mathrm{~m}^{2}=40 \mathrm{~m}$
So, width of the gravel path $=\frac{44-40}{2}$
= 2 metres
43. (B) A.T.Q,

$\square \mathrm{ABCD}$ is a trapezium
Draw $\mathrm{CE} \| \mathrm{DA}$ intersecting AB at E .
$\Rightarrow \square \mathrm{ABCE}$ is a $\| \mathrm{gm}$.
$\Rightarrow \mathrm{DA}=\mathrm{CE}=26 \mathrm{~cm}$
In $\triangle B C E$,
$S=\frac{17+25+26}{2}=\frac{68}{2}=34$
Area ( $\triangle \mathrm{BCE}$ ),
$=\sqrt{34(34-17)(34-25)(34-26)} \mathrm{cm}^{2}$
$=\sqrt{34 \times 17 \times 9 \times 8}$
$=\sqrt{2 \times 17 \times 17 \times 3 \times 3 \times 2 \times 2 \times 2}$
$=2 \times 2 \times 3 \times 17=204 \mathrm{~cm}^{2}$
$\Rightarrow \frac{1}{2} \times \mathrm{BE} \times$ height $=204$
or, $\frac{1}{2} \times 17 \times \mathrm{CM}=204$
$\Rightarrow \mathrm{CM}=\frac{204 \times 2}{17}=24 \mathrm{~cm}$
Area $($ Trap. $A B C D)=\frac{1}{2} \times(60+77) \times 24$
$=\frac{1}{2} \times 137 \times 24=1644$ sq. cm
44. (B) A.T.Q,

$$
25 \%=\frac{1}{4}
$$

Time A : B
4:5
Effi 5: 4
Let, total work is W

| A | A+B | $B$ |
| :--- | :--- | :--- |
| $\frac{W}{2}$ | 4 days | $\frac{W}{20}$ |
| 5 | 9 | 4 |

$\frac{\mathrm{W}}{10}+4+\frac{\mathrm{W}}{80}=13$ days
$\Rightarrow \mathrm{W}=80$ units
$B$ alone does the work,
$\frac{80}{4}=20$ days
45. (C) A.T.Q,

Age $\geq 51 \rightarrow 30$
Age $<51 \rightarrow 39$ (at most)
(y)
( $x$ )
Overall average ages are $\rightarrow 38$ years
Largest possible average age,
$30 \times 51+x y=38(30+x)$
$\Rightarrow 390=(38-y)$
For y maximum $x=39$
$\Rightarrow 38-y=10$
$\Rightarrow y=28$ years
46. (D) A.T.Q,

Let the speed of Partha $\rightarrow$ P km/hr
Speed of Narayan $\rightarrow$ N km/hr

47. (B) Let the filling pipes capacity $\rightarrow x$

Draining pipes capacity $\rightarrow y$
$\frac{6}{x}-\frac{5}{y}=\frac{1}{6}$ and $\frac{5}{x}-\frac{6}{y}=\frac{1}{60}$
$x=12$ hours, $y=15$ hours
When 2 filling pipes and one draining pipe,
$\Rightarrow \frac{2}{12}-\frac{1}{15}=\frac{1}{10}$
Then the tank are filled in 10 hours
48. (D) A.T.Q,

$a+2 b+c=239$
$a+b+c=200$
From equation (i) and (ii)
So, maximum value of C is $=95$
Number of students who like Burger only
= 134 - $105=29$
$29 \leq$ Burger $\leq 95$


Let the area of $\triangle \mathrm{ABC}=x$
$x+\frac{x}{4}+\frac{x}{16}+$
It is an infinite G.P
$\frac{x}{1-\frac{x}{4}}=\frac{4 x}{3}=4 \times \frac{\sqrt{3}}{4} \times 576=192 \sqrt{3}$
50. (D) A.T.Q,


In $\triangle \mathrm{AEN}$

$$
x^{2}+y^{2}=a^{2}
$$

Let $x+y=8$
Area of squares $\mathrm{ABCD}=64$
Area of squares $\mathrm{EFGH}=64 \times \frac{5}{8}=40$
$x^{2}+y^{2}=40$
$x+y=8$
Let, $x=2, y=6$
Required ratio $=\frac{\mathrm{EB}}{\mathrm{CG}}=\frac{2}{6}=\frac{1}{3}$
51. (B) ATQ,

Let Raju have $4 x$ marbels and Lalitha have $9 x$
After giving some marbles by lalitha to raju
$\frac{4 x+y}{9 x-y}=\frac{5}{6}$
$\Rightarrow \frac{x}{y}=\frac{11}{21}$
$\mathrm{L} \rightarrow 99$
Required ratio $=\frac{21}{99}=\frac{7}{33}$
52. (B) A.T.Q,


Radius $=1 \mathrm{~cm}$
$\mathrm{OC}=\mathrm{OD}$
Area of $\triangle \mathrm{OCD}=\frac{\mathrm{R}}{2}$
$=\frac{1}{2}\left(\pi(1)^{2} \times \frac{1}{6}\right)$
Area of $\triangle \mathrm{COD}=\frac{\pi}{12}$
Area of $\triangle \mathrm{OCD}=\frac{\pi}{12}$
$\frac{1}{2} \mathrm{OC}^{2} \times \frac{\sqrt{3}}{2}=\frac{\pi}{12}$
$\Rightarrow \mathrm{OC}^{2}=\left(\frac{\pi}{3 \sqrt{3}}\right)^{1 / 2}$
$\Rightarrow \mathrm{OC}=\left(\frac{\pi}{3 \sqrt{3}}\right)^{1 / 2}$
Then the length of $\mathrm{OC}=\left(\frac{\pi}{3 \sqrt{3}}\right)^{1 / 2}$
53. (B) A.T.Q,

Let two points A and B


Speed $2 y$
$\frac{3 x}{y}-\frac{x}{2 y}=1$
$\Rightarrow \frac{x}{y}=\frac{2}{5}$
$\Rightarrow \frac{x}{2 y}=\frac{2}{5 \times 2} \times 60=12$ minutes
54. (C) A.T.Q,

First
Ins $\frac{11}{10} \times \frac{11}{10}$
Second
121
$\overline{100}$

210 units $\rightarrow ₹ 2,10,000$

121 units $\rightarrow$ ₹ 121,000
Hence, each instalments is $\rightarrow ₹ 121,000$
55. (A) A.T.Q,

Total sales tax $=₹(136.75-130)$
$\frac{9 y}{100}=6.75$
$y=₹ 75$
56. (D) When Sonu born sum of ages

$$
\begin{aligned}
& \mathrm{S} \rightarrow 66 \\
& \text { Age } \rightarrow 0
\end{aligned}
$$

Average of $S$ family at born of
Sonu $=\frac{66}{5}=13.2$
Present Average
S
$\longrightarrow \frac{96}{5}=19.2$
Difference in average $=19.2-13.2=6$ years
Average is increased by 6
So, age of sonu $=6$ years
Father age's $=6 \times 6=36$ years
Present age's of sonu father $=48$ years
57. (B) A.T.Q,

4 lemon +10 oranges
$\downarrow$
2 bottles of oranges
Total 3 oranges bottles
$x, y$ and $z$ have one bottles each
$z$ pays ₹50
Hence cost price of one bottle of orange is ₹50
58. (C) A.T.Q,

Let total property are $=16$ units
Mr. Sharma wife son $_{1} \quad$ son $_{2}$
16


After death 2 units given to his brother raj and to his brother raj and
2 units given his wife

11 units $\longrightarrow 88 \mathrm{k}$

1 unit $\longrightarrow 8 \mathrm{k}$
16 units $\longrightarrow ₹ 128,000$
59. (B) A.T.Q,

Case - I


## Case - II

When two more observation median are lies between the 21 observation hence median does not change.
Because median are positional function So, median remains same
60. (D) $\mathrm{A}: \quad \mathrm{B}$

64,000 : 112,000
After C join total profit 11 units is divided among three


A B
$4-\frac{11}{3} \quad 7-\frac{11}{3}$
$\downarrow \quad \downarrow$
Loss of A Loss of B
$11 \rightarrow 2,20,000$
$1 \rightarrow 20,000$
A : B : C
$4: 7$
$\begin{array}{ll}\frac{11}{3} & \frac{11}{3} \\ \frac{1}{3} & \frac{10}{3}\end{array}$

61. (B) A.T.Q,

## Case - I

Let cost price
Peanuts $\rightarrow ₹ x / \mathrm{kg}$
Walnut $\rightarrow$ ₹ $3 x / \mathrm{kg}$

| $\mathrm{P} \rightarrow x$ | $\mathrm{~W} \rightarrow 3 x$ |
| :--- | :--- |
| 8 kg | 6 kg |
| $10 \%$ | $20 \%$ |

$8 \times \frac{11}{10} x+16 \times \frac{18 x}{5}=\mathrm{CP}$ for shopkeeper
Case - II
After losing 5 kg walnuts and 3 kg peanuts,
$\mathrm{CP} \times \frac{5}{4}=166 \times 16$
$\mathrm{CP}=\frac{166 \times 16 \times 4}{5}$
$\frac{8 \times 11 x}{16}+16 \times \frac{18 x}{5}=166 \times \frac{4}{5} \times 16$
$x=32$
$3 x=96$
Hence, cost price of walnuts is ₹ $96 / \mathrm{kg}$
62. (B) Let $\mathrm{CP}=₹ 100$
$700 \mathrm{~A} \longrightarrow \mathrm{SP}=160$
$1 \mathrm{~A} \longrightarrow \mathrm{SP}=\frac{160}{700}=\frac{8}{35}$
730 articles $\longrightarrow \mathrm{SP}=\frac{8}{35} \times 730=167$
Profit $=67 \%$
63. (A) A.T.Q,

$\because$ Area $=48$
b $\times \mathrm{h}=48$

$$
\begin{aligned}
& h=6 \mathrm{~cm} \\
& \mathrm{~S} \geq 6
\end{aligned}
$$

64. (C) 33 men $\times 30$ days $=990$
$44+43+42 \ldots \ldots$.
$\frac{n}{2}[2 a+(n-1) d]$
$\frac{n}{2}[88+(n-1)(-1)]=990$
$\frac{n}{2}[89-n]=990$
Put value of $n$ from options or assume yourself
$n=44$
$\frac{44}{2}[89-44] \Rightarrow 22 \times 45=990$
$\therefore$ minimum number of days to finish the work $=44$ days
65. (D) A.T.Q,

Let numbers are $x, y$ and 73
$x y \times 73-x y \times 37=720$
$x y=20$
minimum value of $x^{2}+y^{2}$
$x=20$
$x=2 \sqrt{5}$ and $y=2 \sqrt{5}$
minimum value $=x^{2}+y^{2}=2 \times x^{2}$

$$
\begin{aligned}
& =2 \times(2 \sqrt{5})^{2} \\
& =2 \times 4 \times 5=40
\end{aligned}
$$

66. (A) A.T.Q,


Total time taken to cover 150 km
$=\frac{50}{100}+\frac{50}{50}+\frac{50}{25}$
$=\frac{1}{2}+1+2=3$ hours 30 minutes
Time taken to car ${ }_{1}$ to total 20 km
$=\frac{20}{100}=\frac{1}{5}$ hours $=12$ minutes
$\mathrm{Car}_{2}$ start travel at A after 12 minutes Hence $\mathrm{Car}_{2}$ travel 3 hours 18 minutes $\mathrm{Car}_{2}$, first $50 \mathrm{~km}+50 \mathrm{~km}$
30 minutes +1 hour $=1$ hour 30 minutes Remaining time $=1$ hour 48 minutes

$$
=\frac{9}{5} \text { hours }
$$

Distance $=\frac{9}{5} \times 25=45 \mathrm{~km}$
Difference $=50 \mathrm{~km}-45 \mathrm{~km}=5 \mathrm{~km}$
67. (B) A.T.Q,

$\frac{200}{\mathrm{C}_{1}}=\frac{100}{\mathrm{C}_{3}} \Rightarrow \frac{\mathrm{C}_{1}}{\mathrm{C}_{2}}=\frac{2}{1}$
$\frac{\mathrm{C}_{3}}{\mathrm{C}_{2}}=\frac{2}{1}$
$\mathrm{C}_{1}: \mathrm{C}_{2}: \mathrm{C}_{3}$
2 : 1 : (1)
(2) $: 2: 1$

4:2:1
Required ratio $=\frac{1}{4}$
68. (B) A.T.Q,
$(a+b+c)\left(\frac{1}{a}+\frac{1}{b}+\frac{1}{c}\right)$
$=1+\frac{a}{b}+\frac{a}{c}+\frac{b}{a}+1+\frac{b}{c}+\frac{c}{a}+\frac{c}{b}+1$
$=3+\left(\frac{a}{b}+\frac{b}{a}\right)+\left(\frac{b}{c}+\frac{c}{b}\right)+\left(\frac{c}{a}+\frac{a}{a}\right)$
Let, $\frac{a}{b}=x, \frac{b}{c}=y, \frac{c}{a}=z$
$=3+\left(x+\frac{1}{x}\right)+\left(y+\frac{1}{y}\right)+\left(z+\frac{1}{z}\right)$
Now, minimum value $=3+2+2+2=9$
69. (A) Putting the value of $x=y=z=2$ and $a=$ $b=c=3$ in all equation
$\Rightarrow \frac{a}{a+3 x}+\frac{b}{b+3 y}+\frac{c}{c+3 z}$
$=\frac{3}{9}+\frac{3}{9}+\frac{3}{9}=\frac{9}{9}=1$
70. (B) A.T.Q,
$a=1, b=-1, c=0$,
$a+b+c=0$
$\Rightarrow \frac{2\left(a^{4}+b^{4}+c^{4}\right)}{\left(a^{2}+b^{2}+c^{2}\right)}=\frac{2(1+1+0)}{(1+1+0)}=2$
71. (C) Let, $\frac{x}{y}=\frac{z}{w}=k$
$x=k y$ and $z=k w$
$\Rightarrow \frac{x^{m}+y^{m}+z^{m}+w^{m}}{x^{-m}+y^{-m}+z^{-m}+w^{-m}}$
$=\frac{k^{m} y^{m}+y^{m}+k^{m} w^{m}+w^{m}}{k^{-m} y^{-m}+y^{-m}+k^{-m} w^{-m}+w^{-m}}$
$=\frac{y^{m}\left(k^{m}+1\right)+w^{m}\left(k^{m}+1\right)}{y^{-m}\left(k^{-m}+1\right)+w^{-m}\left(k^{-m}+1\right)}$
$=\frac{\left(k^{m}+1\right)\left(y^{m}+w^{m}\right)}{\left(k^{-m}+1\right)\left(y^{-m}+w^{-m}\right)}$
$=\frac{\left(k^{m}+1\right)\left(y^{m}+w^{m}\right)}{\left(\frac{1}{k^{m}}+1\right)\left(\frac{1}{y^{m}}+\frac{1}{w^{m}}\right)}$
$=\frac{\left(k^{m}+1\right)\left(y^{m}+w^{m}\right)}{\frac{\left(k^{m}+1\right)}{k^{m}} \cdot \frac{\left(y^{m}+w^{m}\right)}{y^{m} \cdot w^{m}}}$
$=k^{\mathrm{m}} y^{\mathrm{m}} w^{\mathrm{m}}=(k y w)^{\mathrm{m}}=\left(k^{2} y^{2} w^{2}\right)^{\mathrm{m} / 2}$
$=(k y \cdot y \cdot w \cdot k w)^{\mathrm{m} / 2}=(x y z w)^{\mathrm{m} / 2}$
72. (C) $x^{2}(x+y+z)=36$
$y^{2}(x+y+z)=46$
$x^{2}(x+y+z)=63$
$x y(x+y+z)=111$
$\Rightarrow 2 x y(x+y+z)=222$
$y z(x+y+z)=99$
$\Rightarrow 2 y z(x+y+z)=198$
$z x(x+y+z)=82$
$\Rightarrow 2 z x(x+y+z)=164$
Adding all 6 equation,
$\Rightarrow(x+y+z)\left(x^{2}+y^{2}+z^{2}+2 x y+2 y z+2 z x\right)=729$
$\Rightarrow(x+y+z)(x+y+z)^{2}=729$
$\Rightarrow(x+y+z)^{3}=729$
$\Rightarrow x+y+z=9$
Putting the value of $x+y+z=9$ in equation (i)
$9 x^{2}=36$
$x^{2}=4$
$x=2$
73. (A) A.T.Q,

the distance from the point $(0,0)$ on the line $3 x+4 y+15=0$ is $O D$
$\mathrm{OD}=\left|\frac{0+0-15}{\sqrt{3^{2}+4^{2}}}\right|=3$
$\mathrm{BD}=\sqrt{\mathrm{OB}^{2}-\mathrm{DB}^{2}}=\sqrt{9^{2}-3^{2}}=\sqrt{72}=6 \sqrt{2}$
$\mathrm{AB}=2 \times \mathrm{BD}=12 \sqrt{2}$
(OAB is an isosceles triangle)
The area of triangle $\mathrm{OAB}=\frac{1}{2} \times 12 \sqrt{2} \times 3$

$$
=18 \sqrt{2}
$$

74. (C) $\tan 70^{\circ}=\frac{\tan 80^{\circ}-\tan 10^{\circ}}{1+\tan 80^{\circ} \tan 10^{\circ}}$

$$
\left(\because \tan 80^{\circ} \tan 10^{\circ}=1\right)
$$

$2 \tan 70^{\circ}+\tan 10^{\circ}=\tan 80^{\circ}$
75. (C) $\tan ^{n} 1^{\circ} \tan ^{n} 2^{\circ} \tan ^{n} 3^{\circ}$. $\tan 88^{\circ}$
$\tan 89^{\circ}=1$
$\left(\because \tan ^{\mathrm{n}} 1^{\circ}=\cot ^{\mathrm{n}} 89^{\circ}\right.$ व $\left.\tan ^{\mathrm{n}} 89^{\circ} \cdot \cot ^{\mathrm{n}} 89^{\circ}=1\right)$
76. (C) $\tan ^{5} \theta \cdot \tan ^{5} 5 \theta=1$
$(\tan \theta \cdot \tan 5 \theta)^{5}=1$
$\tan \theta \cdot \tan 5 \theta=1$
$\theta+5 \theta=90^{\circ}$
$6 \theta=90^{\circ}$
$3 \theta=45^{\circ}$
$\tan ^{n} 45^{\circ}=1$
77. (C) $\mathrm{A}+\mathrm{B}=90^{\circ}$
$\tan A=\cot B \quad(\Rightarrow \tan A \cdot \tan B=1)$
$\tan B=\cot A$
$\sin A=\cos B$
$\sin B=\cos A$
$=\sqrt{\frac{\tan A \tan B+\tan A \tan B}{\cos B \cdot \sec B}-\frac{\cos ^{2} A}{\cos ^{2} A}}$
$=\sqrt{\frac{2 \tan \mathrm{~A} \tan \mathrm{~B}}{1}-1}$
$=\sqrt{2-1}=1$
78. (B) $\frac{\mathrm{T}_{3}-\mathrm{T}_{5}}{\mathrm{~T}_{1}}=\frac{\sin ^{3} \theta+\cos ^{3} \theta-\sin ^{5} \theta-\cos ^{5} \theta}{\sin \theta+\cos \theta}$
$=\frac{\sin ^{3} \theta\left(1-\sin ^{2} \theta\right)+\cos ^{3} \theta\left(1-\cos ^{2} \theta\right)}{\sin \theta+\cos \theta}$
$=\frac{\sin ^{2} \theta \cos ^{2} \theta+\cos ^{3} \theta \sin ^{2} \theta}{\sin \theta+\cos \theta}$
$=\frac{\sin ^{2} \theta \cos ^{2} \theta(\sin \theta+\cos \theta)}{\sin \theta+\cos \theta}$
$=\sin ^{2} \theta \cdot \cos ^{2} \theta$
79. (B) $\cos (\theta-\mathrm{A})=\mathrm{a}, \cos (\theta-\mathrm{B})=\mathrm{b}$

Let, $\theta=90^{\circ}$
$\mathrm{a}=\cos \left(90^{\circ}-\mathrm{A}\right)=\sin \mathrm{A}$,
$b=\cos \left(90^{\circ}-B\right)=\sin B$
$\cos \mathrm{A}=\sqrt{1-a^{2}}, \cos \mathrm{~B}=\sqrt{1-b^{2}}$
$\Rightarrow \sin ^{2}(\mathrm{~A}-\mathrm{B})+2 a b \cos (\mathrm{~A}-\mathrm{B})$
$=(\sin A \cos B-\cos A \sin B)^{2}+2 a b(\cos A \cos B$
$+\sin A \sin B)$
$=\left(a \sqrt{1-b^{2}}-b \sqrt{1-a^{2}}\right)+$
$2 a b\left(\sqrt{1-a^{2}} \cdot \sqrt{1-b^{2}}+a b\right)$
$=a^{2}\left(1-b^{2}\right)+b^{2}\left(1-a^{2}\right)-2 a b \sqrt{1-a^{2}} \cdot \sqrt{1-b^{2}}$
$+2 a b \sqrt{1-a^{2}} \cdot \sqrt{1-b^{2}}+2 a^{2} b^{2}$
$=a^{2}-a^{2} b^{2}+b^{2}-a^{2} b^{2}+2 a^{2} b^{2}=a^{2}+b^{2}$
80. (C) $3 \cos \theta=5 \sin \theta$
$\tan \theta=\frac{3}{5} \Rightarrow \sec \theta=\sqrt{1+\tan ^{2} \theta}$
$=\sqrt{1+\frac{9}{25}}=\sqrt{\frac{34}{5}}$
$=\frac{\left(5 \tan \theta-2 \sec ^{4} \theta+2\right)}{\left(5 \tan \theta+2 \sec ^{4} \theta-2\right)}=\frac{5-2 \sec ^{4} \theta}{1+2 \sec ^{4} \theta}$
$=\frac{5-2\left(\frac{1156}{625}\right)}{1+2\left(\frac{1156}{625}\right)}=\frac{271}{979}$
81. (A) $\frac{\sin \mathrm{A}-\sin \mathrm{C}}{\cos \mathrm{C}-\cos \mathrm{A}}=\cot \mathrm{B}$
$=\frac{2 \cos \frac{A+C}{2} \cdot \sin \frac{A-C}{2}}{2 \sin \frac{A+C}{2} \cdot \sin \frac{A-C}{2}}=\cot B$
$=\cot \left(\frac{\mathrm{A}+\mathrm{C}}{2}\right)=\cot \mathrm{B}$
$\frac{\mathrm{A}+\mathrm{C}}{2}=\mathrm{B}=\mathrm{A} . \mathrm{P}$
82. (B) A.T.Q,

Total surface area of the pyramid = curve surface area + perimeter of base $\times$ slant height

$l_{1}=\sqrt{(5)^{2}+(12)^{2}}=13 \mathrm{~cm}$
Similarly, side AD and slant height $C D$ $l_{2}=\sqrt{(16)^{2}+(12)^{2}}=20 \mathrm{~cm}$
Area of triangle sides $A B$ and $C D$,
$=2 \times \frac{1}{2} \times 32 \times 13=416 \mathrm{~cm}^{2}$
Area of triangle sides AD and BC ,
$=2 \times\left(\frac{1}{2} \times 20 \times 10\right)=200 \mathrm{~cm}^{2}$

Curve surface area $=416+200=616 \mathrm{~cm}^{2}$
Base area $=32 \times 10=320 \mathrm{~cm}^{2}$
Total surface area of pyramid $=616+$ $320=936 \mathrm{~cm}^{2}$
83. (C) area of the hexagonal having base a
$=\frac{3 \sqrt{3}}{2} a^{2}$
$\frac{3 \sqrt{3}}{2} a^{2}=96 \sqrt{3} \Rightarrow a=8 \mathrm{~m}$
Let the height of the pyramid is $h \mathrm{~cm}$, then area of the pyramid of one face
$=\frac{1}{2} a \times l$ (where $l$ is slant height)
$\frac{1}{2} a \times l=32 \sqrt{3} \Rightarrow 1=8 \sqrt{3}$
$\frac{3 a^{2}}{4}+h^{2}=l^{2} \Rightarrow \frac{3 \times 64}{4}+h^{2}=64 \times 3$
$h^{2}=64 \times 3\left[1-\frac{1}{4}\right]=196$
$\Rightarrow h=12 \mathrm{~m}$
$\therefore$ Volume of the pyramid $=\frac{1}{3} \times$ base area $\times h$
$=\frac{1}{3} \times 96 \sqrt{3} \times 12=384 \sqrt{3} \mathrm{~m}^{3}$
84. (C)


Volume of cylinder = volume of cone
$\pi r^{2} h=\frac{1}{3} \pi r^{2}{ }_{1} h_{1}$
$\pi \times 18 \times 18 \times 32=\frac{1}{3} \pi \times r^{2} \times 24$
$r=36 \mathrm{~cm}$
85. (A)

$\pi r^{2} \mathrm{~h}_{2}=\frac{1}{3} \pi r^{2} \mathrm{~h}$
$\pi \mathrm{P}^{2} \mathrm{~h}_{1}=\frac{1}{3} \pi a^{2} \mathrm{~h}$
$h_{1}=\frac{a^{2} h}{3 \mathrm{P}^{2}}$
86. (C) Area of the shaded region,
$=\frac{1}{2} \pi(14)^{2}+\frac{1}{2} \pi(7)^{2}+\frac{1}{2}(7)^{2}$
$=\frac{1}{2} \pi(196+49+49)$
$=\frac{1}{2} \times \frac{22}{7} \times 294=462 \mathrm{~cm}^{2}$
87. (A) Area of larger square $=a^{2}$

Diagonal of smaller square $\mathrm{ABCD}=a$
Side of smaller square $=\frac{a}{\sqrt{2}}$
Now,
Side of smaller square $=$ diameter of circle $=\frac{a}{\sqrt{2}}$

Height of equilateral triangle $=\frac{3}{4} \times \frac{a}{\sqrt{2}}$
$=\frac{3 a}{4 \sqrt{2}}$
Hence,
side of equilateral triangle $=\frac{\sqrt{3} a}{2 \sqrt{2}}$
88. (C) A.T.Q,

BPC is an equilateral so all angles are $60^{\circ}$

$\therefore$ In $\triangle \mathrm{ABP}$
$\therefore \mathrm{AB}=\mathrm{BP}=\mathrm{a}$ (side os square)
$\therefore \angle \mathrm{APB}=\angle \mathrm{BAP}=75^{\circ}$
$\therefore$ similarly, $\angle \mathrm{DPC}=75^{\circ}$
$\because 60^{\circ}+75^{\circ}+75^{\circ}+\angle \mathrm{APD}=360^{\circ}$ $\angle \mathrm{APD}=150^{\circ}$
89. (B) ATQ,


Let say ' $r$ ' is the radius of the smaller circle,
$\therefore \mathrm{O}_{1} \mathrm{~A}=\mathrm{AB}=2$
$\therefore \mathrm{O}_{2} \mathrm{~B}=2 \sqrt{2}$
$\therefore \mathrm{O}_{1} \mathrm{C}+\mathrm{CB}=\mathrm{O}_{1} \mathrm{~B}$
$2+\mathrm{CO}_{2}+\mathrm{O}_{2} \mathrm{~B}=2 \sqrt{2}$
$2+r+r \sqrt{2}=2 \sqrt{2}$
$R=\frac{2(\sqrt{2}-1)}{\sqrt{2}+1}=6-4 \sqrt{2}$
90. (A) A.T.Q,
$\mathrm{BC}=2 \mathrm{~cm}$
$\mathrm{BP}=\mathrm{AP}=\mathrm{CD}=\mathrm{QD}=2 \mathrm{~cm}$
$=2 \times 3 \pi r_{\mathrm{s}}+2 \pi r_{1} \times 2+2 \mathrm{p} r_{\mathrm{m}}$
$=2 \times 2 \pi \times 1+2 \times \pi \times 2+2 \pi \times 1$
$=8 \pi+2 \pi=10 \pi \mathrm{~cm}$
91. (C)

| Year | Number of <br> students <br> employed | Number of <br> student <br> employed from <br> finance | Number of <br> student employed <br> from marketing |
| :---: | :---: | :---: | :---: |
| 1992 | 800 | $0.22 \times 800=175$ | $0.36 \times 800=288$ |
| 1993 | 650 | $0.17 \times 650=1105$ | $0.48 \times 650=312$ |
| 1994 | 1100 | $0.23 \times 1100=253$ | $0.43 \times 1100=473$ |
| 1995 | 1200 | $0.19 \times 1200=226$ | $0.37 \times 1200=444$ |
| 1996 | 1000 | $0.32 \times 1000=320$ | $0.32 \times 1000=320$ |
| Total |  | 1087.50 | 1837 |

Required difference,
= 1837 - 1087.5
$=179.5=750$
92. (D) Average salary of finance in 1992
= ₹5450 thousand
average salary of finance in 1996
= ₹9810 thousand
$\therefore$ Required percentage increase
$=\frac{9810-5450}{5450} \times 100 \%$
$=\frac{4360}{5450} \times 100 \%=80 \%$
93. (C) Salary offered in software
in $=1992=₹ 5290$ thousand
in = 1996 = ₹8640 thousand
$\therefore$ Percentage increase
$=\frac{8640-5290}{5290} \times 100 \%$
$=\frac{3350}{5290} \times 100 \%=63.32 \%$
Thus, required average annual increase rate $=\frac{1}{4} \times 63.32=15.9 \%$
94. (A) Average monthly salary to a marketing student,
in $1992=₹ 5170$ thousand
in $1996=₹ 10220$ thousand
$\therefore$ Required percentage increase
$=\frac{10220-5170}{5170} \times 100 \%$
$=\frac{5050}{5170} \times 100 \%=98 \%$
95. (B) In 1994, students seeking jobs in finance earned,
$=23 \%$ of $1100 \times 7550$
= ₹ 1910150
Students seeking jobs in software earned
$=21 \%$ of $1100 \times 7050$
= ₹ 1628550
$\therefore$ Difference in the amount earned
$=1910150-1628550=281600$
= ₹2.81 lakh per annum
$=₹ 2.81 \times 12$ lakh per annum
$=₹ 33.8$ lakh per annum

Using this chart for giving answer (96-100)
Total number of students in the
school = 3000
Number of girls $=\frac{7}{15} \times 3000=1400$

Number of boys $=\frac{8}{15} \times 3000=1600$
Number of boys studying only English $=30 \%$ of $1600=480$
Number of girls studying only English and Hindi $=\frac{2}{7}$ th of 1400
Number of boys studying English and Marathi only $=\frac{1}{8}$ th of 1600
Number of girls studying only English
$=85 \%$ of $480=408$
Number of boys studying only Hindi and
Marathi $=\frac{2}{5}$ th of $1600=640$
Number of girls studying only hindi $=$ $40 \%$ of $1400=560$ Number of girls studying only Hindi and Marathi
$=1400-(400+408+560)$
$=1400-1368=32$
Number of boys studying only English and Hindi
$=10 \%$ of $400=40$
Number of boys studying only Hindi
$=1600-(480+200+640+40)$
$=1600-1360=240$
The tabular form of above information is as follows.

| Subjects | Number of girls | Number of boys |
| :---: | :---: | :---: |
| Hindi | 560 | 240 |
| English | 408 | 480 |
| Marathi | - | - |
| Hindi+English | 400 | 40 |
| English+Marathi | - | 200 |
| Hindi+Marathi | 32 | 640 |
| Total | 1400 | 1600 |

96. (A) Total number of boys studying English $=480+40+200=720$
Total number of girls studying English
$=408+400=808$
$\therefore$ Required ratio $=720: 808:=90: 101$
97. (D) Number of boys studying only Hindi
$=240$ and number of girls studying Hindi
$=560+400+320=992$
$\therefore$ Required percentage,
$=\frac{240}{992} \times 100 \%=24.19 \%$
98. (B) Total number of students studying only English $=408+480=888$
99. (D) Number of girls studying Marathi $=32$
$\therefore$ Number of girls not studying Marathi
$=1400-32=1368$
100. (C) Total number of girls studying Hindi
$=560+400+32=992$

## SSC TIER II (MATHS) MOCK TEST - 52 (ANSWER KEY)

| 1. (D) | 11. (A) | 21. (B) | 31. (B) | 41. (A) | 51. (B) | 61. (B) | 71. (C) | 81. (A) | 91. (C) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. (B) | 12. (C) | 22. (B) | 32. (C) | 42. (C) | 52. (B) | 62. (B) | 72. (C) | 82. (B) | 92. (D) |
| 3. (A) | 13. (B) | 23. (A) | 33. (D) | 43. (B) | 53. (B) | 63. (A) | 73. (A) | 83. (C) | 93. (C) |
| 4. (A) | 14. (B) | 24. (C) | 34. (A) | 44. (B) | 54. (C) | 64. (C) | 74. (C) | 84. (C) | 94. (A) |
| 5. (A) | 15. (A) | 25. (A) | 35. (C) | 45. (C) | 55. (A) | 65. (D) | 75. (C) | 85. (A) | 95. (B) |
| 6. (B) | 16. (A) | 26. (A) | 36. (A) | 46. (D) | 56. (D) | 66. (A) | 76. (C) | 86. (C) | 96. (A) |
| 7. (A) | 17. (C) | 27. (A) | 37. (A) | 47. (B) | 57. (B) | 67. (B) | 77. (C) | 87. (A) | 97. (D) |
| 8. (B) | 18. (A) | 28. (B) | 38. (A) | 48. (D) | 58. (C) | 68. (B) | 78. (B) | 88. (C) | 98. (B) |
| 9. (C) | 19. (B) | 29. (A) | 39. (C) | 49. (D) | 59. (B) | 69. (A) | 79. (B) | 89. (B) | 99. (D) |
| 10. (A) | 20. (B) | 30. (A) | 40. (C) | 50. (D) | 60. (D) | 70. (B) | 80. (C) | 90. (A) | 100. (C) |

Note:- If your opinion differs regarding any answer, please message the mock test and question number to 8860330003

Note:- Whatsapp with Mock Test No. and Question No. at 7053606571 for any of the doubts. Join the group and you may also share your suggestions and experience of Sunday Mock

