

NDA MATHS MOCK TEST - 148 (SOLUTION)

1. (B) Let Probability of success $(p) = \frac{1}{3}$

and probability of unsuccess $(q) = \frac{2}{3}$

Let x is random variable which show for solving 5 questions. It is clear that

$x \sim$ binomial distribution $\left(5, \frac{1}{3}\right)$

$$\therefore P(X = x) = {}^5C_x \left(\frac{1}{3}\right)^x \left(\frac{2}{3}\right)^{5-x}$$

(where $k = 0, 1, \dots, 5$)

\therefore Required Probability

$$P(X \geq 3) = P(X = 3) + P(X = 4) + P(X = 5)$$

$$= {}^5C_3 \left(\frac{1}{3}\right)^3 \left(\frac{2}{3}\right)^2 + {}^5C_4 \left(\frac{1}{3}\right)^4 \left(\frac{2}{3}\right)^1 + {}^5C_5 \left(\frac{1}{3}\right)^5$$

$$= \frac{10 \times 4}{3^5} + \frac{5 \times 2}{3^5} + \frac{1 \times 1}{3^5}$$

$$= \frac{51}{3^5} = \frac{17}{81}$$

2. (A) Given that

$$\int x^2 \cdot e^x dx = ax^2 \cdot e^x + bx \cdot e^x + c \cdot e^x + d \quad \dots(i)$$

$$\text{Let } I = \int x^2 \cdot e^x dx$$

$$I = x^2 \cdot \int e^x dx - \int \left\{ \frac{d}{dx}(x^2) \cdot \int e^x dx \right\} dx$$

$$I = x^2 \cdot e^x - \int 2x \cdot e^x dx$$

$$I = x^2 \cdot e^x - 2 \left[x \cdot \int e^x dx - \int \left\{ \frac{d}{dx}(x) \cdot \int e^x dx \right\} dx \right]$$

$$I = x^2 \cdot e^x - 2 \left[x \cdot e^x - \int 1 \cdot e^x dx \right] + d$$

$$I = x^2 \cdot e^x - 2 \left[x \cdot e^x - e^x \right] + d$$

$$I = x^2 \cdot e^x - 2x \cdot e^x + 2 \cdot e^x + d$$

On comparing with eq(i)

$$a = 1, b = -2 \text{ and } c = 2$$

3. (D) In ΔABC , $c = 4$, $A = \angle 60^\circ$ and $\angle B = 75^\circ$, then $\angle C = 45^\circ$

Sine Rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\text{Now, } \frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\Rightarrow \frac{a}{\sin 60} = \frac{4}{\sin 45}$$

$$\Rightarrow \frac{a}{\sqrt{3}/2} = \frac{4}{1/\sqrt{2}}$$

$$\Rightarrow a = 4 \cdot \sqrt{2} \times \frac{\sqrt{3}}{2} \Rightarrow a = 2\sqrt{6}$$

$$4. (C) I = \int_0^{\pi/2} \frac{\phi(x)}{\phi\left(\frac{\pi}{2} - x\right) + \phi(x)} dx \quad \dots(i)$$

$$\text{Prop. IV } \int_0^a f(x) dx = \int_0^a f(a-x) dx$$

$$I = \int_0^{\pi/2} \frac{\phi\left(\frac{\pi}{2} - x\right)}{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)} dx \quad \dots(ii)$$

from eq(i) and eq(ii)

$$2I = \int_0^{\pi/2} \frac{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)}{\phi(x) + \phi\left(\frac{\pi}{2} - x\right)} dx$$

$$2I = \int_0^{\pi/2} 1 dx$$

$$2I = [x]_0^{\pi/2}$$

$$2I = \frac{\pi}{2} - 0 \Rightarrow I = \frac{\pi}{4}$$

5. (A) $\tan A = 3$ and $\tan B = -2$

$$\text{Now, } \tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \cdot \tan B}$$

$$\Rightarrow \tan(A - B) = \frac{3 - (-2)}{1 + 3 \times (-2)}$$

$$\Rightarrow \tan(A - B) = \frac{5}{-5}$$

$$\Rightarrow \tan(A - B) = -1$$

$$\Rightarrow \tan(A - B) = \tan \frac{3\pi}{4}$$

$$\Rightarrow A - B = \frac{3\pi}{4}$$



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6. (B) Differential equation
 $y^2 dx = x^3 y^2 dx + x^2 dy$
 $\Rightarrow y^2 dx - x^2 dy = x^3 y^2 dx$
 $\Rightarrow \frac{y^2 dx - x^2 dy}{x^2 y^2} = x dx$
 $\Rightarrow \frac{dx}{x^2} - \frac{dy}{y^2} = x dx$
 On integrating
 $\Rightarrow \int \frac{dx}{x^2} - \int \frac{dy}{y^2} = \int x dx$
 $\Rightarrow \frac{-1}{x} + \frac{1}{y} = \frac{x^2}{2} + \frac{c}{2}$
 $\Rightarrow \frac{1}{y} - \frac{1}{x} = \frac{x^2 + c}{2}$
 $\Rightarrow \frac{2(x-y)}{xy} = x^2 + c$
 $\Rightarrow 2(x-y) = x^3 y + cxy$

7. (C) $I = \int_0^1 \frac{\tan^{-1} x}{1+x^2} dx$
 Let $\tan^{-1} x = t$ when $x = 0, t = 0$
 $\frac{1}{1+x^2} dx = dt$ $x = 1, t = \frac{\pi}{4}$
 $I = \int_0^{\pi/4} t dt$
 $I = \left[\frac{t^2}{2} \right]_0^{\pi/4}$
 $I = \frac{1}{2} \left[\frac{\pi^2}{16} - 0 \right] = \frac{\pi^2}{32}$

8. (C) We know that
 $\cos 36^\circ = \frac{\sqrt{5}+1}{4}$ and $\sin 18^\circ = \frac{\sqrt{5}-1}{4}$
 Now, $\cos 36^\circ \cdot \sin 18^\circ$
 $\Rightarrow \frac{\sqrt{5}+1}{4} \times \frac{\sqrt{5}-1}{4}$
 $\Rightarrow \frac{5-1}{16} = \frac{4}{16} = \frac{1}{4}$

9. (A) Odd natural numbers
 1, 3, 5, n
 Sum = 1 + 3 + 5 + n
 Sum = $\frac{n}{2} (2 \times 1 + (n-1) \times 2)$
 Sum = $\frac{n}{2} (2 + 2n - 2)$
 Sum = $\frac{n}{2} \times 2n = n^2$
 Mean = $\frac{n^2}{n} = n$

10. (D) $z = \frac{\sqrt{3}-2i}{\sqrt{3}+2i}$
 $z = \frac{\sqrt{3}-2i}{\sqrt{3}+2i} \times \frac{\sqrt{3}-2i}{\sqrt{3}-2i}$
 $z = \frac{3+4i^2-4\sqrt{3}i}{3-4i^2}$
 $z = \frac{-1-4\sqrt{3}i}{3+4}$
 $z = \frac{-1-4\sqrt{3}i}{7}$
 $|z| = \frac{\sqrt{(-1)^2 + (4\sqrt{3})^2}}{7}$
 $|z| = \frac{\sqrt{1+48}}{7}$
 $|z| = \frac{7}{7} = 1$

11. (C)

2	47	1
2	23	1
2	11	1
2	5	1
2	2	0
2	1	1
0		

 ↑

Hence $(47)_{10} = (101111)_2$

12. (B) $\sec^{-1} \left(\sec \frac{5\pi}{3} \right)$
 $\Rightarrow \sec^{-1} \left[\sec \left(2\pi - \frac{\pi}{3} \right) \right]$
 $\Rightarrow \sec^{-1} \left(\sec \frac{\pi}{3} \right) = \frac{\pi}{3}$

13. (A) Matrix $\begin{bmatrix} x-1 & 2 & 3 \\ 2 & 6 & 0 \\ 4 & -1 & 3 \end{bmatrix}$ is an invertible,
 then $\begin{vmatrix} x-1 & 2 & 3 \\ 2 & 6 & 0 \\ 4 & -1 & 3 \end{vmatrix} = 0$
 $\Rightarrow (x-1)(18-0) - 2(6-0) + 3(-2-24) = 0$
 $\Rightarrow 18(x-1) - 12 - 78 = 0$
 $\Rightarrow 18(x-1) = 90$
 $\Rightarrow x-1 = 5 \Rightarrow x = 6$



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14. (B) $\sin^{-1} \frac{7}{25} + \cos^{-1} \frac{3}{5}$

$$\Rightarrow \tan^{-1} \frac{7}{24} + \tan^{-1} \frac{4}{3}$$

$$\Rightarrow \tan^{-1} \left[\frac{\frac{7}{24} + \frac{4}{3}}{1 - \frac{7}{24} \times \frac{4}{3}} \right]$$

$$\Rightarrow \tan^{-1} \left[\frac{21+96}{72-28} \right] \Rightarrow \tan^{-1} \frac{117}{44}$$

15. (C) $\begin{vmatrix} 2! & 3! & 4! \\ 5! & 6! & 7! \\ 8! & 9! & 10! \end{vmatrix}$

$$\Rightarrow \begin{vmatrix} 2! & 3 \times 2! & 4 \times 3 \times 2! \\ 5! & 6 \times 5! & 7 \times 6 \times 5! \\ 8! & 9 \times 8! & 10 \times 9 \times 8! \end{vmatrix}$$

$$\Rightarrow 2! \times 5! \times 8! \begin{vmatrix} 1 & 3 & 12 \\ 1 & 6 & 42 \\ 1 & 9 & 90 \end{vmatrix}$$

$R_2 \rightarrow R_2 - R_1$ and $R_3 \rightarrow R_3 - R_1$

$$\Rightarrow 2! \times 5! \times 8! \begin{vmatrix} 1 & 3 & 12 \\ 0 & 3 & 30 \\ 0 & 6 & 78 \end{vmatrix}$$

$$\Rightarrow 2! \times 5! \times 8! \times (3 \times 78 - 6 \times 30) - 0$$

$$\Rightarrow 2! \times 5! \times 8! \times (234 - 180)$$

$$\Rightarrow 54 \times 2! \times 5! \times 8!$$

16. (B) $y = \ln(e^{2x} + e^{-2x})$
On differentiating both side w.r.t 'x'

$$\frac{dy}{dx} = \frac{1}{e^{2x} + e^{-2x}} (2e^{2x} - 2e^{-2x})$$

$$\frac{dy}{dx} = \frac{2(e^{2x} - e^{-2x})}{e^{2x} + e^{-2x}}$$

Again, differentiating

$$\frac{d^2y}{dx^2} = 2 \times \frac{(e^{2x} + e^{-2x})(2e^{2x} + 2e^{-2x}) - (e^{2x} - e^{-2x})(2e^{2x} - 2e^{-2x})}{(e^{2x} + e^{-2x})^2}$$

$$\frac{d^2y}{dx^2} = 4 \times \frac{(e^{2x} + e^{-2x})^2 - (e^{2x} - e^{-2x})^2}{(e^{2x} + e^{-2x})^2}$$

$$\frac{d^2y}{dx^2} = 4 \times \frac{(e^{4x} + 2 + e^{-4x}) - (e^{4x} - 2 + e^{-4x})}{(e^{2x} + e^{-2x})^2}$$

$$\frac{d^2y}{dx^2} = 4 \times \frac{2+2}{(e^{2x} + e^{-2x})^2} = \frac{16}{(e^{2x} + e^{-2x})^2}$$

17. (B) Three points (x, 1), (-2, 3) and (2, -1) are

collinear, then $\begin{vmatrix} x & 1 & 1 \\ -2 & 3 & 1 \\ 2 & -1 & 1 \end{vmatrix} = 0$

$$\Rightarrow x(3+1) - 1(-2-2) + 1(2-6) = 0$$

$$\Rightarrow 4x + 4 - 4 = 0 \Rightarrow x = 0$$

18. (B) $\cos^2 5^\circ + \cos^2 10^\circ + \cos^2 15^\circ + \dots + \cos^2 90^\circ$

$$\Rightarrow \cos^2 5^\circ + \cos^2 10^\circ + \cos^2 15^\circ + \dots + \cos^2 15^\circ + \cos^2 80^\circ + \cos^2 85^\circ + 0$$

$$\Rightarrow (\cos^2 5^\circ + \cos^2 85^\circ) + (\cos^2 10^\circ + \cos^2 80^\circ) + \dots + (\cos^2 40^\circ + \cos^2 50^\circ) + \cos^2 45^\circ$$

$$\Rightarrow (\cos^2 5^\circ + \sin^2 5^\circ) + (\cos^2 10^\circ + \sin^2 10^\circ) + \dots$$

$$\dots + (\cos^2 40^\circ + \sin^2 40^\circ) + \left(\frac{1}{\sqrt{2}}\right)^2$$

$$\Rightarrow 1 + 1 + 1 + \dots \text{ 8 times } + \frac{1}{2}$$

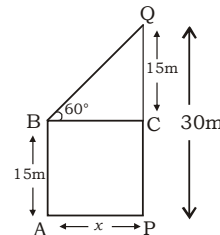
$$\Rightarrow 8 + \frac{1}{2} = \frac{17}{2}$$

19. (C) $S = \sqrt{3} + 2\sqrt{3} + 4\sqrt{3} + \dots n$ terms

$$S = \frac{\sqrt{3}(2^n - 1)}{2 - 1}$$

$$S = \sqrt{3}(2^n - 1)$$

20. (B) Distance between poles = x m



In $\triangle ABCQ$

$$\tan 60^\circ = \frac{QC}{BC}$$

$$\Rightarrow \sqrt{3} = \frac{15}{x}$$

$$\Rightarrow x = \frac{15}{\sqrt{3}} \Rightarrow x = 5\sqrt{3} \text{ m}$$

21. (B) $x = \omega^2 + 2 - \omega$

$$\Rightarrow x - 2 = \omega^2 - \omega$$

On squaring both side

$$\Rightarrow x^2 + 4 - 4x = \omega^4 + \omega^2 - 2\omega^3$$

$$\Rightarrow x^2 + 4 - 4x = \omega + \omega^2 - 2$$

$$\Rightarrow x^2 - 4x + 4 = -1 - 2 \quad [\because 1 + \omega + \omega^2 = 0]$$

$$\Rightarrow x^2 + 4x + 7 = 0$$

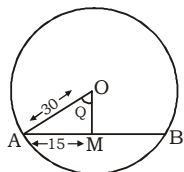
22. (C) $\frac{1}{1 \times 5} + \frac{1}{5 \times 9} + \frac{1}{9 \times 13} + \dots + \frac{1}{25 \times 29}$

$$\Rightarrow \frac{1}{4} \left(1 - \frac{1}{5}\right) + \frac{1}{4} \left(\frac{1}{5} - \frac{1}{9}\right) + \dots + \frac{1}{4} \left(\frac{1}{25} - \frac{1}{29}\right)$$

$$\Rightarrow \frac{1}{4} \left(1 - \frac{1}{29}\right)$$

$$\Rightarrow \frac{1}{4} \times \frac{28}{29} = \frac{7}{29}$$

23. (B) Given that $d = 60 \text{ cm} \Rightarrow r = 30 \text{ cm}$ and $AB = 30 \text{ cm}$



$AM = 15 \text{ cm}$

Let $\angle AOM = \theta$

Now, $\sin \theta = \frac{AM}{AO}$

$$\Rightarrow \sin \theta = \frac{15}{30}$$

$$\Rightarrow \sin \theta = \frac{1}{2} \Rightarrow \theta = \frac{\pi}{6}$$

Now, $\theta = \frac{S}{\pi}$

$$\Rightarrow \frac{\pi}{6} = \frac{S}{30} \Rightarrow S = 5\pi$$

Hence length of arc = $5\pi \text{ cm}$

24. (C) $\cos\left(\frac{\pi}{4} - \theta\right) + \cos\left(\frac{\pi}{4} + \theta\right)$

$$\Rightarrow 2 \cos \frac{\frac{\pi}{4} - \theta + \frac{\pi}{4} + \theta}{2} \cdot \cos \frac{\frac{\pi}{4} - \theta - \frac{\pi}{4} - \theta}{2}$$

$$\Rightarrow 2 \cos \frac{\pi}{4} \cdot \cos \theta$$

$$\Rightarrow 2 \times \frac{1}{\sqrt{2}} \cos \theta = \sqrt{2} \cos \theta$$

25. (B) $1 + \frac{1}{(1+2)} + \frac{1}{(1+2+3)} + \dots + \frac{1}{(1+2+3+\dots+n)}$

$$T_n = \frac{1}{1+2+3+\dots+n}$$

$$T_n = \frac{2}{n(n+1)}$$

Now, $S_n = \sum T_n$

$$S_n = \sum \frac{2}{n(n+1)}$$

$$S_n = 2 \sum \left(\frac{1}{n} - \frac{1}{n+1}\right)$$

$$S_n = 2 \left[\left(1 - \frac{1}{2}\right) + \left(\frac{1}{2} - \frac{1}{3}\right) + \dots + \left(\frac{1}{n} - \frac{1}{n+1}\right) \right]$$

$$S_n = \left[1 - \frac{1}{n+1}\right] = \frac{2n}{n+1}$$

26. (B) Given that $z_1 = 2 + i$ and $z_2 = 1 - 2i$

Now, $\left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \left| \frac{2 + i + 1 - 2i - 1}{2 + i - 1 + 2i + 1} \right|$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \left| \frac{2 - i}{2 + 3i} \right|$$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \left| \frac{2 - i}{2 + 3i} \times \frac{2 - 3i}{2 - 3i} \right|$$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \left| \frac{1 - 8i}{4 - 9i^2} \right|$$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \left| \frac{1 - 8i}{13} \right|$$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \frac{\sqrt{i^2 + (-8)^2}}{13}$$

$$\Rightarrow \left| \frac{z_1 + z_2 - 1}{z_1 - z_2 + 1} \right| = \frac{\sqrt{65}}{13} = \sqrt{\frac{5}{13}}$$

27. (C) $\begin{array}{|c|c|c|c|c|c|} \hline 1 & 1 & 8 & 7 & 6 & 5 \\ \hline \end{array} = 8 \times 7 \times 6 \times 5$

$\downarrow \quad \downarrow$
7 5

= 1680

28. (D) ${}^nC_r + {}^nC_{r+1}$

$$\Rightarrow \frac{n!}{r!(n-r)!} + \frac{n!}{(r+1)!(n-r-1)!}$$

$$\Rightarrow \frac{n!}{r!(n-r)(n-r-1)!} + \frac{n!}{(r+1)r!(n-r-1)!}$$

$$\Rightarrow \frac{n!}{r!(n-r-1)!} \left[\frac{1}{n-r} + \frac{1}{r+1} \right]$$

$$\Rightarrow \frac{n! [r+1+n-r]}{r!(n-r-1)!(n-r)(r+1)}$$

$$\Rightarrow \frac{(n+1)n!}{(r+1)r!(n-r)(n-r-1)!}$$

$$\Rightarrow \frac{(n+1)!}{(r+1)!(n-r)!} = {}^{n+1}C_{r+1}$$

29. (C) A.T.Q.

$$a + ar + ar^2 = 27 \quad \dots(i)$$

$$\text{and } ar^3 + ar^4 + ar^5 = 729$$

$$\Rightarrow r^3(a + ar + ar^2) = 729$$

$$\Rightarrow r^3 \times 27 = 729$$

$$\Rightarrow r^3 = 27 \Rightarrow r = 3$$

from equ. (i)

$$a + a \times 3 + a \times 9 = 27$$

$$\Rightarrow 13a = 27 \Rightarrow a = \frac{27}{13}$$

$$\text{Hence first term} = \frac{27}{13}$$

30. (B) Line

$$6(2x - 3) = 5(y + 1)$$

$$\Rightarrow 12x - 18 = 5y + 5$$

$$\Rightarrow 12x - 5y = 23 \Rightarrow 12x - 5y - 23 = 0$$

$$\text{The required distance} = \frac{12 \times 1 - 5(-2) - 23}{\sqrt{12^2 + (-5)^2}}$$

$$= \frac{|12 + 10 - 23|}{\sqrt{169}} = \frac{1}{13}$$

31. (C) Given that $m_1 = 3$, $\theta = 45^\circ$

$$\text{then } \tan \theta = \frac{m_1 - m_2}{1 + m_1 m_2}$$

$$\Rightarrow \tan 45^\circ = \frac{3 - m_2}{1 + 3 \times m_2}$$

$$\Rightarrow 1 = \frac{3 - m_2}{1 + 3 \times m_2}$$

$$\Rightarrow 1 + 3m_2 = 3 - m_2 \Rightarrow m_2 = \frac{1}{2}$$

Equation of line passing through the point $(2, -3)$

$$y + 3 = \frac{1}{2}(x - 2)$$

$$\Rightarrow 2y + 6 = x - 2 \Rightarrow x - 2y = 8$$

32. (C) $\lim_{x \rightarrow 2} \left[\frac{x^3 - 2x^2}{x^3 - 3x + 2} \right] \left[\frac{0}{0} \right]$ form

by L-Hospital's Rule

$$\Rightarrow \lim_{x \rightarrow 2} \frac{3x^2 - 4x}{3x^2 - 3}$$

$$\Rightarrow \frac{3 \times 2^2 - 4 \times 2}{3 \times 2^2 - 3}$$

$$\Rightarrow \frac{12 - 8}{12 - 3} = \frac{4}{9}$$

33. (D) C.V. (1st distribution) = 60, $\sigma_1 = 21$

C.V. (2nd distribution) = 80, $\sigma_2 = 16$

Let x_1 and x_2 be the means of 1st and 2nd distribution respectively, then

$$\text{C.V. (1st distribution)} = \frac{\sigma_1}{x_1} \times 100$$

$$\Rightarrow 60 = \frac{21}{x_1} \times 100$$

$$\Rightarrow x_1 = \frac{21}{60} \times 100 \Rightarrow x_1 = 35$$

$$\text{and C.V. (2nd distribution)} = \frac{\sigma_2}{x_2} \times 100$$

$$\Rightarrow 80 = \frac{16}{x_2} \times 100$$

$$\Rightarrow x_2 = \frac{16}{80} \times 100 \Rightarrow x_2 = 20$$

Hence means are 35 and 20.

34. (A)

35. (B) We know that

$$\tan^{-1} x = \sin^{-1} \frac{x}{\sqrt{1+x^2}}$$

$$36. (C) [x \ -2 \ 2] \begin{bmatrix} 1 & 0 & -3 \\ 2 & -1 & 4 \\ 3 & -2 & -1 \end{bmatrix} \begin{bmatrix} -2 \\ 3 \\ 0 \end{bmatrix} = 0$$

$$\Rightarrow [x \ -2 \ 3] \begin{bmatrix} -2 \\ -7 \\ -12 \end{bmatrix} = [0]$$

$$\Rightarrow [-2x + 14 - 36] = [0]$$

$$\Rightarrow -2x - 22 = 0 \Rightarrow x = -11$$

$$37. (B) \begin{bmatrix} bc & 1 & a(b+c) \\ ca & 1 & b(c+a) \\ ab & 1 & c(a+b) \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} bc & 1 & ab+ca \\ ca & 1 & bc+ab \\ ab & 1 & ca+bc \end{bmatrix}$$

$$C_3 \rightarrow C_3 + C_1$$

$$\Rightarrow \begin{bmatrix} bc & 1 & ab+bc+ca \\ ca & 1 & ab+bc+ca \\ ab & 1 & ab+bc+ca \end{bmatrix}$$

$$\Rightarrow (ab + bc + ca) \begin{bmatrix} bc & 1 & 1 \\ ca & 1 & 1 \\ ab & 1 & 1 \end{bmatrix}$$

$$\Rightarrow 0 \quad [\because \text{Two columns are identical.}]$$

38. (B) $A = \begin{bmatrix} -4 & 5 \\ -2 & 3 \end{bmatrix}$

$$|A| = -12 + 10 = -2$$

Co-factors of A-

$$C_{11} = (-1)^{1+1} (3) = 3, \quad C_{12} = (-1)^{1+2} (-2) = 2$$

$$C_{21} = (-1)^{2+1} (5) = -5, \quad C_{22} = (-1)^{2+2} (-4) = -4$$

$$C = \begin{bmatrix} 3 & 2 \\ -5 & -4 \end{bmatrix}$$

$$\text{Adj}A = C^T = \begin{bmatrix} 3 & -5 \\ 2 & -4 \end{bmatrix}$$

$$A^{-1} = \frac{\text{Adj}A}{|A|}$$

$$A^{-1} = \frac{\begin{bmatrix} 3 & -5 \\ 2 & -4 \end{bmatrix}}{-2}$$

$$-2A^{-1} = \begin{bmatrix} 3 & -5 \\ 2 & -4 \end{bmatrix}$$

$$\text{Now, } A + 4A^{-1} = \begin{bmatrix} -4 & 5 \\ -2 & 3 \end{bmatrix} - 2(-2A^{-1})$$

$$\Rightarrow A + 4A^{-1} = \begin{bmatrix} -4 & 5 \\ -2 & 3 \end{bmatrix} - 2 \begin{bmatrix} 3 & -5 \\ 2 & -4 \end{bmatrix}$$

$$\Rightarrow A + 4A^{-1} = \begin{bmatrix} -10 & 15 \\ -6 & 11 \end{bmatrix}$$

39. (B) $\cos^2 x + \sin^2 y = 1$

On differentiating both side w.r.t. 'x'

$$\Rightarrow 2\cos x \cdot (-\sin x) + 2\sin y \cdot \cos y \frac{dy}{dx} = 0$$

$$\Rightarrow 2\sin y \cdot \cos y \frac{dy}{dx} = 2\sin x \cdot \cos x$$

$$\Rightarrow \sin 2y \frac{dy}{dx} = \sin 2x \Rightarrow \frac{dy}{dx} = \frac{\sin 2x}{\sin 2y}$$

40. (A) $y = 3e^{2x} + 2e^{3x}$... (i)

On differentiating both side w.r.t 'x'

$$\frac{dy}{dx} = 6e^{2x} + 6e^{3x}$$
 ... (ii)

Again, differentiating

$$\frac{d^2y}{dx^2} = 6 \times 2e^{2x} + 6 \times 3e^{3x}$$

$$\frac{d^2y}{dx^2} = 12e^{2x} + 18e^{3x}$$
 ... (iii)

$$\text{Now, } \frac{d^2y}{dx^2} - 5 \frac{dy}{dx} = 12e^{2x} + 18e^{3x} - 5(6e^{2x} + 6e^{3x})$$

$$\Rightarrow \frac{d^2y}{dx^2} - 5 \frac{dy}{dx} = 12e^{2x} + 18e^{3x} - 30e^{2x} - 30e^{3x}$$

$$\Rightarrow \frac{d^2y}{dx^2} - 5 \frac{dy}{dx} = -18e^{2x} - 12e^{3x}$$

$$\Rightarrow \frac{d^2y}{dx^2} - 5 \frac{dy}{dx} = -6(3e^{2x} + 2e^{3x})$$

$$\Rightarrow \frac{d^2y}{dx^2} - 5 \frac{dy}{dx} = -6y \quad [\text{from eq.(i)}]$$

41. (D) $y = \sqrt{e^{\sqrt{x}}}$

On differentiating both side w.r.t. 'x'

$$\frac{dy}{dx} = \frac{1}{2} (e^{\sqrt{x}})^{-1/2} \times e^{\sqrt{x}} \times \frac{1}{2} (x)^{-1/2}$$

$$\frac{dy}{dx} = \frac{1}{4} \times \frac{e^{\sqrt{x}}}{\sqrt{x} \cdot \sqrt{e^{\sqrt{x}}}}$$

and $z = e^x$

$$\frac{dz}{dx} = e^x$$

$$\text{Now, } \frac{dy}{dz} = \frac{dy}{dx} \times \frac{dx}{dz}$$

$$\Rightarrow \frac{dy}{dz} = \frac{1}{4} \times \frac{e^{\sqrt{x}}}{\sqrt{x} \cdot \sqrt{e^{\sqrt{x}}}} \times \frac{1}{e^x}$$

$$\Rightarrow \frac{dy}{dz} = \frac{\sqrt{e^{\sqrt{x}}}}{4\sqrt{x} \cdot e^x}$$

42. (B) $I = \int \frac{3 - 2\sin x}{\cos^2 x} dx$

$$I = \int (3\sec^2 x - 2\sec x \cdot \tan x) dx$$

$$I = 3\tan x - 2\sec x + c$$

43. (A) Equation $ax^2 + bx + c = 0$

$$\alpha + \beta = \frac{-b}{a} \quad \text{and} \quad \alpha\beta = \frac{c}{a}$$

$$\text{Now, } \alpha^2\beta + \alpha\beta^2 = \alpha\beta(\alpha + \beta)$$

$$= \frac{c}{a} \left(\frac{-b}{a} \right) = \frac{-bc}{a^2}$$

$$\text{and } \alpha^2\beta \cdot \alpha\beta^2 = (\alpha\beta)^3 = \left(\frac{c}{a} \right)^3 = \frac{c^3}{a^3}$$

The required equation

$$x^2 - (\alpha^2\beta + \alpha\beta^2)x + \alpha^2\beta \cdot \alpha\beta^2 = 0$$

$$\Rightarrow x^2 + \frac{bc}{a^2}x + \frac{c^3}{a^3} = 0$$

$$\Rightarrow a^3 + abcx + c^3 = 0$$

44. (B) Line $\frac{x-1}{3} = \frac{y+2}{-4} = \frac{z-1}{5}$

Direction cosines =

$$\left\langle \frac{3}{\sqrt{3^2+(-4)^2+5^2}}, \frac{-4}{\sqrt{3^2+(-4)^2+5^2}}, \frac{5}{\sqrt{3^2+(-4)^2+5^2}} \right\rangle$$

$$= \left\langle \frac{3}{5\sqrt{2}}, \frac{-4}{5\sqrt{2}}, \frac{5}{5\sqrt{2}} \right\rangle = \left\langle \frac{3}{5\sqrt{2}}, \frac{-2\sqrt{2}}{5}, \frac{1}{\sqrt{2}} \right\rangle$$

45. (B) Differential equation

$$x \cdot \log x \frac{dy}{dx} + y = \frac{2}{x} \log x$$

$$\Rightarrow \frac{dy}{dx} + \frac{y}{x \log x} = \frac{2}{x^2}$$

here, $P = \frac{1}{x \log x}$ $Q = \frac{2}{x^2}$

$$I. F. = e^{\int P dx}$$

$$I. F. = e^{\int \frac{1}{x \log x} dx}$$

We know that $\int \frac{1}{x \log x} dx = \log(\log x) + c$

$$I. F. = e^{\log(\log x)} = \log x$$

Solution of the differential equation

$$y \times I. F. = \int Q \times I.F. dx$$

$$\Rightarrow y \times \log x = \int \frac{2}{x^2} \times \log x dx$$

Let $\log x = t \Rightarrow x = e^t \Rightarrow \frac{1}{x} dx = dt$

$$\Rightarrow y \log x = 2 \int t \cdot e^{-t} dt$$

$$\Rightarrow y \log x = 2 \left[t \int e^{-t} dt - \int \left\{ \frac{d}{dt}(t) \cdot \int e^{-t} dt \right\} dt \right]$$

$$\Rightarrow y \log x = 2 \left[-t \cdot e^{-t} - \int 1 \cdot (-e^{-t}) dt \right]$$

$$\Rightarrow y \log x = 2 \left[-t \cdot e^{-t} - e^{-t} \right] + c$$

$$\Rightarrow y \log x = 2 \left[-(\log x) \cdot \frac{1}{x} - \frac{1}{x} \right] + c$$

$$\Rightarrow y \log x = -2 \left[\frac{1 + \log x}{x} \right] + c$$

46. (C) In the expansion of $\left(2\sqrt{x} - \frac{1}{2\sqrt{x}} \right)^8$

Middle term = $\left(\frac{8}{2} + 1 \right)^{\text{th}} = 5^{\text{th}}$

$$T_5 = T_{4+1} = {}^8C_4 \left(2\sqrt{x} \right)^4 \left(\frac{-1}{2\sqrt{x}} \right)^4$$

$$= 70 \times 1 = 70$$

47. (B) $\vec{a} = 3\hat{i} - 4\hat{j} + 5\hat{k}$ and $\vec{b} = 2\hat{i} + \hat{j} - 2\hat{k}$

Projection of \vec{a} on $\vec{b} = \frac{|\vec{a} \cdot \vec{b}|}{|\vec{b}|}$

$$= \frac{|3 \times 2 - 4 \times 1 + 5 \times (-2)|}{\sqrt{2^2 + 1^2 + (-2)^2}}$$

$$= \frac{|6 - 4 - 10|}{\sqrt{9}} = \frac{8}{3}$$

48. (C) Let $y = 11^{33}$

Taking log both side

$$\log_{10} y = 33 \log_{10} 11$$

$$\log_{10} y = 33 \times 1.0414$$

$$\log_{10} y = 34.3662$$

The required number = $34 + 1 = 35$

49. (D) Plane $\vec{r} \cdot (3\hat{i} - 6\hat{j} - 2\hat{k}) = 7$

and point $(-1, 2, -4)$

The required distance

$$= \frac{|(3\hat{i} - 6\hat{j} - 2\hat{k}) \cdot (-\hat{i} + 2\hat{j} - 4\hat{k}) - 7|}{\sqrt{3^2 + (-6)^2 + (-2)^2}}$$

$$= \frac{|-3 - 12 + 8 - 7|}{\sqrt{9 + 36 + 4}}$$

$$= \frac{14}{7} = 2$$

50. (B) $4^{\frac{1}{2}} \times 4^{\frac{1}{4}} \times 4^{\frac{1}{8}} \times \dots \dots \dots \infty$

$$\Rightarrow 4^{\left(\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots \dots \dots \infty \right)}$$

$$\Rightarrow 4^{1 - \frac{1}{2}} = 4$$

51. (B) $\begin{vmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{vmatrix}$

$$\Rightarrow \cos^2 \theta + \sin^2 \theta = 1$$

52. (D) Equation of circle

$$x^2 + y^2 + 2gx + 2fy + c = 0 \quad \dots(i)$$

it passes through the points $(-1, 2)$

$$1 + 4 - 2g + 4f + c = 0$$

$$\Rightarrow -2g + 4f + c = -5 \quad \dots(ii)$$

it passes through the points $(-3, 1)$

$$9 + 1 - 6g + 2f + c = 0$$

$$\Rightarrow -6g + 2f + c = -10 \quad \dots(iii)$$

it passes through the points $(0, 4)$

$$0 + 16 + 0 + 8f + c = 0$$

$$\Rightarrow 8f + c = -16 \quad \dots(iv)$$

On solving eq(ii), (iii) and (iv)

$$g = \frac{7}{2}, f = \frac{-9}{2}, c = 20$$

from eq(i)

$$x^2 + y^2 + 2 \times \frac{7}{2}x + 2 \times \left(\frac{-9}{2} \right)y + 20 = 0$$

$$\Rightarrow x^2 + y^2 + 7x - 9y + 20 = 0$$

53. (B) $x = (\sin y)^{(\sin y)^{(\sin y)^{\dots \infty}}}$

$$x = (\sin y)^x$$

taking log both side

$$\Rightarrow \log x = x \log(\sin y)$$

On differentiating both side w.r.t. 'x'

$$\Rightarrow \frac{1}{x} = x \times \frac{\cos y}{\sin y} \frac{dy}{dx} + \log(\sin y) \cdot 1$$

$$\Rightarrow \frac{1}{x} - \log \sin y = x \cot y \frac{dy}{dx}$$

$$\Rightarrow \frac{1 - x \log \sin y}{x} = x \cot y \frac{dy}{dx}$$

$$\Rightarrow \frac{dy}{dx} = \frac{1 - x \log \sin y}{x^2 \cot y}$$

54. (C) $\tan 13 - \tan 26 - \cot 77 + \cot 64$

$$\Rightarrow \tan 13 - \tan 26 - \cot(90 - 13) + \cot(90 - 26)$$

$$\Rightarrow \tan 13 - \tan 26 - \tan 13 + \tan 26 = 0$$

55. (B) $I = \int \frac{x^4 - x - 1}{x^2 + 1} dx$

$$I = \int \left(x^2 - 1 - \frac{x}{x^2 + 1} \right) dx$$

$$I = \int (x^2 - 1) dx - \frac{1}{2} \int \frac{2x}{x^2 + 1} dx$$

$$I = \frac{x^3}{3} - x - \frac{1}{2} \log(x^2 + 1) + c$$

$$I = \frac{x^3}{3} - x - \log \sqrt{x^2 + 1} + c$$

56. (B) The required Probability = $\frac{1}{52}$

57. (C) $y dx - x dy = x^2 y dy$

$$\Rightarrow \frac{y dx - x dy}{x^2} = y dy$$

$$\Rightarrow -\frac{x dy - y dx}{x^2} = y dy$$

$$\Rightarrow -d\left(\frac{y}{x}\right) = y dy$$

On integrating

$$\Rightarrow -\int d\left(\frac{y}{x}\right) = \int y dy$$

$$\Rightarrow -\frac{y}{x} = \frac{y^2}{2} - \frac{c}{2}$$

$$\Rightarrow -\frac{2y}{x} = y^2 - c$$

$$\Rightarrow y^2 + \frac{2y}{x} = c \quad \dots\dots(i)$$

Given that $y(-1) = 3$

$$(3)^2 + \frac{2 \times 3}{-1} = c \Rightarrow c = 3$$

from eq(i)

$$y^2 + \frac{2y}{x} = 3$$

On putting $x = 1$

$$\Rightarrow y^2 + \frac{2y}{1} = 3$$

$$\Rightarrow y^2 + 2y - 3 = 0$$

$$\Rightarrow y^2 + 3y - y - 3 = 0$$

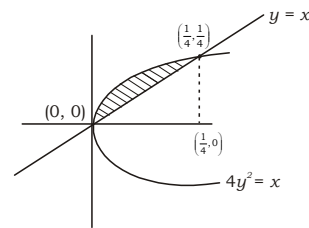
$$\Rightarrow y(y + 3) - 1(y + 3) = 0$$

$$\Rightarrow (y - 1)(y + 3) = 0$$

$$y = 1, -3$$

Hence $y(1) = 1$ or $y(1) = -3$

58. (B)



$$y_1 \Rightarrow 4y^2 = x \text{ and } y_2 \Rightarrow y = x$$

$$\text{Area} = \int_0^{1/4} (y_1 - y_2) dx$$

$$\text{Area} = \int_0^{1/4} \left(\frac{\sqrt{x}}{2} - x \right) dx$$

$$\text{Area} = \frac{1}{2} \left[\frac{x^{3/2}}{3/2} \right]_0^{1/4} - \left[\frac{x^2}{2} \right]_0^{1/4}$$

$$\text{Area} = \frac{1}{2} \times \frac{2}{3} \left[\left(\frac{1}{4} \right)^{3/2} - 0 \right] - \frac{1}{2} \left[\left(\frac{1}{4} \right)^2 - 0 \right]$$

$$\text{Area} = \frac{1}{3} \left[\frac{1}{8} \right] - \frac{1}{2} \left[\frac{1}{16} \right]$$

$$\text{Area} = \frac{1}{24} - \frac{1}{32} = \frac{1}{96} \text{ sq.unit}$$

59. (B)

class	x	f	f × x
0-20	10	60	600
20-40	30	62	1860
40-60	50	58	2900
60-80	70	64	4480
80-100	90	56	5040
		Σf = 300	14880

$$\text{Mean} = \frac{\sum f \times x}{\sum f}$$

$$\text{Mean} = \frac{14880}{300} = 49.6$$

60. (C) ${}^{37}C_{r+7} = {}^{37}C_{3r+2}$
Now, $r + 7 + 3r + 2 = 37$
 $\Rightarrow 4r + 9 = 37 \Rightarrow r = 7$

61. (B) $I = \int \log(x+2) dx$
Let $x + 2 = t \Rightarrow dx = dt$
 $I = \int \log t dt$
 $I = \log t \int 1 \cdot dt - \int \left\{ \frac{d}{dt}(\log t) \cdot \int 1 dt \right\} dt$
 $I = (\log t) \cdot t - \int \frac{1}{t} \cdot t dt$
 $I = t \log t - t + c$
 $I = (x + 2) \log(x + 2) - (x + 2) + c$
 $I = (x + 2) \log(x + 2) - x + c$

62. (C) $\sin^{-1}(0.5) = \sin^{-1}\left(\frac{1}{2}\right)$
 $\Rightarrow \sin^{-1}(0.5) = \sin^{-1}\left(\sin \frac{\pi}{6}\right) = \frac{\pi}{6}$

63. (B) $y = (1 + x^8)(1 + x^4)(1 + x^2)(1 - x^2)$
 $y = (1 + x^8)(1 + x^4)(1 - x^4)$
 $y = (1 + x^8)(1 - x^8)$
 $y = 1 - x^{16}$
On differentiating both side w.r.t. 'x'

$$\frac{dy}{dx} = 0 - 16x^{15}$$

Again, differentiating

$$\frac{d^2y}{dx^2} = -16 \times 15x^{14} = -240x^{14}$$

64. (B) $\begin{array}{|c|c|c|c|c|} \hline 7 & 7 & 6 & 5 & 4 \\ \hline \end{array} = 7 \times 7 \times 6 \times 5 \times 4 = 5880$
↓
'0' can not put here

65. (C) $f(x) = \begin{cases} x^2 - 1, & x \geq 2 \\ 5 + \lambda x, & x < 2 \end{cases}$ is continuous
at $x = 2$,

then $\lim_{x \rightarrow 2^-} f(x) = \lim_{x \rightarrow 2^+} f(x)$
 $\Rightarrow \lim_{x \rightarrow 2^-} (5 + \lambda x) = \lim_{x \rightarrow 2^+} (x^2 - 1)$
 $\Rightarrow 5 + \lambda \times 2 = 2^2 - 1$
 $\Rightarrow 5 + 2\lambda = 3 \Rightarrow \lambda = -1$

66. (D) $A' = \text{cofactor of } A$
 $|A'| = |\text{cofactor of } A|$
 $|A'| = (A)^{5-1}$ [\because order = 5]
 $|A'| = A^4$

67. (B) Equation $ax^2 + bx + c = 0$
roots = α and $\frac{1}{\alpha}$
Now, $\alpha \cdot \frac{1}{\alpha} = \frac{c}{a}$
 $\Rightarrow 1 = \frac{c}{a} \Rightarrow c = a$

68. (A) Let x and y are two persons and they hit a target with the probability A and B respectively.

$$\therefore P(A) = \frac{1}{5} \text{ and } P(B) = \frac{1}{4}$$

P (Probability of hitting the target by any one x or y)

$$\Rightarrow P(A \cap \bar{B}) + P(\bar{A} \cap B)$$

$$\Rightarrow P(A) \cdot P(\bar{B}) + P(\bar{A}) \cdot P(B)$$

$$\Rightarrow \frac{1}{5} \times \frac{3}{4} + \frac{4}{5} \times \frac{1}{4}$$

$$\Rightarrow \frac{3}{20} + \frac{4}{20} = \frac{7}{20}$$

69. (A) $x^3 - 1 = (x - 1)(x^2 + x + 1)$
 $x^3 - 1 = (x - 1)(x - \omega)(x - \omega^2)$

70. (D) In ΔABC , $\overline{AB} = 3\hat{i} + \hat{j} - \hat{k}$, $\overline{AC} = 3\hat{i} - 2\hat{j} + 5\hat{k}$

$$\text{Now, } \overline{AB} \times \overline{AC} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 1 & -1 \\ 3 & -2 & 5 \end{vmatrix}$$

$$\Rightarrow \overline{AB} \times \overline{AC} = \hat{i}(5 - 2) - \hat{j}(15 + 3) + \hat{k}(-6 - 3)$$

$$\Rightarrow \overline{AB} \times \overline{AC} = 3\hat{i} - 18\hat{j} - 9\hat{k}$$

$$\text{Area of } \Delta ABC = \frac{1}{2} |\overline{AB} \times \overline{AC}|$$

$$= \frac{1}{2} \sqrt{3^2 + (-18)^2 + (-9)^2}$$

$$= \frac{1}{2} \sqrt{9 + 324 + 81}$$

$$= \frac{1}{2} \sqrt{414}$$

$$= \frac{1}{2} \times 3 \sqrt{46} = \frac{3}{2} \sqrt{46}$$

71. (B) $3^c = \left(3 \times \frac{180}{\pi}\right)^0$

$$= \left(\frac{540 \times 7}{22}\right)^0$$

$$= \left(\frac{1890}{11}\right)^0 = 171^\circ 49' 5''$$

72. (A) We know that

$$\text{minimum value of } \left(ax^2 + \frac{b}{x^2}\right) = 2\sqrt{ab}$$

$$\begin{aligned} \text{So minimum value of } (27 \sin^2\theta + 12 \operatorname{cosec}^2\theta) &= 2\sqrt{27 \times 12} \\ &= 2\sqrt{9 \times 3 \times 3 \times 4} \\ &= 2 \times 3 \times 3 \times 2 = 36 \end{aligned}$$

73. (C) Differential equation

$$\frac{dy}{dx} + \frac{\sqrt{1-y^2}}{1-x^2} = 0$$

$$\Rightarrow \frac{dy}{dx} = -\frac{\sqrt{1-y^2}}{1-x^2}$$

$$\Rightarrow \frac{dy}{\sqrt{1-y^2}} = \frac{-dx}{\sqrt{1-x^2}}$$

On integrating

$$\Rightarrow \sin^{-1} y = \cos^{-1} x + c$$

$$\Rightarrow \sin^{-1} y - \cos^{-1} x = c$$

74. (C) $\frac{1 + \cos \theta}{1 - \cos \theta} = 3$

$$\Rightarrow 1 + \cos \theta = 3 - 3 \cos \theta$$

$$\Rightarrow 4 \cos \theta = 2$$

$$\Rightarrow \cos \theta = \frac{1}{2}$$

$$\Rightarrow \cos \theta = \cos \frac{\pi}{3}$$

$$\Rightarrow \theta = 2n\pi \pm \frac{\pi}{3}$$

75. (D) $\int_0^{\pi} |\cos x| dx = 2 \int_0^{\pi/2} \cos x dx$

$$= 2 [\sin x]_0^{\pi/2}$$

$$= 2 \left[\sin \frac{\pi}{2} - \sin 0 \right]$$

$$= 2 [1 - 0] = 2$$

76. (D) $\begin{vmatrix} 6i & 2i & 3 \\ 4 & -2i & -i \\ 5 & -6 & -2 \end{vmatrix} = x + iy$

$$\Rightarrow 6i(4i-6i) - 2i(-8+5i) + 3(-24+10i) = x + iy$$

$$\Rightarrow 6i(-2i) + 16i - 10i^2 - 72 + 30i = x + iy$$

$$\Rightarrow -12i^2 + 46i + 10 - 72 = x + iy$$

$$\Rightarrow 12 + 46i - 62 = x + iy$$

$$\Rightarrow -50 + 46i = x + iy$$

On comparing

$$x = -50 \text{ and } y = 46$$

77. (A) A.T.Q.

$$m[a + (m-1)d] = n[a + (n-1)d]$$

$$\Rightarrow am + (m^2-m)d = an + (n^2-n)d$$

$$\Rightarrow a(m-n) = d(n^2-n-m^2+m)$$

$$\Rightarrow a(m-n) = (m-n)(1-m-n)$$

$$\Rightarrow a(m-n) - d(m-n)(1-m-n) = 0$$

$$\Rightarrow (m-n)[a + (m+n-1)d] = 0$$

$$m-n \neq 0, a + (m+n-1)d = 0$$

Hence $(m+n)^{\text{th}}$ term = 0

78. (B) $\begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$ is an elementary matrix

Because its value = 1

79. (C) $(1 - \cos A + \sin A)^2 = 1 + \cos^2 A + \sin^2 A - 2 \cos A - 2 \sin A \cos A + 2 \sin A$

$$\Rightarrow (1 - \cos A + \sin A)^2 = 2 - 2 \cos A - 2 \sin A \cos A + 2 \sin A$$

$$\Rightarrow (1 - \cos A + \sin A)^2 = 2(1 - \cos A) + 2 \sin A (1 - \cos A)$$

$$\Rightarrow (1 - \cos A + \sin A)^2 = 2(1 - \cos A)(1 + \sin A)$$

80. (D) $\frac{\theta^\circ}{\theta^c} = \frac{180}{\pi} \dots(i)$

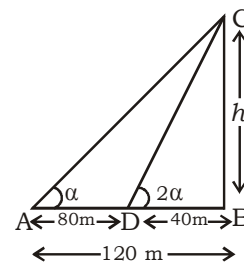
and $\theta^\circ \times \theta^c = \frac{80\pi}{9} \dots(ii)$

From eq(i) and (ii)

$$\frac{\theta^\circ}{\theta^c} \times \theta^\circ \times \theta^c = \frac{180}{\pi} \times \frac{80\pi}{9}$$

$$(\theta^\circ)^2 = 1600 \Rightarrow \theta^\circ = 40^\circ$$

81. (C)



Let $\angle BAC = \alpha$, $BC = h$ m

then $\angle BDC = 2\alpha$

In $\triangle ABC$

$$\tan \alpha = \frac{BC}{AB}$$

$$\Rightarrow \tan \alpha = \frac{h}{120} \dots(i)$$

In $\triangle BDC$

$$\tan 2\alpha = \frac{BC}{BD}$$



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$$\Rightarrow \frac{2 \tan \alpha}{1 - \tan^2 \alpha} = \frac{h}{40}$$

$$\Rightarrow \frac{2 \times \frac{h}{120}}{1 - \frac{h^2}{14400}} = \frac{h}{40}$$

$$\Rightarrow \frac{2 \times 120}{14400 - h^2} = \frac{1}{40}$$

$$\Rightarrow 14000 - h^2 = 9600$$

$$\Rightarrow h^2 = 4800 \Rightarrow h = 40\sqrt{3}$$

Height of the tower = BC = $40\sqrt{3}$ m

82. (B) Given that

$$\int x^3 \ln x \, dx = \frac{x^4}{a} \ln x + \frac{x^4}{b} + c \quad \dots(i)$$

$$\text{Let } I = \int x^3 \ln x \, dx$$

$$I = \ln x \cdot \int x^3 \, dx - \int \left\{ \frac{d}{dx}(\ln x) \int x^3 \, dx \right\} dx$$

$$I = (\ln x) \cdot \frac{x^4}{4} - \int \frac{1}{x} \times \frac{x^4}{4} \, dx$$

$$I = \frac{x^4}{4} \ln x - \frac{1}{4} \times \frac{1}{4} x^4 + c$$

$$I = \frac{x^4}{4} \ln x + \frac{x^4}{(-16)} + c$$

On comparing with eq(i)

$$a = 4 \text{ and } b = -16$$

83. (D) Given that $f(x) = \frac{2x}{1-x}$

$$\text{then } f(f(x)) = f\left[\frac{2x}{1-x}\right]$$

$$\Rightarrow f(f(x)) = \frac{2\left(\frac{2x}{1-x}\right)}{1 - \frac{2x}{1-x}}$$

$$\Rightarrow f(f(x)) = \frac{4x}{1-x-2x} = \frac{4x}{1-3x}$$

84. (D) $\tan^{-1}\left(\tan \frac{5\pi}{6}\right)$

$$\Rightarrow \tan^{-1}\left[\tan\left(\pi - \frac{\pi}{6}\right)\right]$$

$$\Rightarrow \tan^{-1}\left[-\tan\left(\frac{\pi}{6}\right)\right]$$

$$\Rightarrow \tan^{-1}\left[\tan\left(\frac{-\pi}{6}\right)\right] = \frac{-\pi}{6}$$

85. (C) We know that

$$C_0 + C_1x + C_2x^2 + \dots + C_nx^n = (1+x)^n$$

On putting $x = 1$

$$\Rightarrow C_0 + C_1 + C_2 + \dots + C_n = (1+1)^n = 2^n$$

86. (B) $f(x) = \frac{\sqrt{\log_e(3x^2 - 5x + 1)}}{x^2 + 4x - 12}$

Now, $\log_e(3x^2 - 5x + 1) \geq 0$

$$\Rightarrow 3x^2 - 5x + 1 \geq 1$$

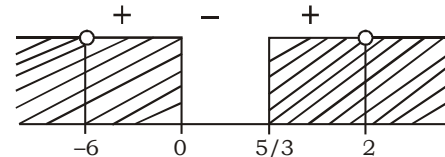
$$\Rightarrow 3x^2 - 5x \geq 0$$

$$\Rightarrow x \leq 0, x \geq \frac{5}{3}$$

and, $x^2 + 4x - 12 \neq 0$

$$\Rightarrow (x+6)(x-2) \neq 0$$

$$\Rightarrow x \neq -6, 2$$



$$\text{Domain} = \left[(-\infty, 0] \cup \left[\frac{5}{3}, \infty\right)\right] - \{-6, 2\}$$

87. (A) $I = \int e^x \sin x \, dx \quad \dots(i)$

$$I = \sin x \cdot \int e^x \, dx - \int \left\{ \frac{d}{dx}(\sin x) \cdot \int e^x \, dx \right\} dx$$

$$I = (\sin x) \cdot e^x - \int \cos x \cdot e^x \, dx$$

$$I = e^x \cdot \sin x - \left[\cos x \cdot \int e^x \, dx - \int \left\{ \frac{d}{dx}(\cos x) \cdot \int e^x \, dx \right\} dx \right]$$

$$I = e^x \cdot \sin x - \left[\cos x \cdot e^x - \int (-\sin x) \cdot e^x \, dx \right] + 2c$$

$$I = e^x \cdot \sin x - \cos x \cdot e^x - \int \sin x \cdot e^x \, dx + 2c$$

$$I = e^x \cdot \sin x - \cos x \cdot e^x - I + 2c \text{ [from eq(i)]}$$

$$2I = e^x (\sin x - \cos x) + 2c$$

$$I = \frac{(\sin x - \cos x) e^x}{2} + c$$

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88. (B) $y = \operatorname{cosec}(\cot^{-1}x)$... (i)
On differentiating both side w.r.t. 'x'
$$\Rightarrow \frac{dy}{dx} = -\operatorname{cosec}(\cot^{-1}x) \cdot \cot(\cot^{-1}x) \left(\frac{-1}{1+x^2} \right)$$

$$\Rightarrow \frac{dy}{dx} = \frac{y \cdot x}{1+x^2} \quad [\text{from eq i)]}$$

$$\Rightarrow (1+x^2) \frac{dy}{dx} = xy$$

89. (A) $x = a \sin\theta \cdot \cos\theta$
On differentiating both side w.r.t. 'θ'
$$\frac{dx}{d\theta} = a \sin\theta \cdot (-\sin\theta) + a \cos\theta \cdot \cos\theta$$

$$\frac{dx}{d\theta} = a(\cos^2\theta - \sin^2\theta)$$

$$\frac{dx}{d\theta} = a \cos 2\theta$$

and $y = a\theta \cdot \cos\theta$
On differentiating both side w.r.t. 'θ'

$$\frac{dy}{d\theta} = a\theta \cdot (-\sin\theta) + a \cos\theta \cdot 1$$

$$\frac{dy}{d\theta} = a(\cos\theta - \theta \sin\theta)$$

Now, $\frac{dy}{dx} = \frac{dy}{d\theta} \times \frac{d\theta}{dx}$

$$\Rightarrow \frac{dy}{dx} = a(\cos\theta - \theta \sin\theta) \times \frac{1}{a \cos 2\theta}$$

$$\Rightarrow \frac{dy}{dx} = \frac{\cos\theta - \theta \sin\theta}{\cos 2\theta}$$

90. (C) Equation $x^2 - 5x + 14 = 0$
Now, $B^2 - 4AC = (-5)^2 - 4 \times 1 \times 14$
 $\Rightarrow B^2 - 4AC = 25 - 56$
 $\Rightarrow B^2 - 4AC = -31 < 0$
Hence roots are imaginary.

91. (C)
$$\begin{vmatrix} 1/x & yz & x^2 \\ 1/y & xz & y^2 \\ 1/z & xy & z^2 \end{vmatrix}$$

$$\Rightarrow \frac{xyz}{xyz} \begin{vmatrix} 1/x & yz & x^2 \\ 1/y & xz & y^2 \\ 1/z & xy & z^2 \end{vmatrix}$$

$$\Rightarrow \frac{1}{xyz} \begin{vmatrix} 1 & xyz & x^3 \\ 1 & xyz & y^3 \\ 1 & xyz & z^3 \end{vmatrix}$$

$$\Rightarrow \frac{xyz}{xyz} \begin{vmatrix} 1 & 1 & x^3 \\ 1 & 1 & y^3 \\ 1 & 1 & z^3 \end{vmatrix}$$

$$= 0 \quad [\because \text{Two columns are identical.}]$$

92. (C) $u^2 + v^2 + w^2 > d$
93. (D) $\sec\theta + \tan\theta = 4$... (i)

$$\sec\theta - \tan\theta = \frac{1}{4}$$

... (ii)

From eq(i) and eq(ii)

$$2 \tan\theta = 4 - \frac{1}{4}$$

$$\Rightarrow 2 \tan\theta = \frac{15}{4} \Rightarrow \tan\theta = \frac{15}{8}$$

94. (B) Given that $\sin\theta = \cos^2\theta$... (i)

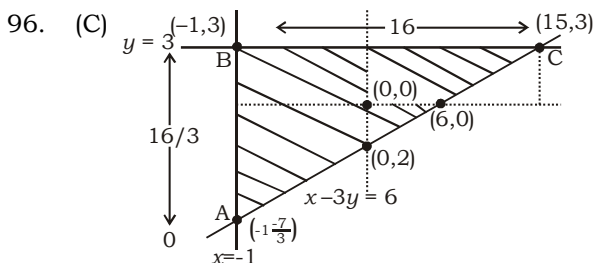
$$\Rightarrow \sin\theta = 1 - \sin^2\theta$$

$$\Rightarrow \sin\theta + \sin^2\theta = 1$$

$$\Rightarrow \sin\theta (1 + \sin\theta) = 1$$

$$\Rightarrow \cos^2\theta (1 + \cos^2\theta) = 1 \quad [\text{from eq(i)}]$$

95. (B)



$$\text{Area of } \Delta ABC = \frac{1}{2} \times AB \times BC$$

$$\text{Area of } \Delta ABC = \frac{1}{2} \times \frac{16}{3} \times 16 = \frac{128}{3} \text{ sq. unit}$$

97. (C) $y = 1 + \left(\frac{x}{3}\right) + \left(\frac{x}{3}\right)^2 + \left(\frac{x}{3}\right)^3 + \dots$

$$\Rightarrow y = \frac{1}{1 - \frac{x}{3}}$$

$$\Rightarrow 1 - \frac{x}{3} = \frac{1}{y}$$

$$\Rightarrow \frac{x}{3} = 1 - \frac{1}{y} \Rightarrow x = 3 \left(1 - \frac{1}{y} \right)$$

98. (B) $P(26, 18) = k \cdot C(26, 8)$

$$\Rightarrow \frac{26!}{(26-18)!} = k \cdot \frac{26!}{8!(26-8)!}$$

$$\Rightarrow \frac{1}{8!} = k \times \frac{1}{8! \times 18!} \Rightarrow k = 18!$$

99. (B) A.T.Q.

$$2a = 3 \times 2b$$

$$\Rightarrow a = 3b$$

$$\text{Now, } b^2 = a^2 (1 - e^2)$$

$$\Rightarrow b^2 = 9b^2 (1 - e^2)$$

$$\Rightarrow \frac{1}{9} = 1 - e^2$$

$$\Rightarrow e^2 = \frac{8}{9} \Rightarrow e = \frac{2\sqrt{2}}{3}$$

100. (A) Class size = 14 - 11.5 = 2.5

101. (B) $\lim_{n \rightarrow \infty} \frac{1^2 + 2^2 + 3^2 + \dots + n^2}{1^3 + 2^3 + 3^3 + \dots + n^3}$

$$\Rightarrow \lim_{n \rightarrow \infty} \frac{\frac{n}{6}(n+1)(2n+1)}{\frac{n^2(n+1)^2}{4}}$$

$$\Rightarrow \lim_{n \rightarrow \infty} \frac{2(2n+1)}{3n(n+1)}$$

$$\Rightarrow \lim_{n \rightarrow \infty} \frac{2 \times n \left(2 + \frac{1}{n}\right)}{3n^2 \left(1 + \frac{1}{n}\right)}$$

$$\Rightarrow \lim_{n \rightarrow \infty} \frac{2 \left(2 + \frac{1}{n}\right)}{3n \left(1 + \frac{1}{n}\right)} = \frac{1}{\infty} = 0$$

102. (C) Differential equation

$$\sin\left(\frac{dy}{dx}\right) = x$$

$$\Rightarrow \frac{dy}{dx} = \sin^{-1}x$$

$$\Rightarrow dy = \sin^{-1}x \, dx$$

On integrating

$$\Rightarrow \int dy = \int \sin^{-1}x \, dx$$

$$y = \sin^{-1}x \cdot \int 1 \, dx - \int \left\{ \frac{d}{dx}(\sin^{-1}x) \cdot \int 1 \, dx \right\} dx$$

$$y = (\sin^{-1}x) \cdot x - \int \frac{1}{\sqrt{1-x^2}} \times x \, dx$$

$$y = x \cdot \sin^{-1}x + \frac{1}{2} \int \frac{-2x}{\sqrt{1-x^2}} \, dx$$

$$y = x \cdot \sin^{-1}x + \frac{1}{2} \times \frac{(1-x^2)^{-\frac{1}{2}+1}}{-\frac{1}{2}+1} + c$$

$$y = x \cdot \sin^{-1}x + \sqrt{1-x^2} + c$$

103. (D) Given that $|\vec{a}| = 3$, $|\vec{b}| = 5$

$$\text{and } (\vec{a} \times \vec{b}) = 12$$

$$\Rightarrow |\vec{a}| |\vec{b}| \sin\theta = 12$$

$$\Rightarrow 3 \times 5 \sin\theta = 12$$

$$\Rightarrow \sin\theta = \frac{4}{5} \Rightarrow \cos\theta = \frac{3}{5}$$

$$\text{Now, } \vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos\theta$$

$$\Rightarrow \vec{a} \cdot \vec{b} = 3 \times 5 \times \frac{3}{5} = 9$$

104. (B) Given that $\vec{a} = -\hat{i} - 2\hat{j} - \hat{k}$, $\vec{b} = -\hat{i} + \hat{j} + 2\hat{k}$

From option (B)

$$\text{Let } \vec{c} = -\hat{i} + \hat{j} - \hat{k}$$

$$\vec{a} \cdot \vec{c} = -1 \times (-1) - 2 \times 1 - 1 \times (-1)$$

$$\vec{a} \cdot \vec{c} = 1 - 2 + 1 = 0$$

$$\text{and } \vec{b} \cdot \vec{c} = -1 \times (-1) + 1 \times 1 + 2 \times (-1)$$

$$\vec{b} \cdot \vec{c} = 1 + 1 - 2 = 0$$

Hence vector $-\hat{i} + \hat{j} - \hat{k}$ perpendicular to the given vectors.

105. (D) $\tan^{-1}\left(\frac{b}{a}\right) + \cot^{-1}\left(\frac{a+b}{a-b}\right)$

$$\Rightarrow \tan^{-1}\left(\frac{b}{a}\right) + \tan^{-1}\left(\frac{a-b}{a+b}\right)$$

$$\Rightarrow \tan^{-1}\left[\frac{\frac{b}{a} + \frac{a-b}{a+b}}{1 - \frac{b}{a} \times \frac{a-b}{a+b}}\right]$$

$$\Rightarrow \tan^{-1}\left[\frac{ab + b^2 + a^2 - ab}{a^2 + ab - ab + b^2}\right]$$

$$\Rightarrow \tan^{-1}\left[\frac{a^2 + b^2}{a^2 + b^2}\right]$$

$$\Rightarrow \tan^{-1}1 = \frac{\pi}{4}$$

106. (B) $\cos\left(\tan^{-1}\left(\tan\left(\sin^{-1}\left(-\frac{1}{2}\right)\right)\right)\right)$

$$\Rightarrow \cos\left(\tan^{-1}\left(\tan\left(\sin^{-1}\left(\sin\left(-\frac{\pi}{6}\right)\right)\right)\right)\right)$$

$$\Rightarrow \cos\left(\tan^{-1}\left(\tan\left(-\frac{\pi}{6}\right)\right)\right)$$

$$\Rightarrow \cos\left(-\frac{\pi}{6}\right)$$

$$\Rightarrow \cos \frac{\pi}{6} = \frac{\sqrt{3}}{2}$$

107. (C) 0.7
 $\frac{\times 2}{1.4}$
 $\frac{\times 2}{0.8}$
 $\frac{\times 2}{1.6}$
 $\frac{\times 2}{1.2}$
 $\frac{\times 2}{0.4}$
 $\frac{\times 2}{0.8}$
 $\frac{\times 2}{1.6}$

Hence $(0.7)_{10} = (0.1011001\dots)_2$

108. (B) (p, q) is the point on the y -axis, i.e.
 $p = 0$
 A.T.Q.

$$\sqrt{(p+1)^2 + (q-3)^2} = \sqrt{(p+3)^2 + (q-2)^2}$$

$$\Rightarrow \sqrt{(0+1)^2 + q^2 + 9 - 6q} = \sqrt{(0+3)^2 + q^2 + 4 - 4q}$$

$$\Rightarrow 1 + q^2 + 9 - 6q = 9 + q^2 + 4 - 4q$$

$$\Rightarrow 10 - 13 = 6q - 4q$$

$$\Rightarrow -3 = 2q \Rightarrow q = -\frac{3}{2}$$

Hence $p = 0, q = -\frac{3}{2}$

109. (B) $C(n, r+1) + 2C(n, r) + C(n, r-1)$

$$\Rightarrow {}^nC_{r+1} + {}^nC_r + {}^nC_r + {}^nC_{r-1}$$

$$\Rightarrow \frac{n!}{(r+1)!(n-r-1)!} + \frac{n!}{r!(n-r)!} + \frac{n!}{r!(n-r)!}$$

$$+ \frac{n!}{(r-1)!(n-r+1)!}$$

$$\Rightarrow \frac{n!}{(r+1)r!(n-r-1)!} + \frac{n!}{r!(n-r)(n-r-1)!}$$

$$+ \frac{n!}{r(r-1)!(n-r)!} + \frac{n!}{(r-1)!(n-r+1)(n-r)!}$$

$$\Rightarrow \frac{n!}{r!(n-r-1)!} \left[\frac{1}{r+1} + \frac{1}{n-r} \right]$$

$$+ \frac{n!}{(r-1)!(n-r)!} \left[\frac{1}{r} + \frac{1}{n-r+1} \right]$$

$$\Rightarrow \frac{n!}{r!(n-r-1)!} \times \frac{n-r+r+1}{(r+1)(n-r)}$$

$$+ \frac{n!}{(r-1)!(n-r)!} \times \frac{n-r+1+r}{r(n-r+1)}$$

$$\Rightarrow \frac{n!(n+1)}{r!(n-r-1)!(r+1)(n-r)}$$

$$+ \frac{n!(n+1)}{r(r-1)!(n-r)!(n-r+1)}$$

$$\Rightarrow \frac{(n+1)!}{(r+1)r!(n-r)!} + \frac{(n+1)!}{r!(n-r+1)(n-r)!}$$

$$\Rightarrow \frac{(n+1)!}{r!(n-r)!} \left[\frac{1}{r+1} + \frac{1}{n-r+1} \right]$$

$$\Rightarrow \frac{(n+1)!}{r!(n-r)!} \times \frac{n-r+1+r+1}{(r+1)(n-r+1)}$$

$$\Rightarrow \frac{(n+1)!(n+2)}{(r+1)!(n-r+1)!}$$

$$\Rightarrow \frac{(n+2)!}{(r+1)!(n-r+1)!} = {}^{n+2}C_{r+1} = C(n+2, r+1)$$

110. (D) Given that $a = 3, b = 2$ and $\sin B = 2/3$
 Sine Rule

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Now, $\frac{\sin A}{a} = \frac{\sin B}{b}$

$$\Rightarrow \frac{\sin A}{3} = \frac{2/3}{2}$$

$$\Rightarrow \sin A = 1$$

$$\Rightarrow \sin A = \sin \frac{\pi}{2} \Rightarrow A = \frac{\pi}{2}$$

111. (D) Given that $2\vec{a} + \vec{b} - 5\vec{c} = \vec{0}$

$$\Rightarrow \vec{b} = 5\vec{c} - 2\vec{a}$$

Now, $\vec{a} \times \vec{b} + \vec{b} \times \vec{c} + \vec{c} \times \vec{a} = \lambda (\vec{a} \times \vec{c})$

$$\Rightarrow \vec{a} \times (5\vec{c} - 2\vec{a}) + (5\vec{c} - 2\vec{a}) \times \vec{c} - \vec{a} \times \vec{c}$$

$$= \lambda (\vec{a} \times \vec{c})$$

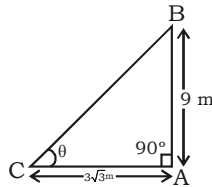
$$\Rightarrow 5\vec{a} \times \vec{c} - 0 + 0 - 2\vec{a} \times \vec{c} - \vec{a} \times \vec{c} = \lambda (\vec{a} \times \vec{c})$$

$$\Rightarrow 2(\vec{a} \times \vec{c}) = \lambda (\vec{a} \times \vec{c})$$

On comparing

$$\lambda = 2$$

112. (B)



Let $\angle ACB = \theta$

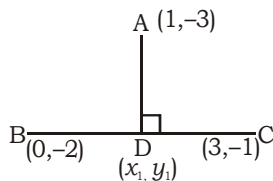
In $\triangle ABC$

$$\tan \theta = \frac{AB}{AC}$$

$$\Rightarrow \tan \theta = \frac{9}{3\sqrt{3}}$$

$$\Rightarrow \tan \theta = \sqrt{3} \Rightarrow \theta = \frac{\pi}{3}$$

113. (A)



Let $D = (x_1, y_1)$

$$\text{Slope of BC}(m_1) = \frac{-1+2}{3-0} = \frac{1}{3}$$

$$\text{Slope of AD}(m_2) = \frac{y_1+3}{x_1-1}$$

$$\text{Slope of DC} = \frac{-1-y_1}{3-x_1}$$

A.T.Q.

$$m_1 \cdot m_2 = -1$$

$$\Rightarrow \frac{1}{3} \times \frac{y_1+3}{x_1-1} = -1$$

$$\Rightarrow y_1 + 3 = -3x_1 + 3$$

$$\Rightarrow 3x_1 + y_1 = 0 \quad \dots(i)$$

$$\text{and } \frac{-1-y_1}{3-x_1} = \frac{1}{3}$$

$$\Rightarrow -3 - 3y_1 = 3 - x_1$$

$$\Rightarrow x_1 - 3y_1 = 6$$

...(ii)

From eq(i) and eq(ii)

$$x_1 = \frac{3}{5} \text{ and } y_1 = \frac{-9}{5}$$

Hence co-ordinate of $D = \left(\frac{3}{5}, \frac{-9}{5}\right)$

114. (B) Let $y = 8 \sin \theta + 6 \sin^2 \theta$

$$y = 6 \left(\sin^2 \theta + \frac{4}{3} \sin \theta \right)$$

$$y = 6 \left(\sin^2 \theta + 2 \times \frac{2}{3} \sin \theta + \left(\frac{2}{3}\right)^2 - \left(\frac{2}{3}\right)^2 \right)$$

$$y = 6 \left(\sin \theta + \frac{2}{3} \right)^2 - 6 \times \frac{4}{9}$$

$$y = 6 \left(\sin \theta + \frac{2}{3} \right)^2 - \frac{8}{3}$$

For maximum value $\sin \theta = 1$

$$\text{Maximum value of } y = 6 \left(1 + \frac{2}{3} \right)^2 - \frac{8}{3}$$

$$= 6 \times \left(\frac{5}{3} \right)^2 - \frac{8}{3} = 6 \times \frac{25}{9} - \frac{8}{3} = \frac{42}{3}$$

115. (B) $\lim_{x \rightarrow 0} \frac{5^x - 6^x}{\sin x} \quad \left[\frac{0}{0} \right] \text{ form}$

by L-Hospital's Rule

$$\Rightarrow \lim_{x \rightarrow 0} \frac{5^x \ln 5 - 6^x \ln 6}{\cos x}$$

$$\Rightarrow \frac{5^0 \ln 5 - 6^0 \ln 6}{\cos 0}$$

$$\Rightarrow \ln 5 - \ln 6 \Rightarrow \ln \left(\frac{5}{6} \right)$$

116. (C) Differential equation

$$\left(\frac{dy}{dx} \right)^{3/2} + \left(\frac{d^2y}{dx^2} \right)^{1/3} = y^2$$

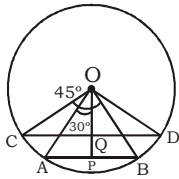
$$\Rightarrow \left(\frac{dy}{dx} \right)^{3/2} - y^2 = \left(\frac{d^2y}{dx^2} \right)^{1/3}$$

$$\Rightarrow \left[\left(\frac{dy}{dx} \right)^{2/3} - y^2 \right]^6 = \left[\left(\frac{d^2y}{dx^2} \right)^{1/3} \right]^6$$

$$\Rightarrow \left[\left(\frac{dy}{dx} \right)^{3/2} - y^2 \right]^6 = \left(\frac{d^2y}{dx^2} \right)^2$$

Order = 2, Degree = 2

117. (B)



Given that
radius of circle = $OA = OC = 30$ cm
 $\angle AOB = 60^\circ$ and $\angle COD = 90^\circ$
then $\angle AOP = 30^\circ$ and $\angle COQ = 45^\circ$

In $\triangle COQ$

$$\cos 45^\circ = \frac{OQ}{OC}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{OQ}{30} \Rightarrow OQ = \frac{30}{\sqrt{2}}$$

In $\triangle AOP$

$$\cos 30^\circ = \frac{PO}{OA}$$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{PO}{30} \Rightarrow PO = 15\sqrt{3}$$

Now, $PQ = PO - OQ$

$$\Rightarrow PQ = 15\sqrt{3} - \frac{30}{\sqrt{2}}$$

$$\Rightarrow PQ = \frac{15\sqrt{6} - 30}{\sqrt{2}}$$

$$\Rightarrow PQ = \frac{15}{\sqrt{2}} (\sqrt{6} - 2) \text{ cm}$$

$$\text{The required distance} = \frac{15}{\sqrt{2}} (\sqrt{6} - 2) \text{ cm}$$

118. (B) Given that $x = a(y + z)$, $y = b(z + x)$,
 $z = c(x + y)$

Now, $x = a(y + z)$

$$\Rightarrow a = \frac{x}{y + z}$$

$$\Rightarrow a + 1 = \frac{x + y + z}{y + z}$$

$$\text{Similarly } b + 1 = \frac{x + y + z}{x + z}, c + 1 = \frac{x + y + z}{x + y}$$

$$\text{Now, } \frac{1}{1+a} + \frac{1}{1+b} + \frac{1}{1+c}$$

$$\Rightarrow \frac{y+z}{x+y+z} + \frac{x+z}{x+y+z} + \frac{x+y}{x+y+z}$$

$$\Rightarrow \frac{2(x+y+z)}{x+y+z} = 2$$

119. (C) In $\triangle ABC$, $A(-1, 2)$, $B(-2, 5)$, $C(-4, 6)$

$$\text{centroid} = \left(\frac{-1-2-4}{3}, \frac{2+5+6}{3} \right)$$

$$= \left(\frac{-7}{3}, \frac{13}{3} \right)$$

120. (B) $y = \log_a x + \log_x a + \log_x x + \log_a a$

$$y = \frac{\log_e x}{\log_e a} + \frac{\log_e a}{\log_e x} + 1 + 1$$

On differentiating both side w.r.t. 'x'

$$\frac{dy}{dx} = \frac{1}{\log_e a} \times \frac{1}{x} + \log_e a \left[\frac{-1}{(\log_e x)^2} \right] \times \frac{1}{x}$$

$$\frac{dy}{dx} = \frac{1}{x \log_e a} - \frac{\log_e a}{x (\log_e x)^2}$$

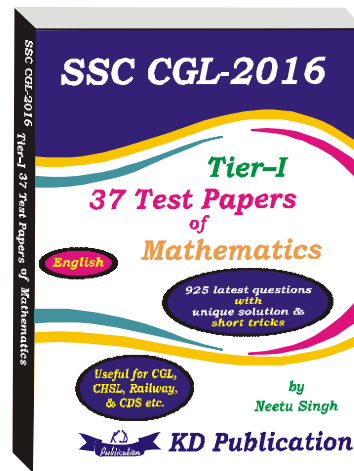
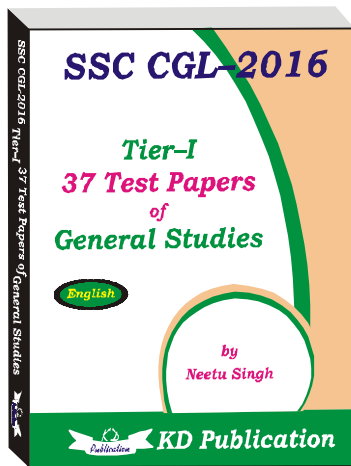


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NDA (MATHS) MOCK TEST - 148 (Answer Key)

- | | | | | | |
|---------|---------|---------|---------|----------|----------|
| 1. (B) | 21. (B) | 41. (D) | 61. (B) | 81. (C) | 101. (B) |
| 2. (A) | 22. (C) | 42. (B) | 62. (C) | 82. (B) | 102. (C) |
| 3. (D) | 23. (B) | 43. (A) | 63. (B) | 83. (D) | 103. (D) |
| 4. (C) | 24. (C) | 44. (B) | 64. (B) | 84. (D) | 104. (B) |
| 5. (A) | 25. (B) | 45. (B) | 65. (C) | 85. (C) | 105. (D) |
| 6. (B) | 26. (B) | 46. (C) | 66. (D) | 86. (B) | 106. (B) |
| 7. (C) | 27. (C) | 47. (B) | 67. (B) | 87. (A) | 107. (C) |
| 8. (C) | 28. (D) | 48. (C) | 68. (A) | 88. (B) | 108. (B) |
| 9. (A) | 29. (C) | 49. (D) | 69. (A) | 89. (A) | 109. (B) |
| 10. (D) | 30. (B) | 50. (B) | 70. (D) | 90. (C) | 110. (D) |
| 11. (C) | 31. (C) | 51. (B) | 71. (B) | 91. (C) | 111. (D) |
| 12. (B) | 32. (C) | 52. (D) | 72. (A) | 92. (C) | 112. (B) |
| 13. (A) | 33. (D) | 53. (B) | 73. (C) | 93. (D) | 113. (A) |
| 14. (B) | 34. (A) | 54. (C) | 74. (C) | 94. (B) | 114. (B) |
| 15. (C) | 35. (B) | 55. (B) | 75. (D) | 95. (B) | 115. (B) |
| 16. (B) | 36. (C) | 56. (B) | 76. (D) | 96. (C) | 116. (C) |
| 17. (B) | 37. (B) | 57. (C) | 77. (A) | 97. (C) | 117. (B) |
| 18. (B) | 38. (B) | 58. (B) | 78. (B) | 98. (B) | 118. (B) |
| 19. (C) | 39. (B) | 59. (B) | 79. (C) | 99. (B) | 119. (C) |
| 20. (B) | 40. (A) | 60. (C) | 80. (D) | 100. (A) | 120. (B) |



Note:- If your opinion differs regarding any answer, please message the mock test and question number to 8860330003

Note:- Whatsapp with Mock Test No. and Question No. at 7053606571 for any of the doubts, also share your suggestions and experience of Sunday Mock

Note:- If you face any problem regarding result or marks scored, please contact 9313111777