

NDA MATHS MOCK TEST - 74 (SOLUTION)

1. (C) Equation of the line AB

$$\frac{2x-1}{\sqrt{3}} = \frac{y+2}{2} = \frac{z-3}{3}$$

$$x - \frac{1}{2} = \frac{y+2}{2} = \frac{z-3}{3}$$

direction cosines of a line parallel to AB

$$= \left[\frac{\sqrt{3}}{2\sqrt{\left(\frac{\sqrt{3}}{2}\right)^2 + (2)^2 + (3)^2}}, \frac{2}{\sqrt{\left(\frac{\sqrt{3}}{2}\right)^2 + (2)^2 + (3)^2}}, \frac{3}{\sqrt{\left(\frac{\sqrt{3}}{2}\right)^2 + (2)^2 + (3)^2}} \right]$$

$$= \left(\frac{\sqrt{3}}{\sqrt{55}}, \frac{4}{\sqrt{55}}, \frac{6}{\sqrt{55}} \right)$$

2. (A) Given that

$$U = \{1, 2, 3, 4, 5, 6, 7\}, A = \{2, 4, 6\}$$

$$B = \{3, 5\} \text{ and } C = \{1, 2, 4, 7\}$$

$$(B \cap C) = \phi$$

$$A - (B \cap C) = \{2, 4, 6\} - \phi$$

$$= \{2, 4, 6\}$$

3. (C) Given that

$$f(x) = \frac{x^3 - x + 3}{x^2 - 1}$$

$$x^2 - 1 \neq 0$$

$$x^2 \neq 1$$

$$x \neq -1, 1$$

then domain of the function = $R - \{-1, 1\}$

4. (B) Given that

Class	x_i	f_i	$f_i \times x_i$	$d_i = x_i - A $	$f_i \times d_i$
10-20	15	2	30	30	60
20-30	25	3	75	20	60
30-40	35	8	280	10	80
40-50	45	14	630	0	0
50-60	55	8	440	10	80
60-70	65	3	195	20	60
70-80	75	2	150	30	60
	$\Sigma f_i = 40$		$\Sigma f_i \times x_i = 1800$		$\Sigma f_i \times d_i = 400$

$$A = \frac{\Sigma f_i \times x_i}{\Sigma f_i} = \frac{1800}{40} = 45$$

$$\text{Mean deviation} = \frac{\Sigma f_i \times d_i}{\Sigma f_i}$$

$$= \frac{400}{40} = 10$$

5. (A) One card is drawn from a well shuffled deck of 52 cards.

total sample space $n(S) = 52$

four ace in the deck of 52 cards

$$n(E) = 4$$

Probability that the card drawn is an ace

$$P(E) = \frac{n(E)}{n(S)} = \frac{4}{52} = \frac{1}{13}$$

then probability that the card drawn is not ace

$$P(\bar{E}) = 1 - \frac{1}{13} = \frac{12}{13}$$

6. (A) $S = \{(H, 1), (H, 2), (H, 3), (H, 4), (H, 5), (H, 6), (T, H), (T, T)\}$, $n(S) = 8$

$$E = (T, H), n(E) = 1$$

Probability of getting one tail

$$P(E) = \frac{1}{8}$$

7. (D) Let $f(x) = \frac{x}{[x]}$

$$\text{L.H.L.} = \lim_{x \rightarrow 2^-} f(x) = \lim_{h \rightarrow 0} f(2-h)$$

$$= \lim_{h \rightarrow 0} \frac{2-h}{[2-h]}$$

$$= \lim_{h \rightarrow 0} \frac{2-h}{1}$$

$$= 2$$

$$\text{R.H.L.} = \lim_{x \rightarrow 2^+} f(x) = \lim_{h \rightarrow 0} f(2+h)$$

$$= \lim_{h \rightarrow 0} \frac{2+h}{[2+h]}$$

$$= \lim_{h \rightarrow 0} \frac{2+h}{2}$$

$$= 1$$

L.H.L. \neq R.H.L.

Hence limit does not exist.

8. (D) $\lim_{x \rightarrow 0} \frac{x \cdot 5^x - x}{1 - \cos x}$ $\left(\frac{0}{0}\right)$ Form

by L-hospital's Rule

$$= \lim_{x \rightarrow 0} \frac{x \cdot 5^x \log 5 + 5^x \cdot 1 - 1}{0 + \sin x}$$

$$= \lim_{x \rightarrow 0} \frac{(\log 5)x \cdot 5^x + 5^x - 1}{\sin x} \quad \left(\frac{0}{0}\right) \text{Form}$$

again by L-Hospital's Rule

$$= \lim_{x \rightarrow 0} \frac{(\log 5)\{x \cdot 5^x \log 5 + 5^x \cdot 1\} + 5^x \cdot \log 5 - 0}{\cos x}$$

$$= \frac{(\log 5)\{0 + 5^0\} + 5^0 \cdot \log 5}{\cos 0}$$

$$= \frac{\log 5 + \log 5}{1}$$

$$= 2 \log 5$$

9. (C) Points A(1, 3, 4), B(-1, 6, 10), C(-7, 4, 7) and D(-5, 1, 1)

$$AB = \sqrt{(-2)^2 + (3)^2 + (6)^2} = \sqrt{4 + 9 + 36} = 7$$

$$BC = \sqrt{(-6)^2 + (-2)^2 + (-3)^2} = \sqrt{36 + 4 + 9} = 7$$

$$CD = \sqrt{(2)^2 + (-3)^2 + (-6)^2} = \sqrt{4 + 9 + 36} = 7$$

$$DA = \sqrt{(6)^2 + (2)^2 + (3)^2} = \sqrt{36 + 4 + 9} = 7$$

$$AB = BC = CD = DA$$

then

these points are vertices of a Rhombus.

10. (D) Differential equation

$$(1 - x^2) \frac{dy}{dx} - 2xy = 1$$

$$\frac{dy}{dx} + \left(\frac{-2x}{1-x^2}\right)y = \frac{1}{1-x^2}$$

On comparing with general equation

$$\frac{dy}{dx} + Py = Q$$

$$P = \frac{-2x}{1-x^2}, Q = \frac{1}{1-x^2}$$

$$\text{I.F.} = e^{\int P \cdot dx}$$

$$= e^{\int \frac{-2x}{1-x^2} dx}$$

$$= e^{\log(1-x^2)} = (1-x^2)$$

Solution of the differential equation

$$y \times \text{I.F.} = \int Q \times \text{I.F.} \cdot dx + c$$

$$y \times (1 - x^2) = \int \frac{1}{1-x^2} \times (1-x^2) dx + c$$

$$y \times (1 - x^2) = \int 1 \cdot dx + c$$

$$y(1 - x^2) = x + c$$

11. (B) degree = 2

12. (D) Let $a + ib = \sqrt{1 + \sqrt{3}i}$

On squaring both side

$$(a^2 - b^2) + i(2ab) = 1 + \sqrt{3}i$$

On comparing

$$a^2 - b^2 = 1 \text{ and } 2ab = \sqrt{3} \quad \dots(i)$$

$$(a^2 + b^2)^2 - 4a^2b^2 = 1$$

$$(a^2 + b^2)^2 - 3 = 1 \quad [\because 2ab = \sqrt{3}]$$

$$(a^2 + b^2)^2 = 4$$

$$a^2 + b^2 = 2 \quad \dots(ii)$$

from equation (i) and equation (ii)

$$a = \pm \sqrt{\frac{3}{2}} \text{ and } b = \pm \sqrt{\frac{1}{2}}$$

$$\text{then square root of } (1 + \sqrt{3}i) = \pm \left(\frac{\sqrt{3} + i}{\sqrt{2}}\right)$$

$$13. (B) \begin{vmatrix} a^2 & a^2 & b^2 + c^2 \\ b^2 & c^2 + a^2 & b^2 \\ a^2 + b^2 & c^2 & c^2 \end{vmatrix}$$

$$\Rightarrow a^2(c^4 + a^2c^2 - b^2c^2) - a^2(b^2c^2 - a^2c^2 - b^4) + (b^2 + c^2)(b^2c^2 - a^2c^2 - a^4 - b^2c^2 - a^2b^2)$$

On solving

$$\Rightarrow -4a^2b^2c^2$$

$$14. (B) \begin{vmatrix} \sin^2\theta & \cos^2\theta & 1 \\ -\sec^2\theta & \tan^2\theta & -1 \\ -30 & 32 & 2 \end{vmatrix}$$

$$C_3 \rightarrow C_3 - C_2$$

$$= \begin{vmatrix} \sin^2\theta & \cos^2\theta & 1 - \cos^2\theta \\ -\sec^2\theta & \tan^2\theta & -1 - \tan^2\theta \\ -30 & 32 & -30 \end{vmatrix}$$

$$= \begin{vmatrix} \sin^2\theta & \cos^2\theta & \sin^2\theta \\ -\sec^2\theta & \tan^2\theta & -\sec^2\theta \\ -30 & 32 & -30 \end{vmatrix}$$

$$= 0 \quad [\because C_1 \text{ and } C_3 \text{ are same}]$$

15. (B) $f(x) = \begin{vmatrix} \cos x & 0 & \sin x \\ 0 & 1 & 0 \\ -\sin x & 0 & \cos x \end{vmatrix}$

$$f(x) = \cos x(\cos x - 0) - 0 + \sin x(0 + \sin x)$$

$$= \cos^2 x + \sin^2 x$$

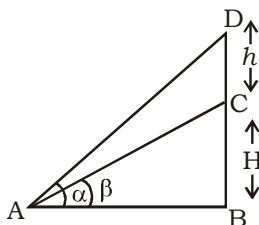
$$f(x) = 1$$

$$f(y) = 1$$

$$f(x+y) = 1$$

then $f(x+y) = f(x) \cdot f(y)$

16. (D)



Given that

Height of flag staff (CD) = h

Let height of tower (BC) = H

In $\triangle ABC$

$$\tan b = \frac{BC}{AB} = \frac{H}{AB} \quad \dots(i)$$

In $\triangle ABD$

$$\tan a = \frac{BD}{AB} = \frac{H+h}{AB} \quad \dots(ii)$$

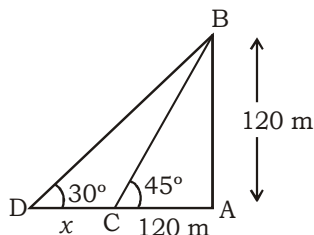
From equation (i) and (ii)

$$\frac{\tan \beta}{\tan \alpha} = \frac{H}{H+h}$$

$$H \tan b + h \tan b = H \tan a$$

$$H = \frac{h \tan \beta}{\tan \alpha - \tan \beta}$$

17. (C) Let the distance between two house = x m



In $\triangle ABC$

$$\tan 45^\circ = \frac{AB}{AC}$$

$$1 = \frac{120}{AC}$$

$$AC = 120$$

In $\triangle ABD$

$$\tan 30^\circ = \frac{AB}{AD}$$

$$\frac{1}{\sqrt{3}} = \frac{120}{x+120}$$

$$x = 120(\sqrt{3}-1)m$$

$$\text{distance between two houses} = 120(\sqrt{3}-1)m$$

18. (A) Given that $x + y = 15$

$$\text{Let } P = xy^2 \quad \dots(i)$$

$$P = x(15-x)^2$$

$$P = 225x + x^3 - 30x^2$$

differentiate both side w.r.t. 'x'

$$\frac{dP}{dx} = 225 + 3x^2 - 60x$$

again differentiate both side w.r.t. 'x'

$$\frac{d^2P}{dx^2} = 6x - 60 \quad \dots(ii)$$

For maxima and minima

$$\frac{dP}{dx} = 0$$

$$3x^2 - 60x + 225 = 0$$

$$(x-15)(x-5) = 0$$

$$x = 5, 15 \text{ and } y = 10, 0$$

on putting $x = 5$ in equation (ii)

$$\left(\frac{d^2P}{dx^2}\right)_{at x=5} = 6 \times 5 - 60 = -30 \text{ (maxima)}$$

on putting $x = 15$ in equation (ii)

$$\left(\frac{d^2P}{dx^2}\right)_{at x=15} = 15 \times 6 - 60 = 30 \text{ (minima)}$$

$$\text{minimum value of } P(\text{at } x = 15, y = 0) = 0$$

19. (B) Given that diameter of sphere = D

$$\text{radius of sphere } r = \frac{D}{2}$$

then surface area $S = 4\pi r^2$

$$S = 4\pi \times \left(\frac{D}{2}\right)^2$$

$$S = \pi D^2$$

$$\frac{dS}{dt} = \pi \times 2D \times \frac{dD}{dt} \quad \dots(i)$$

and volume $V = \frac{4}{3} \pi r^3$

$$V = \frac{4}{3} \pi \left(\frac{D}{2}\right)^3$$

$$V = \frac{\pi D^3}{6}$$

$$\frac{dV}{dt} = \frac{\pi}{6} \times 3D^2 \frac{dD}{dt} \dots \text{(ii)}$$

from equation (i) and equation (ii)

$$\frac{dV}{dt} = \frac{1}{4} D \frac{dS}{dt}$$

20. (B) $I = \int \frac{1}{(x^2 - a^2)} dx$

$$I = \int \frac{1}{(x-a)(x+a)} dx$$

$$= \frac{1}{2a} \int \left[\frac{1}{x-a} - \frac{1}{x+a} \right] dx$$

$$I = \frac{1}{2a} [\log(x-a) - \log(x+a)] + C$$

$$I = \frac{1}{2a} \log \left[\frac{x-a}{x+a} \right] + C$$

21. (D) Given that,

$$A = \{1, 2\} \text{ and } B = \{1, 3, 4\}$$

then $(A \cap B) = \{1\}$ and $(A \cup B) = \{1, 2, 3, 4\}$

$$[(A \cap B) \times (A \cup B)] = [\{1\} \times \{1, 2, 3, 4\}]$$

$$[(A \cap B) \times (A \cup B)] = [(1, 1), (1, 2), (1, 3), (1, 4)]$$

22. (A) E is universal set and $A = B \cap C$

then $E - (E - (E - A))$

$$\Rightarrow E - (E - A') \quad [\because E - A = A']$$

$$\Rightarrow E - A$$

$$\Rightarrow A'$$

$$\Rightarrow (B \cap C)' = (B' \cup C')$$

23. (A) Given that

$$g(x) = 4x + 7$$

$$\text{Let } g(x) = y$$

$$y = 4x + 7$$

$$x = \frac{y-7}{4}$$

$$g^{-1}(y) = \frac{y-7}{4}$$

$$g^{-1}(x) = \frac{x-7}{4}$$

24. (A) We know that

$$\frac{-1 + \sqrt{3}i}{2} = \omega \text{ and } \frac{-1 - \sqrt{3}i}{2} = \omega^2$$

$$\text{then } \left(\frac{1 - \sqrt{3}i}{2}\right)^{36} - \left(\frac{-1 - \sqrt{3}i}{2}\right)^{36}$$

$$= (-\omega)^{36} - (\omega^2)^{36}$$

$$= (\omega^3)^{12} - (\omega^3)^{24}$$

$$= 1 - 1$$

$$= 0$$

25. (A) Let $z = \sqrt{2}i + \sqrt{-2}i$

$$z = \sqrt{2}i + i\sqrt{2} \times i$$

$$z = \sqrt{2}(i-1)$$

$$\text{modulus of } z = |z| = |\sqrt{2}(i-1)|$$

$$= \sqrt{2} \sqrt{1+1}$$

$$|z| = 2$$

26. (C) Statement (S):-

We know that

$$\frac{-1 + \sqrt{3}i}{2} = \omega \text{ and } \frac{-1 - \sqrt{3}i}{2} = \omega^2$$

$$\text{then } \left(\frac{-1 - \sqrt{3}i}{2}\right)^{30} - \left(\frac{-1 - \sqrt{3}i}{2}\right)^{30}$$

$$\Rightarrow (\omega)^{30} - (\omega^2)^{30}$$

$$\Rightarrow 1 - 1$$

$$\Rightarrow 0$$

Statement is true.

Reason (R) is false because $\omega^3 = 1$

27. (C) $n!, 2 \times n!, (n+1)!$ are in A.P.

then $2 \times 2 \times n! = n! + (n+1)!$ [$\because 2b = a + c$]

$$4 \times n! = n! + (n+1)!$$

$$4 \times n! = n! + (n+1)n!$$

$$n = 2$$

28. (B) Let three terms of G.P.

$$a, ar, ar^2$$

according to question

$$a = \frac{1}{3}(ar + ar^2)$$

$$3 = r + r^2$$

$$r^2 + r - 3 = 0$$

$$\text{then } r = \frac{-1 \pm \sqrt{(-1)^2 - 4 \times 1 \times (-3)}}{2 \times 1}$$

$$r = \frac{-1 \pm \sqrt{13}}{2}$$

$$\text{positive term } r = \frac{\sqrt{13} - 1}{2}$$

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29. (D) Two dice are thrown together

$$n(S) = 6 \times 6 = 36$$

the difference of the numbers appearing on them is 2.

$$E = \{(1, 3), (3, 1), (2, 4), (4, 2), (3, 5), (5, 3), (4, 6), (6, 4)\}$$

$$n(E) = 8$$

$$P(E) = \frac{n(E)}{n(S)} = \frac{8}{36} = \frac{2}{9}$$

30. (C) Given that

$$x = (1011)_2 \text{ and } y = (100)_2$$

$$\begin{array}{r} 1011 \\ \hline 1 \times 2^0 = 1 \\ 1 \times 2^1 = 2 \\ 0 \times 2^2 = 0 \\ 1 \times 2^3 = 8 \\ \hline 11 \end{array}$$

$$x = (1011)_2 = (11)_{10}$$

$$\begin{array}{r} 100 \\ \hline 0 \times 2^0 = 0 \\ 0 \times 2^1 = 0 \\ 0 \times 2^2 = 4 \\ \hline 4 \end{array}$$

$$y = (100)_2 = (4)_{10}$$

$$\begin{aligned} x^2 - y^2 &= (11)^2 - (4)^2 \\ &= 121 - 16 \\ &= (105)_{10} \end{aligned}$$

$$\begin{array}{r|rr} 2 & 105 & \\ \hline 2 & 52 & 1 \\ 2 & 26 & 0 \\ 2 & 13 & 0 \\ 2 & 6 & 1 \\ 2 & 3 & 0 \\ 2 & 1 & 1 \\ \hline & 0 & 1 \end{array} \uparrow$$

$$x^2 - y^2 = (105)_{10} = 1101001$$

31. (C) Vectors $6\hat{i} + 2\hat{j}$, $3\hat{i} - 4\hat{j}$ and $2\hat{i} - \lambda\hat{j}$ are collinear.

$$\text{then } \begin{vmatrix} 6 & 2 & 1 \\ 3 & -4 & 1 \\ 2 & -\lambda & 1 \end{vmatrix} = 0$$

$$\begin{aligned} 6(-4 + \lambda) - 2(3 - 2) + 1(-3\lambda + 8) &= 0 \\ 3\lambda - 18 &= 0 \\ \lambda &= 6 \end{aligned}$$

32. (B) $3^{2 - \log_3 4 + \log_3 2}$

$$\Rightarrow 3^2 \times 3^{-\log_3 4} \times 3^{\log_3 2}$$

$$= 9 \times 3^{\log_3 \frac{1}{4}} \times 3^{\log_3 2}$$

$$= 9 \times \frac{1}{4} \times 2$$

$$= \frac{9}{2}$$

33. (A) Given = {1, 2, 3, 4, 5, 6}

4 digit number less than 2000.

$$\boxed{1} \boxed{6} \boxed{6} \boxed{6} = 1 \times 6 \times 6 \times 6 = 216$$

Only (1) can put here.

number of 4 digit numbers each less than 2000 = 216

34. (A) ${}^nC_{32} = {}^nC_5$
 $n = 32 + 5$

$$= 37 \quad [\because {}^nC_r = {}^nC_s \text{ then } n = r + s]$$

35. (B) {0, 1, 2, 3, 4, 5, 6}

3 digit numbers formed by using the digits when repetition is not allowed.

$$\boxed{6} \boxed{6} \boxed{5} = 6 \times 6 \times 5 = 180$$

'0' can not put here.

number of 3 digit numbers = 180

36. (D)

Age	Person (f)	C
0-10	6	6
10-20	7	13
20-30	10	23
30-40	12	35
40-50	18	53
50-60	7	60

$$\frac{n}{2} = \frac{60}{2} = 30$$

$$l_1 = 30, l_2 = 40$$

$$f_1 = 12, C = 23$$

$$\text{Median} = l_1 + \frac{\frac{n}{2} - C}{f} \times (l_2 - l_1)$$

$$= 30 + \frac{30 - 23}{12} \times (40 - 30)$$

$$= 30 + \frac{7}{12} \times 10$$

$$= 30 + \frac{35}{6}$$

$$\text{Median} = \frac{215}{6}$$

37. (A)

class	x	f	f × x
0-4	2	9	18
4-8	6	6	36
8-12	10	8	80
12-16	14	2	28
16-20	18	5	90
		Σf = 30	Σf × x = 252

$$\begin{aligned} \text{Mean} &= \frac{\sum f \times x}{\sum f} \\ &= \frac{252}{30} \\ &= 8.4 \end{aligned}$$

38. (C)

Conic

$$\begin{aligned} 4x^2 - 16y^2 + 24x + 64y &= 4 \\ 4x^2 + 24x - 16y^2 + 64y &= 4 \\ 4(x+3)^2 - 16(y-2)^2 &= -4 \\ \frac{(x+3)^2}{6} - \frac{(y-2)^2}{\frac{3}{2}} &= -1 \end{aligned}$$

$$a^2 = 6, \quad b^2 = \frac{3}{2}$$

then

$$\begin{aligned} e^2 &= 1 + \frac{a^2}{b^2} \\ e^2 &= 1 + \frac{6 \times 2}{3} \\ e^2 &= 5 \end{aligned}$$

eccentricity $e = \sqrt{5}$

39. (A) Let locus of a point = (h, k, l) which is equidistance from the points (3, -4, -2) and (4, 3, -2).

$$\begin{aligned} \Rightarrow \sqrt{(h-3)^2 + (k+4)^2 + (l+2)^2} \\ &= \sqrt{(h-4)^2 + (k-3)^2 + (l+2)^2} \\ \Rightarrow h^2 + 9 - 6h + k^2 + 16 + 8k + (l+2)^2 \\ &= h^2 + 16 - 8h + k^2 + 9 - 6k + (l+2)^2 \\ \Rightarrow -6h + 8k &= -8h - 6k \\ \Rightarrow 14k &= -2h \\ \Rightarrow h + 7k &= 0 \end{aligned}$$

Locus of a point is $x + 7y = 0$

40. (B) Equation of the circle

$$x^2 + y^2 + x - 3y + 5 = 0$$

On comparing with general equation

$$x^2 + y^2 + 2gx + 2fy + c = 0$$

$$g = \frac{1}{2}, \quad f = -\frac{3}{2}, \quad c = 5$$

$$\text{centre} = (-g, -f) = \left(-\frac{1}{2}, \frac{3}{2}\right)$$

41. (B) Given that

$$f(x) = \tan^{-1} \left(\frac{x^x - x^{-x}}{2} \right)$$

differentiate both side w.r.t. 'x'.

$$f'(x) = \frac{1}{1 + \left(\frac{x^x - x^{-x}}{2} \right)^2} \frac{d}{dx} \left(\frac{x^x - x^{-x}}{2} \right)$$

$$f'(x) = \frac{4}{(x^x + x^{-x})^2} \times \frac{1}{2} \left[\frac{d}{dx}(x^x) - \frac{d}{dx}(x^{-x}) \right]$$

we know that $\frac{d}{dx}(x^x) = x^x(1 + \log x)$

and $\frac{d}{dx}(x^{-x}) = -x^x(1 + \log x)$

$$f'(x) = \frac{2}{(x^x + x^{-x})^2} [x^x(1 + \log x) + x^x(1 + \log x)]$$

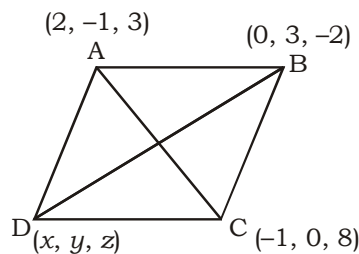
$$f'(x) = \frac{2}{(x^x + x^{-x})^2} [(1 + \log x)(x^x + x^{-x})]$$

$$f'(x) = \frac{2(1 + \log x)}{(x^x + x^{-x})}$$

42. (C) $C(25, 5) + \sum_{r=1}^4 C(29-r, 4)$

$$\begin{aligned} \Rightarrow {}^{25}C_5 + C(28, 4) + C(27, 4) + C(26, 4) + C(25, 4) \\ \Rightarrow {}^{25}C_5 + {}^{25}C_4 + {}^{26}C_4 + {}^{27}C_4 + {}^{28}C_4 \\ \Rightarrow {}^{26}C_5 + {}^{26}C_4 + {}^{27}C_4 + {}^{28}C_4 \quad [\because {}^nC_r + {}^nC_{r+1} = {}^{n+1}C_{r+1}] \\ \Rightarrow {}^{27}C_5 + {}^{27}C_4 + {}^{28}C_4 \\ \Rightarrow {}^{28}C_5 + {}^{28}C_4 \\ \Rightarrow {}^{29}C_5 = C(29, 5) \end{aligned}$$

43. (D) Let $D = (x, y, z)$



In Rhombus mid-point of diagonals are same.

So mid-point of AC = mid point of BD

$$\left(\frac{2-1}{2}, \frac{-1+0}{2}, \frac{3+8}{2} \right) = \left(\frac{x+0}{2}, \frac{y+3}{2}, \frac{z-2}{2} \right)$$

$$\left(\frac{1}{2}, \frac{-1}{2}, \frac{11}{2} \right) = \left(\frac{x}{2}, \frac{y+3}{2}, \frac{z-2}{2} \right)$$

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on comparing

$$\frac{x}{2} = \frac{1}{2} \Rightarrow x = 1$$

$$\frac{y+3}{2} = \frac{-1}{2} \Rightarrow y = -4$$

$$\frac{z-2}{2} = \frac{11}{2} \Rightarrow z = 13$$

$$D(x, y, z) = (1, -4, 13)$$

44. (A) Given that

$$\text{eccentricity } e = \frac{\sqrt{17}}{4},$$

$$\text{length of latusrectum} = \frac{15}{4}$$

$$\sqrt{1 + \frac{b^2}{a^2}} = \frac{\sqrt{17}}{4}, \quad \frac{2b^2}{a} = \frac{15}{4} \dots(i)$$

$$1 + \frac{b^2}{a^2} = \frac{17}{16}$$

$$\frac{b^2}{a^2} = \frac{1}{16}$$

$$\frac{b}{a} = \frac{1}{4} \quad \dots(ii)$$

put the equation (i)

$$2b \times \frac{1}{4} = \frac{15}{4}$$

$$b = \frac{15}{2}$$

from equation (ii)

$$a = 30$$

$$\text{length of transverse axis} = 2a = 2 \times 30 = 60$$

45. (B) $z = 1 - \sqrt{3}i$

$$\text{argument } (\theta) = \tan^{-1} \left(\frac{b}{a} \right) \left[\begin{array}{l} \because \text{when } z = a + ib \\ \text{then } \theta = \tan^{-1} \left(\frac{b}{a} \right) \end{array} \right]$$

$$\theta = \tan^{-1} \left(-\tan \frac{\pi}{3} \right)$$

$$\theta = \tan^{-1} \left(\tan \frac{-\pi}{3} \right)$$

$$\theta = \frac{-\pi}{3}$$

46. (B) $3^x = 5^y = 37 \dots(i)$

$$\text{and } 3^{x+2} - 5^{y+1} = 218$$

$$3^x \cdot 9 - 5^y \cdot 5 = 218 \dots(ii)$$

$$\text{Let } 3^x = a, 5^y = b$$

from equation (i) and equation (ii)

$$a + b = 32 \text{ and } 9a - 5b = 218$$

on solving the equation

$$b = 5 \text{ and } a = 27$$

$$5^y = 5, \quad 3^x = 27$$

$$y = 1, \quad x = 3$$

47. (D) 'TRANSVERSE'

Total number of words which is formed from

$$\text{the letters of the given word} = \frac{10!}{2!2!2!}$$

$$= \frac{10!}{8}$$

TRANSVERSE \rightarrow (AEE) TRNSVRS



as a one letter

Total number of words when vowels comes together

$$= \frac{8!}{2!2!} \times \frac{3!}{2!}$$

$$= \frac{8! \times 3!}{8}$$

Total number of words when vowels never comes together.

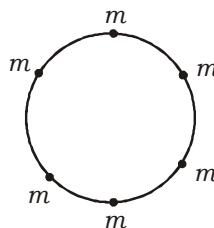
$$= \frac{10!}{8} - \frac{8! \times 3!}{8}$$

$$= \frac{1}{8} [10 \times 9 \times 8! - 8! \times 3 \times 2 \times 1]$$

$$= \frac{8!}{8} \times 84$$

$$= \frac{21}{2} \times 8!$$

48. (D) Find we fix the alternate position of the men. 6 men can be seated around the circle in $(6 - 1)! = 5!$



6 women can be seated in 6 vacant place by 6!. Total number of ways = $5! \times 6!$

49. (C) Given that

$$P(A) = \frac{1}{2}, \quad P\left(\frac{B}{A}\right) = \frac{1}{2} \text{ and } P\left(\frac{A}{B}\right) = \frac{1}{4}$$

$$P\left(\frac{B}{A}\right) = \frac{P(B \cap A)}{\frac{1}{2}}$$

$$\frac{1}{2} = \frac{P(B \cap A)}{\frac{1}{4}}$$

$$P(A \cap B) = \frac{1}{8}$$

$$\text{and } P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$\frac{1}{4} = \frac{\frac{1}{8}}{P(B)}$$

$$P(B) \times \frac{1}{4} = \frac{1}{8}$$

$$P(B) = \left(\frac{1}{2}\right)$$

$$P(A \cap B) = \frac{1}{8} = \frac{1}{4} \times \frac{1}{2} = P(A) \cdot P(B)$$

A and B are independent.

$$\text{Now } P\left(\frac{A'}{B}\right) = \frac{P(A' \cap B)}{P(B)}$$

$$= \frac{P(A')P(B)}{P(B)}$$

$$= P(A')$$

$$P\left(\frac{A'}{B}\right) = \frac{3}{4} \quad \left[\because P(A) = \frac{1}{4} \right]$$

50. (A) We know that

$$1^3 + 2^3 + 3^3 \dots + n^3 = \left[\frac{1}{2} + (n+1) \right]^2$$

$$\text{and } 1 + 2 + 3 + \dots + n = \frac{1}{2} n(n+1)$$

$$\text{then } n\text{th term of the series} = \frac{1^3 + 2^3 + 3^3 \dots n^3}{1 + 2 + 3 + \dots + n}$$

$$= \frac{\left(\frac{1}{2}n(n+1)\right)^2}{\frac{1}{2}n(n+1)}$$

$$= \frac{1}{2} n(n+1)$$

51. (C) Statement (I) :

2	305	1
2	152	1
2	76	0
2	38	0
2	19	0
2	9	1
2	4	1
2	2	0
2	1	0
	0	1

$$(305)_{10} = (100110001)_2$$

Statement (I) is correct.

Statement (II) is correct.

$$52. (B) \quad \sin 10 \sin 30 \sin 50 \sin 70$$

$$= \sin 30 (\sin 10 \sin 50 \sin 70)$$

$$= \frac{1}{2} \times \frac{1}{4} \times \sin 30$$

$$[\sin \theta \sin (60 - \theta) \sin (60 + \theta) = 1/4 \sin 3\theta]$$

$$= \frac{1}{8} \times \frac{1}{2} = \frac{1}{16}$$

53. (C) Given that In ΔABC

$\angle A, \angle B, \angle C$ are in A.P.

Let $\angle A = B - P, \angle B, \angle C = B + P$

then $B - P + B + B + P = 130$

$$3B = 180$$

$$B = 60$$

and given that $b : c = \sqrt{3} : 2$

sine rule

$$\frac{\sin B}{b} = \frac{\sin C}{c}$$

$$\frac{\sin 60}{\sqrt{3}} = \frac{\sin C}{2}$$

$$\sin C = 1$$

$$C = 90^\circ$$

54. (D) $B = 60^\circ, C = 90^\circ$ then $A = 30^\circ$

55. (D) sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{a}{\sin 30} = \frac{b}{\sin 60} = \frac{c}{\sin 90}$$

$$\frac{a \times 2}{1} = \frac{b \times 2}{\sqrt{3}} = \frac{c}{1}$$

$$\frac{a}{1} = \frac{b}{\sqrt{3}} = \frac{c}{2}$$

$$a : b : c = 1 : \sqrt{3} : 2$$

56. (A) $A = 30^\circ, B = 60^\circ, C = 90^\circ$

ΔABC is a right angle triangle.

57. (A) $\cos^2 A + \cos^2 B + \cos^2 C$

$$\Rightarrow \cos^2 30 + \cos^2 60 + \cos^2 90$$

$$\Rightarrow \left(\frac{\sqrt{3}}{2}\right)^2 + \left(\frac{1}{2}\right)^2 + (0)^2$$

$$\Rightarrow \frac{3}{4} + \frac{1}{4} + 0$$

$$\Rightarrow 1$$

58. (C) Angles of a triangle = 1 : 3 : 8

Let angles $x, 3x, 8x$

$$x + 3x + 8x = 180$$

$$12x = 180$$

$$x = 15$$

angles $15^\circ, 45^\circ, 120^\circ$

Sine Rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\text{then } \frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\frac{\text{greatest side}}{\text{least side}} = \frac{c}{a} = \frac{\sin C}{\sin A}$$

$$\frac{c}{a} = \frac{\sin 120}{\sin 15}$$

$$\frac{c}{a} = \frac{\frac{\sqrt{3}}{2}}{\frac{(\sqrt{3}-1)}{2\sqrt{2}}}$$

$$\frac{c}{a} = \frac{\sqrt{6}}{(\sqrt{3}-1)}$$

$$\frac{c}{a} = \frac{3+\sqrt{3}}{\sqrt{2}}$$

$$c : a = (3 + \sqrt{3}) : \sqrt{2}$$

59. (D) In ΔABC

Sine Rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = K$$

$$a = K \sin A, b = K \sin B, c = K \sin C$$

$$\text{then } \frac{a+b}{c} = \frac{K \sin A + K \sin B}{K \sin C}$$

$$= \frac{\sin A + \sin B}{\sin C}$$

$$= \frac{2 \sin \frac{A+B}{2} \cdot \cos \frac{A-B}{2}}{2 \cdot \sin \frac{C}{2} \cdot \cos \frac{C}{2}}$$

$$= \frac{2 \sin \left[90 - \frac{C}{2} \right] \cdot \cos \frac{A-B}{2}}{2 \cdot \sin \frac{C}{2} \cdot \cos \frac{C}{2}}$$

$$= \frac{2 \cos \frac{C}{2} \cdot \cos \frac{A-B}{2}}{2 \sin \frac{C}{2} \cdot \cos \frac{C}{2}}$$

$$\frac{a+b}{c} = \frac{\cos \frac{A-B}{2}}{\sin \frac{C}{2}}$$

60. (D) $\tan^{-1} \left[\frac{\sqrt{1-\sin x} - \sqrt{1+\sin x}}{\sqrt{1-\sin x} + \sqrt{1+\sin x}} \right]$

$$\Rightarrow \tan^{-1} \left[\frac{\sqrt{1-\sin x} - \sqrt{1+\sin x}}{\sqrt{1-\sin x} + \sqrt{1+\sin x}} \times \frac{\sqrt{1-\sin x} - \sqrt{1+\sin x}}{\sqrt{1-\sin x} - \sqrt{1+\sin x}} \right]$$

$$\Rightarrow \tan^{-1} \left[\frac{2 - 2\sqrt{1-\sin^2 x}}{-2 \sin x} \right]$$

$$\Rightarrow \tan^{-1} \left[\frac{2(1-\cos x)}{-2 \sin x} \right]$$

$$\Rightarrow \tan^{-1} \left[\frac{-2 \sin^2 \frac{x}{2}}{2 \sin \frac{x}{2} \cdot \cos \frac{x}{2}} \right]$$

$$\Rightarrow \tan^{-1} \left[-\tan \frac{x}{2} \right]$$

$$\Rightarrow \tan^{-1} \left[\tan \left(-\frac{x}{2} \right) \right]$$

$$\Rightarrow -\frac{x}{2}$$

61. (B) Given that

$$\sin^{-1} \left(\frac{1}{\sqrt{7}} \right) = \theta$$

$$\sin \theta = \frac{1}{\sqrt{7}}$$

$$\operatorname{cosec} \theta = \sqrt{7}$$

$$\theta = \operatorname{cosec}^{-1} (\sqrt{7})$$

$$\theta = \frac{\pi}{2} - \sec^{-1} (\sqrt{7})$$

$$\sec^{-1} (\sqrt{7}) = \frac{\pi}{2} - \theta$$

$$62. (D) \cos \left[\cos^{-1} \left(\frac{3}{5} \right) - \sin^{-1} x \right] = 1$$

$$\cos \left[\cos^{-1} \left(\frac{3}{5} \right) - \sin^{-1} x \right] = \cos 0$$

$$\cos^{-1} \left(\frac{3}{5} \right) - \sin^{-1} x = 0$$

$$\sin^{-1} x = \cos^{-1} \left(\frac{3}{5} \right)$$

$$\sin^{-1} x = \sin^{-1} \left(\frac{4}{5} \right)$$

$$[\because \cos^{-1} x = \sin^{-1} \sqrt{1-x^2}]$$

$$x = \frac{4}{5}$$

$$63. (D) \cot \left[2 \tan^{-1} \left(\frac{1}{3} \right) - \frac{\pi}{4} \right]$$

$$\cot \left[2 \tan^{-1} \frac{2 \times \frac{1}{3}}{1 - \left(\frac{1}{3} \right)^2} - \frac{\pi}{4} \right]$$

$$[\because 2 \tan^{-1} x = \tan^{-1} \frac{2x}{1-x^2}]$$

$$\cot \left[\tan^{-1} \left(\frac{3}{4} \right) - \tan^{-1} (1) \right]$$

$$\cot \left[\tan^{-1} \left(\frac{\frac{3}{4} - 1}{1 + \frac{3}{4} \times 1} \right) \right]$$

$$\cot \left[\tan^{-1} \left(\frac{-1}{7} \right) \right]$$

$$\cot [\cot^{-1} (-7)] = -7$$

$$64. (D) \cos \left[\tan^{-1} \frac{12}{5} - \tan^{-1} \frac{4}{3} \right]$$

$$\Rightarrow \cos \left[\tan^{-1} \left(\frac{\frac{12}{5} - \frac{4}{3}}{1 + \frac{12}{5} \times \frac{4}{3}} \right) \right]$$

$$[\because \tan^{-1} x - \tan^{-1} y = \tan^{-1} \left(\frac{x-y}{1+xy} \right)]$$

$$= \cos \left[\tan^{-1} \left(\frac{16}{63} \right) \right]$$

$$= \cos \left[\cos^{-1} \left(\frac{1}{\sqrt{1 + \left(\frac{16}{63} \right)^2}} \right) \right]$$

$$[\because \tan^{-1} x = \cos^{-1} \left(\frac{1}{\sqrt{1+x^2}} \right)]$$

$$= \cos \left(\cos^{-1} \left(\frac{63}{65} \right) \right)$$

$$= \frac{63}{65}$$

$$65. (C) \cot \left[\cot^{-1} \frac{7}{3} + \cos^{-1} \frac{3}{5} \right]$$

$$\Rightarrow \cot \left[\cot^{-1} \left(\frac{7}{3} \right) + \cot^{-1} \left(\frac{3}{4} \right) \right]$$

$$\Rightarrow \cot \left[\cot^{-1} \left(\frac{\frac{7}{3} \times \frac{3}{4} - 1}{\frac{7}{3} + \frac{3}{4}} \right) \right]$$

$$\left[\cot^{-1} x + \cot^{-1} y = \cot^{-1} \left(\frac{xy-1}{x+y} \right) \right]$$

$$\Rightarrow \cot \left(\cot^{-1} \frac{9}{37} \right) = \frac{9}{37}$$

$$66. (C) f(x) = \lim_{x \rightarrow \infty} \left\{ x^2 \sin \frac{2}{x} \right\}$$

$$= \lim_{x \rightarrow \infty} \left\{ x \frac{\sin \frac{2}{x}}{\frac{1}{x}} \right\}$$

$$= \lim_{x \rightarrow \infty} \left\{ 2x \frac{\sin \frac{2}{x}}{\frac{2}{x}} \right\}$$

$$= \lim_{x \rightarrow \infty} \{ 2x \times 1 \} \left\{ \because \lim_{x \rightarrow \infty} \frac{\sin \frac{1}{x}}{\frac{1}{x}} = 1 \right\}$$

$$= 2 \times \infty = \infty$$

67. (B) $f(x) = \lim_{x \rightarrow 0} \left[\frac{1 - \sin x}{1 - \tan x} \right]^{\operatorname{cosec} x}$ $[1^\infty]$ Form

$$= \lim_{x \rightarrow 0} \frac{[1 - \sin x]^{\frac{1}{\sin x}}}{\left[\left(1 - \frac{\sin x}{\cos x} \right)^{\frac{\cos x}{\sin x}} \right]^{\frac{1}{\cos x}}}$$

$$= \frac{e^{-1}}{e^{-\lim_{x \rightarrow 0} \frac{1}{\cos x}}} \quad \left[\because \lim_{x \rightarrow 0} (1 + \lambda x)^{\frac{1}{x}} = e^\lambda \right]$$

$$= \frac{e^{-1}}{e^{-1}}$$

$$= \frac{e^{-1}}{e^{-1}}$$

$$= 1$$

68. (A) $f(x) = \begin{cases} 4x - 7, & 0 \leq x \leq 3 \\ 2x - \lambda, & 3 < x \leq 5 \end{cases}$ is continuous

at $x = 3$ then

$$\lim_{x \rightarrow 3^+} f(x) = \lim_{x \rightarrow 3^-} f(x)$$

$$2 \times 3 - \lambda = 4 \times 3 - 7$$

$$6 - \lambda = 12 - 7$$

$$6 - \lambda = 5$$

$$\lambda = 1$$

69. (C) $f(x) = \lim_{x \rightarrow \infty} \left(1 + \frac{4}{x+2} \right)^{4x-3}$ (1^∞) form

$$f(x) = \lim_{x \rightarrow \infty} \left[\left(1 + \frac{4}{x+2} \right)^{\frac{x+2}{4}} \right]^{\frac{4}{x+2}(4x-3)}$$

$$f(x) = e^{\lim_{x \rightarrow \infty} \frac{4(4x-3)}{x+2}} \quad \left[\because \lim_{x \rightarrow \infty} \left(1 + \frac{1}{x} \right)^x = e \right]$$

$$= \lim_{x \rightarrow \infty} \frac{x(16 - \frac{12}{x})}{x(1 + \frac{2}{x})}$$

$$= e^{\frac{16}{1}} = e^{16}$$

70. (C) $f(x) = \begin{cases} 5 \times 6^x, & x \leq 1 \\ 8a - 2x, & x > 1 \end{cases}$ is continuous at $x = 1$

then $\lim_{x \rightarrow 1^+} f(x) = \lim_{x \rightarrow 1^-} f(x)$

$$\lim_{x \rightarrow 1} 8a - 2x = \lim_{x \rightarrow 1} 5 \times 6^x$$

$$8a - 2 \times 1 = 5 \times 6^1$$

$$8a - 2 = 30$$

$$8a = 32$$

$$a = 4$$

71. (A) Given that

A.M of $(a$ and $b)$: G.M of $(a$ and $b) = 5 : 4$

$$\frac{a+b}{2} : \sqrt{ab} = 5 : 4$$

$$\frac{a+b}{2\sqrt{ab}} = \frac{5}{4}$$

$$\frac{a+b+2\sqrt{ab}}{a+b-2\sqrt{ab}} = \frac{5+4}{5-1} \quad (\text{by componendo and dividendo Rule})$$

$$\frac{(\sqrt{a} + \sqrt{b})^2}{(\sqrt{a} - \sqrt{b})^2} = \frac{9}{1}$$

$$\frac{\sqrt{a} + \sqrt{b}}{\sqrt{a} - \sqrt{b}} = \frac{3}{1}$$

$$\frac{\sqrt{a}}{\sqrt{b}} = \frac{4}{2} \quad [\text{again componendo and dividendo Rule}]$$

$$\frac{\sqrt{a}}{\sqrt{b}} = \frac{2}{1}$$

$$\frac{a}{b} = \frac{4}{1} \quad \text{or } a : b = 4 : 1$$

72. (C)

73. (D) $\begin{vmatrix} 1 + 2\omega^{100} + \omega^{200} & \omega^2 & 1 \\ 1 & 1 + \omega^{100} + 2\omega^{200} & \omega \\ \omega & \omega^2 & 2 + \omega^{100} + 2\omega^{200} \end{vmatrix}$

$$= \begin{vmatrix} 1 + 2\omega + \omega^2 & \omega^2 & 1 \\ 1 & 1 + \omega + 2\omega^2 & \omega \\ \omega & \omega^2 & 2 + \omega + 2\omega^2 \end{vmatrix}$$

$$= \begin{vmatrix} -\omega + 2\omega & \omega^2 & 1 \\ 1 & -\omega^2 + 2\omega^2 & \omega \\ \omega & \omega^2 & -2\omega + \omega \end{vmatrix} \quad [\because 1 + \omega + \omega^2 = 0]$$

$$= \begin{vmatrix} \omega & \omega^2 & 1 \\ 1 & \omega^2 & \omega \\ \omega & \omega^2 & -\omega \end{vmatrix}$$

$$= \omega(-\omega^3 - \omega^3) - \omega^2(-\omega - \omega^2) + 1(\omega^2 - \omega^3)$$

$$= -2\omega - 1$$

74. (D) Given that $a^{-1} + b^{-1} + c^{-1} = 0$

$$\frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 0$$

$$\begin{vmatrix} 1+a & 1 & 1 \\ 1 & 1+b & 1 \\ 1 & 1 & 1+c \end{vmatrix} = \lambda$$



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$$abc \begin{vmatrix} \frac{1}{a}+1 & \frac{1}{b} & \frac{1}{c} \\ \frac{1}{a} & \frac{1}{b}+1 & \frac{1}{c} \\ \frac{1}{a} & \frac{1}{b} & \frac{1}{c}+1 \end{vmatrix} = \lambda$$

$$C_1 \rightarrow C_1 + C_2 + C_3$$

$$abc \begin{vmatrix} \frac{1}{a} + \frac{1}{b} + \frac{1}{c} & \frac{1}{b} & \frac{1}{c} \\ \frac{1}{a} + \frac{1}{b} + \frac{1}{c} & \frac{1}{b} + 1 & \frac{1}{c} \\ \frac{1}{a} + \frac{1}{b} + \frac{1}{c} & \frac{1}{b} & \frac{1}{c} + 1 \end{vmatrix} = \lambda$$

$$abc \begin{vmatrix} 1 & \frac{1}{b} & \frac{1}{c} \\ 1 & \frac{1}{b}+1 & \frac{1}{c} \\ 1 & \frac{1}{b} & \frac{1}{c}+1 \end{vmatrix} = \lambda \quad \left[\because \frac{1}{a} + \frac{1}{b} + \frac{1}{c} = 0 \right]$$

$$R_1 \rightarrow R_1 - R_2, \quad R_3 \rightarrow R_3 - R_2$$

$$abc \begin{vmatrix} 0 & -1 & 0 \\ 1 & \frac{1}{b}+1 & \frac{1}{c} \\ 0 & -1 & 1 \end{vmatrix} = \lambda$$

$$abc [0 + 1(1-0) + 0] = \lambda$$

$$abc [1] = \lambda$$

$$\lambda = abc$$

75. (B) Series

$$S = 3 + 7 + 13 + 21 + \dots + a_{n-1} + a_n$$

$$S = \quad 3 + 7 + 13 + \dots + a_{n-1} + a_n$$

$$\quad - \quad - \quad - \quad - \quad - \quad -$$

$$0 = (3 + 4 + 6 + 8 + \dots + n \text{ term}) - a_n$$

$$a_n = 3 + 4 + 6 + 8 + \dots n \text{ term}$$

$$= 3 + (4 + 6 + 8 \dots (n-1) \text{ term})$$

$$= 3 + \frac{n-1}{2} [2 \times 4 + (n-2) \times 2]$$

$$= 3 + n-1 [4 + n-2]$$

$$a_n = 3 + (n-1)(n+2)$$

$$a_n = n^2 + n + 1$$

$$10^{\text{th}} \text{ term } a_{10} = (10)^2 + 10 + 1$$

$$= 100 + 11$$

$$= 111$$

76. (A) $\left(-4x^2 + \frac{1}{3x^2}\right)^4$

3rd term in the expansion

$$T_3 = T_{2+1} = {}^4C_2 (-4x^2)^{4-2} \left(\frac{1}{3x^2}\right)^2$$

$$= \frac{4!}{2!2!} (-4x^2)^2 \frac{1}{9x^4}$$

$$= 6 \times \frac{16x^4}{9x^4}$$

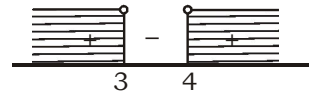
$$= 6 \times \frac{16}{9}$$

$$= \frac{32}{3}$$

77. (A) $x^2 - 7x + 12 > 0$

$$(x-4)(x-3) > 0$$

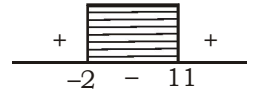
$$x = 3, 4$$



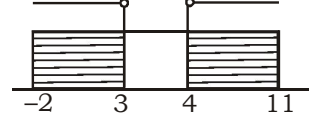
and $x^2 - 9x - 22 \leq 0$

$$(x-11)(x+2) \leq 0$$

$$x = 11, -2$$



then



$$-2 \leq x < 3 \text{ and } 4 < x \leq 11$$

$$x \in [-2, 3) \cup (4, 11]$$

78. (A) $\sin^2 30^\circ, \sin^2 45^\circ$ and $\sin^2 60^\circ$

$$\left(\frac{1}{2}\right)^2, \left(\frac{1}{\sqrt{2}}\right)^2 \text{ and } \left(\frac{\sqrt{3}}{2}\right)^2$$

$$\frac{1}{4}, \frac{1}{2} \text{ and } \frac{3}{4} \text{ are in A.P.}$$

then $\sin^2 30^\circ, \sin^2 45^\circ$ and $\sin^2 60^\circ$ are in A.P.

79. (D) $f(x) = \frac{x}{x^2 + 1}$

for one-one
 $f(x_1) = f(x_2)$

$$\frac{x_1}{x_1^2 + 1} = \frac{x_2}{x_2^2 + 1}$$

$$x_1 x_2^2 + x_1 = x_1^2 x_2 + x_2$$

$x_1 - x_2 + x_1x_2^2 - x_1^2x_2 = 0$
 $(x_1 - x_2)(1 - x_1x_2) = 0$
 $x_1 = x_2, x_1x_2 \neq 1$
 So, function $f(x)$ is one-one.

Let $y = \frac{x}{x^2+1}$

$yx^2 + y = x$
 $yx^2 - x + y = 0$

$$x = \frac{-1 \pm \sqrt{(-1)^2 - 4 \times y \times y}}{2 \times y}$$

$$x = \frac{-1 \pm \sqrt{1 - 4y^2}}{2y}$$

$1 - 4y^2 \geq 0$ and $y \neq 0$
 $(1 - 2y)(1 + 2y) \geq 0$
 $(2y - 1)(2y + 1) \leq 0$

$$\begin{array}{c} + \quad - \quad + \\ \hline \frac{-1}{2} \quad \frac{1}{2} \end{array}$$

$$y \in \left[-\frac{1}{2}, \frac{1}{2}\right] - \{0\}$$

and codomain = R
 Range(y) \neq codomain
 so, $f(x)$ is not onto.

Hence $f(x)$ is one-one but not onto.

80. (C) Let $y = 3^{96}$

taking log
 $\log_{10}y = 96 \log_{10}3$
 $= 96 \times 0.4771$
 $= 45.8016$

The number of digits in $3^{96} = 46$.

81. (C) $\sqrt{2 + \sqrt{2 + \sqrt{2 + \sqrt{2 + 2 \cos 8\theta}}}}$

$$\Rightarrow \sqrt{2 + \sqrt{2 + \sqrt{2 + \sqrt{2(1 + \cos 8\theta)}}}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 + \sqrt{2 + \sqrt{2 \times 2 \cos^2 4\theta}}}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 + \sqrt{2 + 2 \cos 4\theta}}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 + \sqrt{2(1 + \cos 4\theta)}}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 + \sqrt{2 \times 2 \cos^2 2\theta}}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 + 2 \cos 2\theta}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2(1 + \cos 2\theta)}}$$

$$\Rightarrow \sqrt{2 + \sqrt{2 \times 2 \cos^2 \theta}}$$

$$\Rightarrow \sqrt{2 + 2 \cos \theta}$$

$$\Rightarrow \sqrt{2(1 + \cos \theta)}$$

$$\Rightarrow 2 \cos \frac{\theta}{2}$$

82. (D) $f(x) = 2x^3 - 3x^2 - 72x + 6$

$$f'(x) = 6x^2 - 6x - 72 \quad \dots(i)$$

again differentiate w.r.t 'x'

$$f''(x) = 12x - 6 \quad \dots(ii)$$

for maxima and minima

$$f'(x) = 0$$

$$6x^2 - 6x - 72 = 0$$

$$(x - 4)(x + 3) = 0$$

$$x = -3, 4$$

On putting the value of x in equation (ii)

$$f''(-3) = 12(-3) - 6 \text{ and } f''(4) = 12 \times 4 - 6$$

$$= -42 \text{ (maxima)} \quad = 42 \text{ (minima)}$$

function is maximum at $x = -3$

83. (B) $I = \int_{-1}^0 x(1+x)^6 dx$

$$I = \int_{-1}^0 (-1-x)(1-x)^6 dx$$

$$\left[\text{Property } \int_a^b f(x) dx = \int_a^b f(a+b-x) dx \right]$$

$$I = \int_{-1}^0 (-1-x)x^6 dx$$

$$I = \int_{-1}^0 (-x^6 - x^7) dx$$

$$= \left[-\frac{x^7}{7} - \frac{x^8}{8} \right]_{-1}^0$$

$$= \left[0 - \left(\frac{(-1)^7}{7} - \frac{(-1)^8}{8} \right) \right]$$

$$= \left[1 - \left(\frac{-1}{7} - \frac{1}{8} \right) \right]$$

$$= \frac{15}{56}$$

84. (A) $\begin{bmatrix} 5 & 0 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} -x \\ y \end{bmatrix} \downarrow = \begin{bmatrix} -10 \\ 3 \end{bmatrix}$

$$\begin{bmatrix} -5x + 0 \\ -3x + y \end{bmatrix} = \begin{bmatrix} -10 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} -5x \\ -3x + y \end{bmatrix} = \begin{bmatrix} -10 \\ 3 \end{bmatrix}$$

on comparing

$$-5x = -10$$

$$x = 2$$

$$\text{and } -3x + y = 3$$

$$-3 \times 2 + y = 3$$

85. (B) Given that $y = 9$

5th term in expansion of $\left(\frac{4}{3}x^2 - \frac{3}{2x^2}\right)^n$ is independent of x .
then

$$T_5 = T_{4+1} = {}^nC_4 \left(\frac{4}{3}x^2\right)^{n-4} \left(\frac{-3}{2x^2}\right)^4$$

$$= {}^nC_4 \left(\frac{4}{3}\right)^{n-4} \left(\frac{-3}{2}\right)^4 x^{2n-16}$$

then $2n - 16 = 0$
 $n = 8$

86. (A) In ΔABC

Let $B - p, B, B + p$ are angles of ΔABC .

$$B - p, B, B + p = 180$$

$$3B = 180$$

$$B = 60$$

then $\cos B = \frac{a^2 + c^2 - b^2}{2ac}$

$$\cos 60 = \frac{a^2 + c^2 - b^2}{2ac}$$

$$\frac{1}{2} = \frac{a^2 + c^2 - b^2}{2ac}$$

$$ac = a^2 + c^2 - b^2$$

$$b^2 = a^2 + c^2 - ac$$

87. (B) $\lim_{x \rightarrow -5} \left(\frac{x+5}{x^3+125}\right)$ $\left[\frac{0}{0}\right]$ Form

by L-Hospital's Rule

$$= \lim_{x \rightarrow -5} \frac{1+0}{3x^2+0}$$

$$= \frac{1}{3 \times (-5)^2}$$

$$= \frac{1}{3 \times 25} = \frac{1}{75}$$

88. (D) $I = \int \sec x^\circ dx$

$$I = \int \sec \frac{\pi x}{180} dx \quad \left[\because 1^\circ = \left(\frac{\pi}{180}\right)^\circ \right]$$

Let $\frac{\pi x}{180} = t$

$$\frac{\pi}{180} dx = dt$$

$$dx = \frac{180}{\pi} dt$$

$$I = \frac{180}{\pi} \int \sec t dt$$

$$I = \frac{180}{\pi} \log \tan \left(\frac{\pi}{4} + \frac{t}{2}\right) + C$$

$$\left[\because \int \sec dx = \log \tan \left(\frac{\pi}{4} + \frac{x}{2}\right) + 1 \right]$$

$$I = \frac{180}{\pi} \log \tan \left(\frac{\pi}{4} + \frac{\pi x}{360}\right) + C$$

89. (B) $I = \int_0^{\frac{\pi}{2}} \log \cos x dx \dots (i)$

$$I = \int_0^{\frac{\pi}{2}} \log \sin x dx \dots (ii) \text{ (Property IV)}$$

on adding equation (i) and equation (ii)

$$2I = \int_0^{\frac{\pi}{2}} [\log \cos x + \log \sin x] dx$$

$$2I = \int_0^{\frac{\pi}{2}} \log \left(\frac{2 \sin x \cdot \cos x}{2}\right) dx$$

$$2I = \int_0^{\frac{\pi}{2}} [\log \sin 2x - \log 2] dx$$

$$2I = \int_0^{\frac{\pi}{2}} \log \sin 2x dx - \int_0^{\frac{\pi}{2}} \log 2 dx$$

Let $2x = t$ when $x \rightarrow 0, t \rightarrow 0$

$$2dx = dt \quad x \rightarrow \frac{\pi}{2}, t \rightarrow \pi$$

$$dx = \frac{1}{2} dt$$

$$2I = \int_0^{\pi} \log \sin t \times \frac{1}{2} dt - \log 2 [x]_0^{\frac{\pi}{2}}$$

$$2I = \frac{1}{2} \int_0^{2 \times \frac{\pi}{2}} \log \sin t dt - \log 2 \left[\frac{\pi}{2} - 0\right]$$

$$2I = \frac{1}{2} \times 2 \int_0^{\frac{\pi}{2}} \log \sin t dt - \frac{\pi}{2} \log 2$$

$$\left[\because \int_0^{2a} f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{if } f(2a-x) = f(x) \\ 0, & \text{if } f(2a-x) = -f(x) \end{cases} \right]$$

$$2I = \int_0^{\frac{\pi}{2}} \sin x dx - \frac{\pi}{2} \log 2 \left[\because \int_0^a f(x) dx = \int_0^a dt \right]$$

$$2I = I - \frac{\pi}{2} \log 2$$

$$I = -\frac{\pi}{2} \log 2$$

$$\int_0^{\frac{\pi}{2}} \log \cos x dx = -\frac{\pi}{2} \log 2$$

90. (C) eccentricities

$e = 0$ for circle

$e = 1$ for parabola

$e < 1$ for ellipse

$e > 1$ for hyperbola

91. (B) $y = e^{\cos \sqrt{x^2+1}}$

differentiate both side w.r.t. x .

$$\begin{aligned} \frac{dy}{dx} &= e^{\cos \sqrt{x^2+1}} \frac{d}{dx} [\cos(\sqrt{x^2+1})] \\ &= e^{\cos \sqrt{x^2+1}} (-\sin \sqrt{x^2+1}) \frac{1}{2\sqrt{x^2+1}} \times 2x \\ &= \frac{-x \sin \sqrt{x^2+1}}{\sqrt{x^2+1}} \cdot e^{\cos \sqrt{x^2+1}} \end{aligned}$$

92. (B) $y = e^{\tan x}$

differentiate both side w.r.t. x .

$$\begin{aligned} \frac{dy}{dx} &= e^{\tan x} \cdot \sec^2 x \\ &= \sec^2 x \cdot e^{\tan x} \end{aligned}$$

93. (A) Let $y = e^{x^2}$ and $z = \log x^2$

$$z = 2 \log x$$

differentiate both w.r.t. x .

$$\frac{dy}{dx} = e^{x^2} \cdot (2x) \text{ and } \frac{dz}{dx} = \frac{2}{x}$$

$$\frac{dy}{dx} = 2x \cdot e^{x^2}, \quad \frac{dx}{dz} = \frac{x}{2}$$

$$\text{then } \frac{dy}{dz} = \frac{dy}{dx} \times \frac{dx}{dz}$$

$$\begin{aligned} &= 2x e^{x^2} \times \frac{x}{2} \\ &= x^2 e^{x^2} \end{aligned}$$

94. (A) Given that

$$\vec{a} = 2\hat{i} - \hat{j} + 3\hat{k} \text{ and } \vec{b} = 4\hat{i} + 4\hat{j} + 2\hat{k}$$

Projection of the vector \vec{a} on the vector \vec{b}

$$= \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|}$$

$$= \frac{2 \times 4 + (-1) \times 4 + 3 \times 2}{\sqrt{(4)^2 + (4)^2 + (2)^2}}$$

$$= \frac{10}{6}$$

$$= \frac{5}{3}$$

95. (A) Let $y = \cos \left[2 \cot^{-1} \sqrt{\frac{1+x}{1-x}} \right]$

Let $x = \cos \phi$

$$y = \cos \left[2 \cot^{-1} \sqrt{\frac{1+\cos \theta}{1-\cos \theta}} \right]$$

$$y = \cos \left[2 \cot^{-1} \sqrt{\frac{2 \cos^2 \frac{\theta}{2}}{2 \sin^2 \frac{\theta}{2}}} \right]$$

$$y = \cos \left[2 \cot^{-1} \left(\cot \frac{\theta}{2} \right) \right]$$

$$y = \cos \left[2 \times \frac{\theta}{2} \right]$$

$$y = \cos \phi$$

$$y = x$$

$$\int \cos \left[2 \cot^{-1} \sqrt{\frac{1+x}{1-x}} \right] dx = \int y dx$$

$$= \int x dx$$

$$= \frac{x^2}{2} + C$$

96. (C) $I = \int \left(\frac{x^2-1}{x^2} \right) \cdot \sec^2 \left(x + \frac{1}{x} \right) dx$

$$\text{Let } x + \frac{1}{x} = t$$

$$\left[1 + \left(\frac{-1}{x^2} \right) \right] dx = dt$$

$$\left(\frac{x^2-1}{x^2} \right) dx = dt$$

$$I = \int \sec^2 t \cdot dt$$

$$= \tan t + c$$

$$I = \tan \left(x + \frac{1}{x} \right) + c$$

97. (B) $I = \int e^x \left(\cos^{-1} x - \frac{1}{\sqrt{1-x^2}} \right) dx$

$$I = \int e^x \left[\cos^{-1} x + \left(\frac{-1}{\sqrt{1-x^2}} \right) \right] dx$$

$$I = e^x \cos^{-1} x + C$$

$$\left[\because \int e^x (f(x) + f'(x)) dx = e^x \cdot f(x) \right]$$

98. (A) $I = \int \frac{x^2 + 1}{x^3 - x} dx$

$$I = \int \frac{1 + \frac{1}{x^2}}{x - \frac{1}{x}} dx$$

Let $x - \frac{1}{x} = t$

$$\left(1 + \frac{1}{x^2}\right) dx = dt$$

$$I = \int \frac{1}{t} dt$$

$$I = \log t + c$$

$$I = \log\left(x - \frac{1}{x}\right) + c$$

99. (B) $I = \int \frac{(x-1)^2}{x(x^2+1)} dx$

$$I = \int \frac{x^2 + 1 - 2x}{x(x^2 + 1)} dx$$

$$I = \int \frac{(x^2 + 1)}{x(x^2 + 1)} dx - \int \frac{2x}{x(x^2 + 1)} dx$$

$$I = \int \frac{1}{x} dx - 2 \int \frac{1}{1 + x^2} dx$$

$$I = \int \frac{1}{x} dx - 2 \int \frac{1}{1 + x^2} dx$$

$$I = \log x - 2 \tan^{-1} x + c$$

100. (A) $I = \int_0^{\frac{\pi}{2}} \frac{\cot x - \tan x}{1 + \sin x \cdot \cos x} dx \quad \dots(i)$

$$I = \int_0^{\frac{\pi}{2}} \frac{\cot\left(\frac{\pi}{2} - x\right) - \tan\left(\frac{\pi}{2} - x\right)}{1 + \sin\left(\frac{\pi}{2} - x\right) \cdot \cos\left(\frac{\pi}{2} - x\right)} dx$$

$$I = \int_0^{\frac{\pi}{2}} \frac{\tan x - \cot x}{1 + \sin x \cdot \cos x} dx \quad \dots(ii)$$

on adding equation (i) and equation (ii)

$$2I = 0$$

$$I = 0$$

101. (D) Let teacher's age = x years.

ATQ,

$$30 \times 12 + x = (30 + 1) \times (12 + 2)$$

$$360 + x = 31 \times 14$$

$$360 + x = 434$$

$$x = 74$$

teacher's age = 74 years.

102. (B) Plane $x + 2y - 5z = 0$
direction cosines of the normal to the plane

$$= \left(\frac{1}{\sqrt{(1)^2 + (2)^2 + (-5)^2}}, \frac{2}{\sqrt{(1)^2 + (2)^2 + (-5)^2}}, \frac{-5}{\sqrt{(1)^2 + (2)^2 + (-5)^2}} \right)$$

$$= \left(\frac{1}{\sqrt{30}}, \frac{2}{\sqrt{30}}, \frac{-5}{\sqrt{30}} \right)$$

103. (C) $I = \int x^2 \cdot \log x dx$

$$I = \log x \int x^2 dx - \int \left\{ \frac{d}{dx}(\log x) \cdot \int x^2 dx \right\} dx + C$$

$$I = (\log x) \times \frac{x^3}{3} - \int \left\{ \frac{1}{x} \cdot \frac{x^3}{3} dx \right\} + C$$

$$I = \frac{x^3}{3} \log x - \frac{1}{3} \int x^2 dx + C$$

$$I = \frac{x^3}{3} \log x - \frac{1}{3} \cdot \frac{x^3}{3} + C$$

$$I = \frac{x^3}{3} \log x - \frac{x^3}{9} + C$$

104. (C) Case - I

Let white ball is drawn from the first bag and placed unseen in the second bag and white ball is drawn from the second bag.

$$\text{Then probability} = \frac{{}^6C_1}{{}^{10}C_1} \times \frac{{}^4C_1}{{}^9C_1} = \frac{24}{90} = \frac{8}{30}$$

Case-II

Let black ball is drawn from the first bag and placed unseen in the second bag and white is drawn from the second bag.

$$\text{then probability} = \frac{{}^4C_1}{{}^{10}C_1} \times \frac{{}^3C_1}{{}^9C_1} = \frac{12}{90} = \frac{4}{30}$$

$$\text{then required probability} = \frac{8}{30} + \frac{4}{30} = \frac{12}{30}$$

$$= \frac{2}{5}$$

105. (B) $2 \log_8 2 - \frac{\log_3 9}{3}$

$$\Rightarrow 2 \times \frac{1}{\log_2 8} - \frac{\log_3 3^2}{3}$$

$$\Rightarrow 2 \times \frac{1}{3 \log_2 2} - \frac{2 \log_3 3}{3}$$

$$\Rightarrow \frac{2}{3} - \frac{2}{3} = 0$$

106. (C) $f(x) = \frac{1}{(x^2 - 1)\log(x + 2)}$

$$\begin{array}{ll} x^2 - 1 \neq 0 & x + 2 > 1 \\ x^2 \neq 1 & x > -1 \\ x \neq \pm 1 & \end{array}$$

domain $x \in (-1, \infty) - \{1\}$

107. (A) $f(x) = 2 - |x - 3|$
for every x , $|x - 3| \geq 0$
 $-|x - 3| \leq 0$
 $2 - |x - 3| \leq 0 + 2$
 $2 - |x - 3| \leq 2$
 $f(x) \leq 2$

Range of $f(x) = (-\infty, 2]$

108. (B) In an A.P.
 p th term $T_p = a + (p - 1)d$

$$\frac{1}{q} = a + (p - 1)d \quad \dots(i)$$

$$q\text{th term } \frac{1}{p} = a + (q - 1)d \quad \dots(ii)$$

equation (i) and equation (ii)

$$d = \frac{1}{pq}, \quad a = \frac{1}{pq}$$

sum of (pq) terms

$$\begin{aligned} S_{pq} &= \frac{pq}{2} (2a + (pq - 1)d) \\ &= \frac{pq}{2} \left(\frac{2}{pq} + \frac{pq - 1}{pq} \right) \end{aligned}$$

$$S_{pq} = \frac{1}{2} (pq + 1)$$

109. (A) Data
20, 20, 20, 20, 21, 21, 22, 22, 22, 23, 23, 23,
24, 24, 25, 25, 22, 22, 24, 23
mode = 22

110. (C) Three observations
2, -4, 8

$$\text{H.M.} = \frac{1}{\frac{1}{n} \left(\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} + \dots + \frac{1}{x_n} \right)}$$

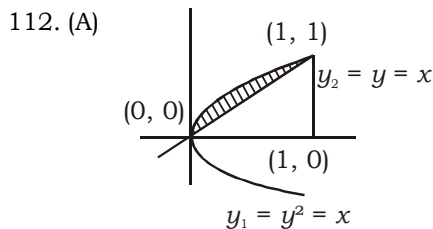
$$\text{then H.M.} = \frac{1}{\frac{1}{3} \left(\frac{1}{2} + \frac{1}{-4} + \frac{1}{8} \right)}$$

$$= \frac{1}{\frac{1}{3} \left(\frac{3}{8} \right)}$$

$$= \frac{1}{\frac{1}{8}} = 8$$

111. (C) $I = \int_0^{2\pi} |\sin x| dx$

$$\begin{aligned} &= \int_0^{\pi} \sin x dx + \int_{\pi}^{2\pi} (-\sin x) dx \\ &= [-\cos x]_0^{\pi} + [\cos x]_{\pi}^{2\pi} \\ &= [-\cos \pi + \cos 0] + [\cos 2\pi - \cos \pi] \\ &= [1 + 1] + [1 + 1] \\ &= 4 \end{aligned}$$

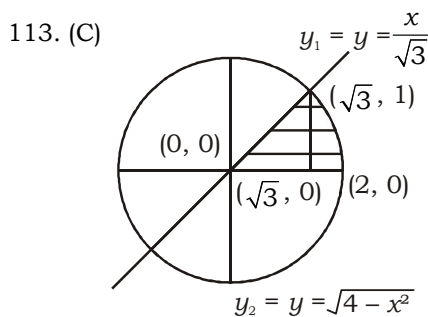


curve $y_1 \Rightarrow y = \sqrt{x} \quad \dots(i)$

and line $y_2 \Rightarrow y = x \quad \dots(ii)$

on solving the equation (i) and equation (ii)
 $x = 0, 1$
 $y = 0, 1$

$$\begin{aligned} \text{Area} &= \int_0^1 (y_1 - y_2) dx \\ &= \int_0^1 (\sqrt{x} - x) dx \\ &= \left[\frac{2}{3} x^{\frac{3}{2}} - \frac{x^2}{2} \right]_0^1 \\ &= \frac{2}{3} - \frac{1}{2} - 0 \\ &= \frac{1}{6} \end{aligned}$$



circle $x^2 + y^2 = 4$

$y_2 \Rightarrow y = \sqrt{4 - x^2} \quad \dots(i)$

and line $x = \sqrt{3} y$

$y_1 \Rightarrow y = \frac{x}{\sqrt{3}} \quad \dots(ii)$

on solving equation (i) and equation (ii)
 $x = \sqrt{3}$ and $y = 1$

$$\text{Area} = \int_0^{\sqrt{3}} y_1 dx + \int_{\sqrt{3}}^2 y_2 dx$$

$$= \int_0^{\sqrt{3}} \frac{x}{\sqrt{3}} dx + \int_{\sqrt{3}}^2 \sqrt{4-x^2} dx$$

$$= \left[\frac{x^2}{2\sqrt{3}} \right]_0^{\sqrt{3}} + \left[\frac{1}{2} x\sqrt{4-x^2} + \frac{4}{2} \sin^{-1} \frac{x}{2} \right]_{\sqrt{3}}^2$$

$$= \left[\frac{(\sqrt{3})^2}{2\sqrt{3}} - 0 \right] + \left[0 + 2\sin^{-1} 1 - \left(\frac{\sqrt{3}}{2} \times 1 + 2\sin^{-1} \frac{\sqrt{3}}{2} \right) \right]$$

$$= \frac{3}{2\sqrt{3}} + \left[2 \times \frac{\pi}{2} - \frac{\sqrt{3}}{2} - 2 \times \frac{\pi}{3} \right]$$

$$= \frac{\sqrt{3}}{2} + \pi - \frac{\sqrt{3}}{2} - \frac{2\pi}{3}$$

$$= \frac{\pi}{3}$$

114. (A) curve $4x^2 + 9y^2 = 1$

$$\frac{x^2}{\frac{1}{4}} + \frac{y^2}{\frac{1}{9}} = 1$$

$$a^2 = \frac{1}{4}, b^2 = \frac{1}{9}$$

$$a = \frac{1}{2}, b = \frac{1}{3}$$

this curve is an ellipse.
 So area of ellipse = πab

$$= \pi \times \frac{1}{2} \times \frac{1}{3}$$

$$= \frac{\pi}{6}$$

115. (D) degree = 2

116. (A) differential equation

$$\frac{dy}{dx} + 2y \tan x = \sin x$$

On comparing with general equation

$$\frac{dy}{dx} + Py = Q$$

$$P = 2 \tan x, Q = \sin x$$

$$I.F. = e^{\int 2 \tan x dx}$$

$$= e^{2 \log \sec x}$$

$$= \sec^2 x$$

Solution of the differential equation

$$y \times I.F. = \int Q \times I.F. dx + C$$

$$y \times \sec^2 x = \int \sin x \sec^2 x dx + C$$

$$y \times \sec^2 x = \int \sec x \tan x dx + C$$

$$y \times \sec^2 x = \sec x + C$$

$$y = \cos x + C \times \cos^2 x$$

117. (D) Triangle with vertices (2, 3), (0, 3) and (2, k)
 Area of the triangle = 2

$$\frac{1}{2} \begin{vmatrix} 2 & 3 & 1 \\ 0 & 3 & 1 \\ 2 & k & 1 \end{vmatrix} = 2$$

$$\begin{vmatrix} 2 & 3 & 1 \\ 0 & 3 & 1 \\ 2 & k & 1 \end{vmatrix} = 4$$

$$2(3-k) - 3(0-2) + 1(0-6) = 4$$

$$6 - 2k + 6 - 6 = 4$$

$$2 = 2k$$

$$k = 1$$

118. (B) Centre of the circle = (4, -3)

and Area = 49π

$$\pi r^2 = 49\pi$$

$$r = 7$$

Equation of the circle

$$(x-4)^2 + (y+3)^2 = (7)^2$$

$$x^2 + 16 - 8x + y^2 + 9 + 6y = 49$$

$$x^2 + y^2 - 8x + 6y - 24 = 0$$

119. (A) Equation of the parabola

$$y^2 = 16x$$

$$4a = 16$$

$$a = 4$$

equation of directrix -

$$x = -a$$

$$x = -4$$

120. (D) Equation of the parabola

$$x^2 + 8x + 2y + 4 = 0$$

$$x^2 + 8x + 16 - 16 + 2y + 4 = 0$$

$$(x+4)^2 = -2y + 12$$

$$(x+4)^2 = -2(y-6)$$

$$X^2 = -2Y \quad \text{where } X = x + 4$$

$$4a = 2$$

$$Y = y - 6$$

$$a = \frac{1}{2}$$

focus of the parabola (X, Y) = (0, -a)

$$X = 0 \quad \text{and } Y = -a$$

$$x + 4 = 0 \quad y - 6 = -\frac{1}{2}$$

$$x = -4 \quad y = \frac{11}{2}$$

focus of the parabola = $\left(-4, \frac{11}{2}\right)$



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NDA (MATHS) MOCK TEST - 74 (Answer Key)

- | | | | | | |
|---------|---------|---------|---------|----------|----------|
| 1. (C) | 21. (D) | 41. (B) | 61. (B) | 81. (C) | 101. (D) |
| 2. (A) | 22. (A) | 42. (C) | 62. (D) | 82. (D) | 102. (B) |
| 3. (C) | 23. (A) | 43. (D) | 63. (D) | 83. (B) | 103. (C) |
| 4. (B) | 24. (A) | 44. (A) | 64. (D) | 84. (A) | 104. (C) |
| 5. (A) | 25. (A) | 45. (B) | 65. (C) | 85. (B) | 105. (B) |
| 6. (A) | 26. (C) | 46. (B) | 66. (C) | 86. (A) | 106. (C) |
| 7. (D) | 27. (C) | 47. (D) | 67. (B) | 87. (B) | 107. (A) |
| 8. (D) | 28. (B) | 48. (D) | 68. (A) | 88. (D) | 108. (B) |
| 9. (C) | 29. (D) | 49. (C) | 69. (C) | 89. (B) | 109. (A) |
| 10. (D) | 30. (C) | 50. (A) | 70. (C) | 90. (C) | 110. (C) |
| 11. (B) | 31. (C) | 51. (C) | 71. (A) | 91. (B) | 111. (C) |
| 12. (B) | 32. (D) | 52. (B) | 72. (C) | 92. (B) | 112. (A) |
| 13. (B) | 33. (A) | 53. (C) | 73. (D) | 93. (A) | 113. (C) |
| 14. (B) | 34. (A) | 54. (D) | 74. (D) | 94. (A) | 114. (A) |
| 15. (B) | 35. (B) | 55. (D) | 75. (B) | 95. (A) | 115. (D) |
| 16. (D) | 36. (D) | 56. (A) | 76. (A) | 96. (C) | 116. (A) |
| 17. (C) | 37. (A) | 57. (A) | 77. (A) | 97. (B) | 117. (D) |
| 18. (A) | 38. (C) | 58. (C) | 78. (A) | 98. (A) | 118. (B) |
| 19. (B) | 39. (A) | 59. (D) | 79. (D) | 99. (B) | 119. (A) |
| 20. (B) | 40. (B) | 60. (D) | 80. (C) | 100. (A) | 120. (D) |

Note : *If your opinion differ regarding any answer, please message the mock test and Question number to 8860330003*

Note : *If you face any problem regarding result or marks scored, please contact : 9313111777*