

## NDA MATHS MOCK TEST - 76 (SOLUTION)

1. (B) Set of odd natural numbers divisible by 2 is null set.

set of even prime number = {2}

{x : x is a natural number  $x < 3$  and  $x > 6$ } is null set.

2. (C)  $\sin 20^\circ \sin 40^\circ \sin 60^\circ \sin 80^\circ$   
 $\Rightarrow \sin 60^\circ [\sin 20^\circ \sin 40^\circ \sin 80^\circ]$

$$\Rightarrow \frac{\sqrt{3}}{2} \left[ \frac{1}{4} \sin(3 \times 20) \right]$$

$$\left[ \because \sin \theta \sin(60 - \theta) \cdot \sin(60 + \theta) = \frac{1}{2} \sin 3\theta \right]$$

$$\Rightarrow \frac{\sqrt{3}}{2} \times \frac{1}{4} \times \frac{\sqrt{3}}{2}$$

$$\Rightarrow \frac{3}{16}$$

3. (D)  $I = \int \frac{1 - \log x}{x^2 \cos^2 \left( \frac{\log x}{x} \right)} dx$

$$\text{Let } \frac{\log x}{x} = t$$

$$\frac{1 - \log x}{x^2} dx = dt$$

$$I = \int \frac{1}{\cos^2 t} dt$$

$$I = \int \sec^2 t dt$$

$$I = \tan t + c$$

$$I = \tan \left( \frac{\log x}{x} \right) + c$$

4. (A) Formula

$$\int \sec x dx = \log(\sec x + \tan x) + c$$

5. (D)  $y = \sqrt{\sin x - \sqrt{\sin x - \sqrt{\sin x ...}}}$

$$y = \sqrt{\sin x - y}$$

on squaring

$$y^2 = \sin x - y$$

$$y^2 + y = \sin x$$

On differentiating both side w.r.t. 'x'

$$2y \frac{dy}{dx} + \frac{dy}{dx} = \cos x$$

$$(2y + 1) \frac{dy}{dx} = \cos x$$

$$\frac{dy}{dx} = \frac{\cos x}{1 + 2y}$$

6. (C)  $y = 2x\sqrt{1-x^2}$

on differencing both side w.r.t 'x'

$$\frac{dy}{dx} = 2 \left[ x \cdot \frac{(-2x)}{2\sqrt{1-x^2}} + \sqrt{1-x^2} \cdot 1 \right]$$

$$\frac{dy}{dx} = 2 \left[ \frac{1-2x^2}{\sqrt{1-x^2}} \right]$$

7. (B)  $\begin{vmatrix} k & a+b & a^2+b^2 \\ k & b+c & b^2+c^2 \\ k & c+a & c^2+a^2 \end{vmatrix} = (a-b)(b-c)(c-a)$

$$\Rightarrow k \begin{vmatrix} 1 & a+b & a^2+b^2 \\ 1 & b+c & b^2+c^2 \\ 1 & c+a & c^2+a^2 \end{vmatrix} = (a-b)(b-c)(c-a)$$

$$R_2 \rightarrow R_2 - R_1, R_3 \rightarrow R_3 - R_1$$

$$\Rightarrow k \begin{vmatrix} 1 & a+b & a^2+b^2 \\ 0 & c-a & c^2-a^2 \\ 0 & c-b & c^2-b^2 \end{vmatrix} = (a-b)(b-c)(c-a)$$

$$\Rightarrow k(c-a)(c-b) \begin{vmatrix} 1 & a+b & a^2+b^2 \\ 0 & 1 & c+a \\ 0 & 1 & c+b \end{vmatrix}$$

$$= (a-b)(b-c)(c-a)$$

$$\Rightarrow -k(c-a)(b-c) \begin{vmatrix} 1 & a+b & a^2+b^2 \\ 0 & 1 & c+a \\ 0 & 1 & c+b \end{vmatrix}$$

$$= (a-b)(b-c)(c-a)$$

$$\Rightarrow -k[1(c+b-c-a)-(a+b)(0)+(a^2+b^2)(0)] = (a-b)$$

$$\Rightarrow -k(b-a) = (a-b)$$

$$\Rightarrow -k(a-b) = (a-b)$$

$$k = 1$$

8. (A) 2-digits number formed from the digits (1, 2, 3, 4, 5, 6, 7, 8, 9)

$$\boxed{9} \boxed{9} = 9 \times 9 = 81$$

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3 digits number less than 500

$$\begin{array}{|c|c|c|} \hline 4 & 9 & 9 \\ \hline \end{array} = 4 \times 9 \times 9 = 324$$

because only {1, 2, 3, 4} can put here.

number formed lying between 10 and 500  
 $= 81 + 324 = 405$

9. (B)

1	1	0	1	0	1	0	1
→	→	→	→	→	→	→	→
$1 \times 2^0 = 1$	$0 \times 2^1 = 0$	$1 \times 2^2 = 4$	$0 \times 2^3 = 0$	$1 \times 2^4 = 16$	$0 \times 2^5 = 0$	$1 \times 2^6 = 64$	$1 \times 2^7 = 128$
213							

$$(11010101)_2 = (213)_{10}$$

0	0	1
0 = 0 × 2 <sup>-1</sup>	0 = 2 × 2 <sup>-2</sup>	1/8 = 1 × 2 <sup>-3</sup>
0.125		

$$(0.001)_2 = (0.125)_{10}$$

then  $(11010101.001)_2 = (213.125)_{10}$

10. (D)  $2^x + 2^y = 2^{x+y}$   
 On differentiating both side w.r.t. 'x'

$$2^x \log 2 + 2^y \log 2 \frac{dy}{dx} = 2^{x+y} \log 2 \left(1 + \frac{dy}{dx}\right)$$

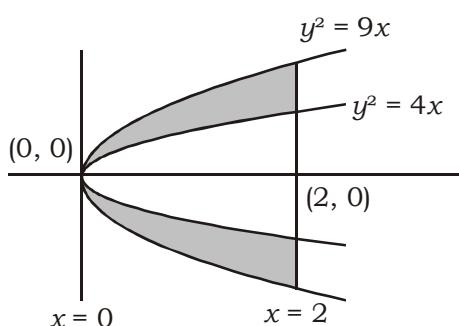
$$(2^y - 2^{x+y}) \frac{dy}{dx} = 2^{x+y} - 2^x$$

$$\frac{dy}{dx} = \frac{2^{x+y} - 2^x}{2^y - 2^{x+y}}$$

$$\frac{dy}{dx} = \frac{2^y}{-2^x} \quad [\text{from equation ...(i)}]$$

$$\frac{dy}{dx} = -2^{y-x}$$

11. (C)



$$\text{Parabolas } y_1 \Rightarrow y = 3\sqrt{x}$$

$$y_2 \Rightarrow y = 2\sqrt{x}$$

and line  $x = 2$

$$\text{Area} \Rightarrow 2 \int_0^2 (y_1 - y_2) dx$$

$$\Rightarrow 2 \int_0^2 (3\sqrt{x} - 2\sqrt{x}) dx$$

$$= 2 \int_0^2 \sqrt{x} dx$$

$$= 2 \times \frac{2}{3} \left[ x^{\frac{3}{2}} \right]_0$$

$$= \frac{4}{3} \left[ 2^{\frac{3}{2}} - 0 \right]$$

$$= \frac{4}{3} \times 2\sqrt{2}$$

$$= \frac{8\sqrt{2}}{3}$$

12. (C)  $S = \{(HHH), (HTT), (HHT), (HTH), (THT), (THH), (TTH), (TTT)\}$

$$n(S) = 8$$

$$E = \{(HHT), (HTH), (THH), (HHH)\}$$

$$n(E) = 4$$

$$P(E) = \frac{n(E)}{n(S)} = \frac{4}{8} = \frac{1}{2}$$

13. (A) Probability of getting first card is an ace

$$= \frac{4}{52}$$

Probability of getting second card without re-

placement is an ace =  $\frac{3}{51}$

$$\text{Required Probability } P(E) = \frac{4}{52} \times \frac{3}{51} = \frac{1}{221}$$

14. (B) Probability of 5 Friday in July =  $\frac{3}{7}$

15. (C) ELEPHANT

LPHNT EEA

as a one letter

$$\text{total arrangement} = \frac{4!}{2!} \times 5! = 1440$$

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16. (D) In expansion of  $\left(\frac{3}{2}x^2 + \frac{1}{4x}\right)^7$

general term

$$T_{r+1} = {}^7C_r \left(\frac{3}{2}x^2\right)^{7-r} \left(\frac{1}{4x}\right)^r$$

$$= {}^7C_r \left(\frac{3}{2}\right)^{7-r} x^{14-3r} \left(\frac{1}{4}\right)^r$$

$$= 14 - 3r = 0$$

$$r = \frac{14}{3}$$

Which is not possible.

Thus, no such term exists in the expansion of the given expression.

17. (B) 
$$\begin{vmatrix} b^2 - ab & b - c & bc - ac \\ ab - a^2 & a - b & b^2 - ab \\ bc - ac & c - a & ab - a^2 \end{vmatrix}$$

$$= \begin{vmatrix} b(b-a) & b - c & c(b-a) \\ a(b-a) & a - b & b(b-a) \\ c(b-a) & c - a & a(b-a) \end{vmatrix}$$

$$= (b-a)(b-a) \begin{vmatrix} b & b - c & c \\ a & a - b & b \\ c & c - a & a \end{vmatrix}$$

$$C_2 \rightarrow C_2 + C_3$$

$$\Rightarrow (b-a)(b-a) \begin{vmatrix} b & b & c \\ a & a & b \\ c & c & a \end{vmatrix}$$

$\Rightarrow 0$  [∴ two columns are identical.]

18. (C) 
$$\begin{vmatrix} a & b & a+b \\ b & a & b+c \\ a-b & c-b & 0 \end{vmatrix}$$

$$C_1 \rightarrow C_1 + C_2$$

$$\Rightarrow \begin{vmatrix} a+b & b & a+b \\ b+c & c & b+c \\ a+c-2b & c-b & 0 \end{vmatrix}$$

$$\Rightarrow \begin{vmatrix} a+b & b & a+b \\ b+c & c & b+c \\ 0 & c-b & 0 \end{vmatrix} \quad [\because a, b, c, \text{are in A.P.}]$$

$\Rightarrow 0$  [∴ two columns are identical.]

19. (B)

20. (C)

$$A = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{bmatrix}$$

$$A = -1 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A = (-1)I$$

21. (A)  $\log_{10} \frac{3}{4} - \log_{10} \frac{10}{3} + \log_{10} \frac{5}{9}$

$$\Rightarrow \log_{10} \left( \frac{\frac{3}{4}}{\frac{10}{3}} \right) + \log_{10} \frac{5}{9} \quad [\because \log m - \log n = \log \frac{m}{n}]$$

$$\Rightarrow \log_{10} \left( \frac{9}{40} \right) + \log_{10} \left( \frac{5}{9} \right)$$

$$\Rightarrow \log_{10} \left( \frac{9}{40} \times \frac{5}{9} \right)$$

$$\Rightarrow \log_{10} \left( \frac{1}{8} \right) = 3 \log 2$$

$$= -3 \times 0.3010 \\ = -0.9030$$

22. (A) General term of G.P.

$$T_n = ar^{n-1}$$

Given that

$$T_7 = ar^6 = 16 \quad \dots(i)$$

$$T_3 = ar^2 = 9 \quad \dots(ii)$$

from equation (i) and equation (ii)

$$ar^6 \times ar^2 = 16 \times 9$$

$$(ar^4)^2 = 144$$

$$ar^4 = 12$$

$$a \times \frac{16}{9} = 12$$

$$a = \frac{27}{4}$$

9th term  $= T_9 = ar^8$

$$= \frac{27}{4} \times \left( \frac{16}{9} \right)^2$$

$$= \frac{64}{3}$$

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23. (B) We know that

$$1^2 + 2^2 + 3^2 + \dots + n^2 = \frac{n}{6} (n+1)(2n+1)$$

then

$$\begin{aligned} & 11^2 + 12^2 + 13^2 + \dots + 20^2 \\ \Rightarrow & (1^2 + 2^2 + 3^2 + \dots + 11^2 + 12^2 + \dots + 20^2) \\ & - (1^2 + 2^2 + 3^2 + \dots + 10^2) \end{aligned}$$

$$\Rightarrow \frac{20}{6} (21) \times (41) - \frac{10}{6} \times (11) \times (21)$$

$$\Rightarrow \frac{21}{6} (20 \times 41 - 10 \times 11)$$

$$\Rightarrow \frac{7}{2} (820 - 110)$$

$$\Rightarrow \frac{7}{2} \times 710$$

$$\Rightarrow 7 \times 710$$

$$\Rightarrow 7 \times 355$$

$$\Rightarrow 2485$$

24. (A)  $x^2 - 8x - 20 \geq 0$

$$(x-10)(x+2) \geq 0$$

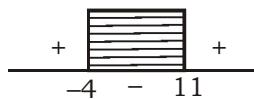
$$x = 10, -2$$



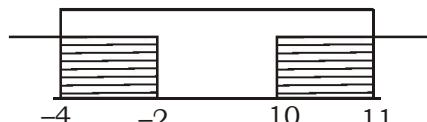
$$\text{and } x^2 - 7x - 44 \leq 0$$

$$(x-11)(x+4) \leq 0$$

$$x = 11, -4$$



general solution



$$x \in [-4, -2] \cup [10, 11]$$

$$-4 \leq x \leq -2 \text{ or } 10 \leq x \leq 11$$

25. (D)  $I = \int \frac{dx}{x^2 + 6x + 13}$

$$= \int \frac{dx}{(x+3)^2 + 4}$$

$$= \int \frac{dx}{(x+3) + (2)^2}$$

$$= \frac{1}{2} \tan^{-1} \left( \frac{x+3}{2} \right) + c$$

$$\left[ \because \int \frac{1}{x^2 + a^2} dx = \frac{1}{a} \tan^{-1} \frac{x}{a} \right]$$

26. (C) A polygon has ( $n = 12$ ) sides

$$\text{then number of diagonals} = \frac{n(n-3)}{2}$$

$$\begin{aligned} & = \frac{12 \times 9}{2} \\ & = 54 \end{aligned}$$

27. (B)  $(2 + 2\omega - 2\omega^2)^{23}$

$$\Rightarrow [2(1 + \omega) - 2\omega^2]^{23} \quad [\because 1 + \omega + \omega^2 = 0]$$

$$\Rightarrow (-4\omega^2)^{23}$$

$$\Rightarrow -4^{23} \omega^{46}$$

$$\Rightarrow -4^{23} \omega$$

$$[\because \omega^3 = 1]$$

28. (B)  $\cos \left[ \cos^{-1} \frac{4}{5} + 2 \tan^{-1} \frac{1}{3} \right]$

$$\Rightarrow \cos \left[ \cos^{-1} \frac{4}{5} + \tan^{-1} \left( \frac{\frac{2}{3}}{1 - \left( \frac{1}{2} \right)^2} \right) \right]$$

$$\left[ \because 2 \tan^{-1} x = \tan^{-1} \frac{2x}{1-x^2} \right]$$

$$\Rightarrow \cos \left[ \cos^{-1} \frac{4}{5} + \tan^{-1} \left( \frac{3}{4} \right) \right]$$

$$\Rightarrow \cos \left[ \tan^{-1} \frac{3}{4} + \tan^{-1} \frac{3}{4} \right]$$

$$\left[ \because \cos^{-1} x = \tan \frac{\sqrt{1-x^2}}{x} \right]$$

$$\Rightarrow \cos \left[ 2 \tan^{-1} \frac{3}{4} \right]$$

$$\Rightarrow \cos \left[ \tan^{-1} \frac{24}{7} \right] \quad [\because 2 \tan^{-1} x = \tan^{-1} \frac{2x}{1-x^2}]$$

$$\Rightarrow \cos \left( \cos^{-1} \frac{7}{25} \right)$$

$$\Rightarrow \frac{7}{25}$$

29. (C)  $\sin (1305)^\circ = \sin (4 \times 360 - 135)$

$$= -\sin 135$$

$$= -\cos 45^\circ$$

$$= -\frac{1}{\sqrt{2}}$$

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$$\begin{aligned}
 30. (A) & \cos 420^\circ \sin 390^\circ + \sin (-300^\circ) \cdot \cos (-330^\circ) \\
 & \Rightarrow \cos (360 + 60) \sin (360 + 30) \\
 & \quad - \sin (360 - 60) \cos (360 - 30) \\
 & \Rightarrow \cos 60 \sin 30 + \sin 60 \cos 30 \\
 & \Rightarrow \cos(30 + 60) \\
 & [\because \sin(A + B) = \sin A \cos B + \cos A \sin B] \\
 & \Rightarrow \sin 90 \\
 & \Rightarrow 1
 \end{aligned}$$

$$\begin{aligned}
 31.(B) \text{ Sphere } & x^2 + y^2 + z^2 - 3x + 6y - z + 8 = 0 \\
 \text{on comparing with general equation} \\
 & x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + k = 0 \\
 u = & \frac{-3}{2}, v = 3, w = \frac{-1}{2} \\
 \text{and plane } & 2x - 4y - 4z + 6 = 0 \\
 a = 2, b = -4, c = -4, d = 6
 \end{aligned}$$

$$\begin{aligned}
 \text{radius of the sphere} &= \sqrt{\frac{|-au - bv - cw + d|}{\sqrt{a^2 + b^2 + c^2}}} \\
 &= \sqrt{\frac{-2 \times \left(\frac{-3}{2}\right) - (-4) \times 3 - (-4) \times \left(\frac{-1}{2}\right) + 6}{\sqrt{(-2)^2 + (-4)^2 + (-4)^2}}} \\
 &= \frac{19}{6}
 \end{aligned}$$

32. (B) given that focus of ellipse = (0, -4) and directrix  $x + 3y + 4 = 0$

$$\text{eccentricity } (e) = \frac{1}{\sqrt{2}}$$

We know that

$$SP = e PM$$

$$\sqrt{(x-0)^2 + (y+4)^2} = \frac{1}{\sqrt{2}} \sqrt{x + 3y + 4}$$

on squaring both side

$$\begin{aligned}
 x^2 + y^2 + 16 + 8y &= \frac{1}{2} \\
 \left[ \frac{x^2 + 9y^2 + 16 + 6xy + 24y + 8x}{10} \right]
 \end{aligned}$$

On solving

$$19x^2 + 11y^2 - 6xy - 8x + 136y + 304 = 0$$

33. (A) Ellipse

$$\frac{(x-3)^2}{25} + \frac{(y-4)^2}{9} = 1$$

$$a^2 = 25, b^2 = 9$$

$$a = 5, b = 3$$

$$\frac{X^2}{25} + \frac{Y^2}{9} = 1 \dots(i) \quad \text{where } X = x - 3$$

$$Y = y - 4$$

parameter of the ellipse ( $a \sin \phi, b \cos \phi$ )

then  $X = a \sin \phi, Y = b \cos \phi$

$$x - 3 = 5 \sin \phi, y - 4 = 3 \cos \phi$$

$$x = 5 \sin \phi + 3, y = 3 \cos \phi + 4$$

The point of the ellipse is  $(5 \sin \phi + 3, 3 \cos \phi + 4)$ .

$$34. (A) 2(1 - e^x) y dy = e^x dx$$

$$2y dy = \frac{e^x}{1 - e^x} dx$$

on integrating

$$2 \int y dy = - \int \frac{(-e^x)}{1 - e^x} dx$$

$$\frac{2y^2}{2} = - \log(1 - e^x) + \log(c)$$

$$y^2 = \log\left(\frac{c}{1 - e^x}\right)$$

$$35. (B) \text{ Mean (A)} = 30, h = 15 - 15 = 10$$

Class Interval	$f_i$	$x_i$	$d_i = \frac{x_i - 30}{10}$	$f_i d_i$	$d_i^2$	$f_i d_i^2$
5-15	8	10	-2	-16	4	32
15-25	12	20	-1	-12	1	12
25-35	15	30	0	0	0	0
35-45	9	40	1	9	1	9
45-55	6	50	2	12	4	24

$$\sum f_i = 56$$

$$\sum f_i d_i = -7$$

$$\sum f_i d_i^2 = 77$$

$$\text{Standard deviation } (\sigma) = h \sqrt{\frac{\sum f_i d_i^2}{\sum f_i} - \left( \frac{\sum f_i d_i}{\sum f_i} \right)^2}$$

$$= 10 \sqrt{\frac{77}{50} - \left( \frac{-7}{50} \right)^2}$$

$$= 10 \sqrt{\frac{77}{50} - \frac{49}{2500}}$$

$$= 10 \sqrt{\frac{3801}{2500}}$$

$$= 12.33$$

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36. (C) Given data 2, 4, 8, 7, 9, 8, 8, 4, 3, 1

$$\text{Mean } \bar{X} = \frac{2+4+8+7+9+8+8+4+3+1}{10}$$

$$= \frac{54}{10} = 5.4$$

$$\text{Mean deviation} = \frac{\sum |X - \bar{X}|}{n}$$

$$\begin{aligned} & |2 - 5.4| + |4 - 5.4| + |8 - 5.4| + |7 - 5.4| + |9 - 5.4| \\ &= \frac{|2 - 5.4| + |4 - 5.4| + |8 - 5.4| + |7 - 5.4| + |9 - 5.4|}{10} \\ &= \frac{3.4 + 1.4 + 2.6 + 1.6 + 3.6 + 2.6 + 2.6 + 1.4 + 2.4 + 4.4}{10} \\ &= \frac{26.0}{10} = 2.6 \end{aligned}$$

37. (A) Straight line  $\frac{x-3}{2} = \frac{y-5}{4} = \frac{z-3}{5}$  is parallel to the plane but perpendicular to its normal.

Then condition

$$a_1 a_2 + b_1 b_2 + c_1 c_2 = 0$$

from option (a) : plane  $4x + 3y - 4z = 0$

$$\begin{aligned} 2 \times 4 + 4 \times 3 - 5 \times 4 &= 0 \\ 8 + 12 - 20 &= 0 \\ 0 &= 0 \end{aligned}$$

Hence plane  $4x + 3y - 4z = 0$  is parallel to the straight line.

38. (A) Centre C(3, -1, 2) and point P(4, 2, 4)

$$\begin{aligned} \text{radius} &= \sqrt{(4-3)^2 + (2+1)^2 + (4-2)^2} \\ &= \sqrt{1+9+4} \\ &= \sqrt{14} \end{aligned}$$

equation of the sphere

$$\begin{aligned} (x-3)^2 + (y+1)^2 + (z-2)^2 &= (\sqrt{14})^2 \\ x^2 + 9 - 6x + y^2 + 1 + 2y + z^2 + 4 - 4z &= 14 \\ x^2 + y^2 + z^2 - 6x + 2y - 4z &= 0 \end{aligned}$$

39. (C)  $(x+1)^2 = 4(y-3)$

$$\begin{aligned} X^2 &= 4Y & \text{where } X = x+1 \\ 4a &= 4 & Y = y-3 \\ a &= 1 \end{aligned}$$

equation of directrix

$$\begin{aligned} Y &= -a \\ y-3 &= -1 \\ y &= 2 \end{aligned}$$

40. (B) Given that  $x = 8 \sec \theta, y = 4 \tan \theta$

$$\sec \theta = \frac{x}{8}, \tan \theta = \frac{y}{4}$$

$$\sec^2 \theta - \tan^2 \theta = \frac{x^2}{64} - \frac{y^2}{16}$$

$$1 = \frac{x^2}{64} - \frac{y^2}{16}$$

$$\frac{x^2}{64} - \frac{y^2}{16} = 1$$

$$a = 8, b = 4$$

$$e = \sqrt{1 + \frac{b^2}{a^2}}$$

$$e = \sqrt{1 + \frac{16}{64}}$$

$$e = \frac{\sqrt{5}}{2}$$

$$\text{distance between the directrices} = \frac{2a}{e}$$

$$= \frac{2 \times 8}{\sqrt{5}} \times 2$$

$$= \frac{32}{\sqrt{5}}$$

$$41. (D) I = \int_0^{\frac{\pi}{2}} \cos x \cdot \sin^2 x \, dx$$

$$\text{Let } \sin x = t \quad \text{when } x \rightarrow 0, t \rightarrow 0$$

$$\cos x \, dx = dt \quad x \rightarrow \frac{\pi}{2}, t \rightarrow 1$$

$$I = \int_0^1 t^7 \, dt$$

$$= \left[ \frac{t^8}{8} \right]_0^1$$

$$= \frac{1}{8} - 0 = \frac{1}{8}$$

$$42. (B) P = \int e^x \cos x \, dx \text{ and } Q = \int e^x \sin x \, dx$$

$$\frac{dP}{dx} = e^x \cos x \text{ and } \frac{dQ}{dx} = e^x \sin x$$

$$P + Q = \int e^x \cos x \, dx + \int e^x \sin x \, dx$$

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$$\begin{aligned}
 &= e^x \cdot \int \cos x dx - \int \left\{ \frac{d}{dx}(e^x) \cdot \int \cos x dx \right\} dx \\
 &\quad + \int e^x \sin x dx + c \\
 &= e^x \cdot \sin x - \int e^x \sin x dx + \int e^x \sin x dx + c \\
 P + Q &= e^x \cdot \sin x + c
 \end{aligned}$$

$$P + Q = \frac{dQ}{dx} + c$$

43. (D)  $I = \int \left[ \operatorname{cosech}^2 x + \frac{x^5 (\tan^{-1} x^6)}{(1+x^{12})} \right] dx$

let  $\tan^{-1} x^6 = t$

$$\frac{1}{1+x^{12}} \cdot 6x^5 dx = dt$$

$$\frac{x^5}{1+x^{12}} dx = \frac{1}{6} dt$$

$$I = \coth x + \frac{1}{6} \int t dt$$

$$= \coth x + \frac{1}{6} \times \frac{t^2}{2} + c$$

$$= \coth x + \frac{1}{12} (\tan^{-1} x^6)^2 + c$$

44. (C)  $I = \int e^{\log x \cos x} dx$

$$I = \int x \cos x dx$$

$$I = x \cdot \int \cos x dx - \int \left\{ \frac{d}{dx}(x) \cdot \int \cos x dx \right\} dx + c$$

$$I = x \sin x - \int 1 \cdot \sin x dx + c$$

$$I = x \sin x + \cos x + c$$

45. (C)  $I = \int_1^e (\log x)^2 dx$

Let  $\log x = t \Rightarrow x = e^t$  when  $x \rightarrow 1, t \rightarrow 0$

$$\frac{1}{x} dx = dt \quad x \rightarrow e, t \rightarrow 1$$

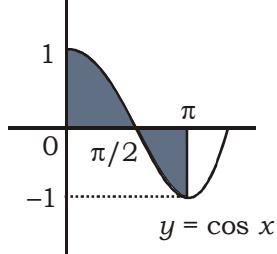
$$dx = x dt$$

$$dx = e^t dt$$

$$I = \int_0^1 t^2 \cdot e^t dt$$

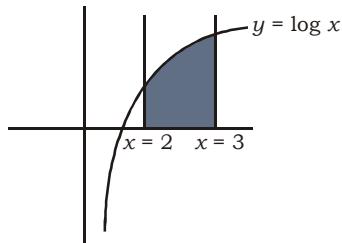
$$\begin{aligned}
 &= \left[ t^2 \int e^t dt - \int \left\{ \frac{d}{dt}(t^2) \cdot \int e^t dt \right\} dt \right]_0^1 \\
 &= \left[ t^2 \cdot e^t - \int 2t \cdot e^t dt \right]_0^1 \\
 &= \left[ t^2 \cdot e^t - 2 \left\{ t \int e^t dt - \int \left\{ \frac{d}{dt}(t) \int e^t dt \right\} dt \right\} \right]_0^1 \\
 &= \left[ t^2 e^t - 2te^t + 2 \int 1 \cdot e^t dt \right]_0^1 \\
 &= \left[ t^2 e^t - 2t \cdot e^t + 2e^t \right]_0^1 \\
 &= e - 2 \times 1 \times e + 2 \cdot e - 0 + 0 - 2e^0 \\
 &= e - 2
 \end{aligned}$$

46. (A)



$$\begin{aligned}
 \text{Area} &= \int_0^{\pi/2} y dx + \int_{\pi/2}^{\pi} (-y) dx \\
 &= \int_0^{\pi/2} \cos x dx - \int_{\pi/2}^{\pi} \cos x dx \\
 &= [\sin x]_0^{\pi/2} - [\sin x]_{\pi/2}^{\pi} \\
 &= \left( \sin \frac{\pi}{2} - \sin 0 \right) - \left( \sin \pi - \sin \frac{\pi}{2} \right) \\
 &= (1 - 0) - (0 - 1) \\
 &= 1 + 1 \\
 &= 2 \text{ square unit}
 \end{aligned}$$

47. (D)



$$y = \log x$$

$$\text{Area} = \int_2^3 y dx$$

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$$\begin{aligned}
 &= \int_2^3 \log x \, dx \\
 &= \left[ \log x \int 1 \cdot dx - \int \left\{ \frac{d}{dx}(\log x) \cdot \int 1 \cdot dx \right\} dx \right]_2^3 \\
 &= \left[ x \log x - \int \frac{1}{x} \cdot x \, dx \right]_2^3 \\
 &= [x \log x - x]_2^3 \\
 &= (3 \log 3 - 3) - (2 \log 2 - 2) \\
 &= 3 \log 3 - 3 - 2 \log 2 + 2 \\
 &= \log 27 - \log 4 - 1 \\
 &= \log \left( \frac{27}{4} \right) - 1
 \end{aligned}$$

48. (A)  $\frac{dy}{dx} + y \left( \tan x + \frac{1}{x} \right) = \frac{1}{x} \sec x$

On comparing with general equation

$$\frac{dy}{dx} + Py = Q$$

$$P = \tan x + \frac{1}{x}, Q = \frac{1}{x} \sec x$$

$$I.F. = e^{\int P dx}$$

$$= e^{\int \left( \tan x + \frac{1}{x} \right) dx}$$

$$I.F. = e^{(\log \sec x + \log x)}$$

$$\begin{aligned}
 I.F. &= e^{\log(x \cdot \sec x)} \\
 &= x \cdot \sec x
 \end{aligned}$$

Solution of the differential equation

$$y \times I.F. = \int Q \times I.F. \, dx$$

$$y \times x \cdot \sec x = \int \frac{1}{x} \sec x \times x \sec x \, dx$$

$$xy \sec x = \int \sec^2 x \, dx$$

$$xy \sec x = \tan x + c$$

$$xy = \sin x + c \cdot \cos x$$

49. (C) Eccentricity  $e = 2\sqrt{2}$

and distance between foci =  $2ae = 16$

$$2a \times 2\sqrt{2} = 16$$

$$a = \frac{4}{\sqrt{2}}$$

$$a^2 = 8$$

then

$$e^2 = 1 + \frac{b^2}{a^2}$$

$$8 = 1 + \frac{b^2}{8}$$

$$7 = \frac{b^2}{8}$$

$$b^2 = 56$$

equation of hyperbola

$$\begin{aligned}
 \frac{x^2}{8} - \frac{y^2}{56} &= 1 \\
 7x^2 - y^2 &= 56
 \end{aligned}$$

50. (D) parabola

$$(y+4)^2 = 8(x-2)$$

$$Y^2 = 8X$$

where  $X = x - 2$

$$4a = 8$$

$$Y = y + 4$$

$$a = 2$$

Focus of parabola  $(X, Y) = (a, 0)$

$$X = a \quad Y = 0$$

$$x - 2 = 2 \quad y + 4 = 0$$

$$x = 4 \quad y = -4$$

focus of parabola =  $(4, -4)$

51. (B) Differential equation

$$x \, dy - y \, dx = yx^2 \, dy$$

$$\frac{x \, dy - y \, dx}{x^2} = y \, dy$$

$$d\left(\frac{y}{x}\right) = y \, dy$$

On integrating

$$\frac{y}{x} = \frac{y^2}{2} + c$$

$$2y = xy^2 + 2cx$$

52. (A)  $I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{dx}{1 + \sqrt{\cot x}}$

$$I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} \quad \dots(i)$$

$$I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{\sqrt{\cos x}}{\sqrt{\cos x} + \sqrt{\sin x}} \quad \dots(ii)$$

$$\left[ \because \int_a^b f(x) \, dx = \int_a^b f(a+b-x) \, dx \right]$$

From equation (i) and (ii)

$$2I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} 1 \cdot dx$$

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$$2I = \left[ x \right]_{\frac{\pi}{6}}^{\frac{\pi}{3}}$$

$$2I = \frac{\pi}{3} - \frac{\pi}{6}$$

$$2I = \frac{\pi}{6}$$

$$I = \frac{\pi}{12}$$

53. (B)  $(x+y)(dx+dy) = dx - dy$   
 $(x+y)dx + (x+y)dy = dx - dy$   
 $(x+y+1)dy = (1-x-y)dx$

$$\frac{dy}{dx} = \frac{1-x-y}{x+y+1} \quad \dots(i)$$

$$\text{Let } x+y=t$$

$$1 + \frac{dy}{dx} = \frac{dt}{dx}$$

$$\frac{dy}{dx} = \frac{dt}{dx} - 1$$

from equation (i)

$$\frac{dt}{dx} - 1 = \frac{1-t}{1+t}$$

$$\frac{dt}{dx} = \frac{2}{1+t}$$

$$(1+t)dt = 2dx$$

On integrating

$$t + \frac{t^2}{2} = 2x + \frac{C}{2}$$

$$2t + t^2 = 4x + C$$

$$2(x+y) + (x+y)^2 = 4x + C$$

$$(x+y)^2 = 2x - 2y + C$$

54. (A)  $I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{3^{\tan x}}{3^{\tan x} + 3^{\cot x}} dx \quad \dots(i)$

$$I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{3^{\cot x}}{3^{\tan x} + 3^{\cot x}} dx \quad \dots(ii)$$

$$\left[ \because \int_a^b f(x) dx = \int_a^b f(a+b-x) dx \right]$$

On adding equation (i) and (ii)

$$2I = \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} 1 . dx$$

$$2I = \left[ x \right]_{\frac{\pi}{6}}^{\frac{\pi}{3}}$$

$$2I = \frac{\pi}{3} - \frac{\pi}{6}$$

$$2I = \frac{\pi}{6} \Rightarrow I = \frac{\pi}{12}$$

55. (C)  $y = \log(x + \sqrt{1+x^2})$

on differentiating both side w.r.t. 'x'

$$\frac{dy}{dx} = \frac{1}{x + \sqrt{1+x^2}} \left[ 1 + \frac{1}{2\sqrt{1+x^2}}(2x) \right]$$

$$\frac{dy}{dx} = \frac{1}{x + \sqrt{1+x^2}} \left[ \frac{\sqrt{1+x^2} + x}{\sqrt{1+x^2}} \right]$$

$$\frac{dy}{dx} = \frac{1}{\sqrt{1+x^2}}$$

again, differentiating both side w.r.t. 'x'

$$\frac{d^2y}{dx^2} = \frac{-1}{2} (1+x^2)^{-\frac{3}{2}} (2x)$$

$$\frac{d^2y}{dx^2} = \frac{-x}{(1+x^2)^{\frac{3}{2}}}$$

56. (B) L.H.L =  $\lim_{x \rightarrow 2^-} \frac{(x-2)^2}{|x-2|} = \lim_{h \rightarrow 0} \frac{(2-h-2)^2}{|2-h-2|}$

$$= \lim_{h \rightarrow 0} \frac{h^2}{h}$$

$$= \lim_{h \rightarrow 0} h = 0$$

R.H.L =  $\lim_{x \rightarrow 2^+} \frac{(x-2)^2}{|x-2|} = \lim_{h \rightarrow 0} \frac{(2+h-2)^2}{|2+h-2|}$

$$= \lim_{h \rightarrow 0} \frac{h^2}{h}$$

$$= 0$$

L.H.L. = R.H.L. = 0

Hence  $\lim_{x \rightarrow 2} \frac{(x-2)^2}{|x-2|} = 0$

57. (A)  $\lim_{x \rightarrow 0} \frac{a^{\sin x} - a^{\tan x}}{\tan\left(\frac{\pi}{4} - x\right) - \cot\left(\frac{\pi}{4} - x\right)} \begin{bmatrix} 0 \\ 0 \end{bmatrix}$  form

by L-hospital's rule

$$\Rightarrow \lim_{x \rightarrow 0} \frac{a^{\sin x} \cdot \log a \cdot \cos x - a^{\tan x} \cdot \log a \cdot \sec^2 x}{-\sec^2\left(\frac{\pi}{4} - x\right) + \left(-\operatorname{cosec}^2\left(\frac{\pi}{4} - x\right)\right)}$$

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$$\Rightarrow \lim_{x \rightarrow 0} \frac{\log a(a^{\sin x} \cdot \cos x - a^{\tan x} \cdot \sec^2 x)}{-\sec^2\left(\frac{\pi}{4} - x\right) - \operatorname{cosec}^2\left(\frac{\pi}{4} - x\right)}$$

$$\Rightarrow \frac{\log a(a^{\sin 0} \cdot \cos 0 - a^{\tan 0} \cdot \sec^2 0)}{-\sec^2 \frac{\pi}{4} - \operatorname{cosec}^2 \frac{\pi}{4}}$$

$$= 0$$

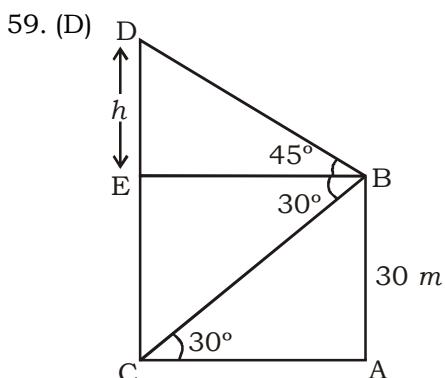
58. (B)  $\lim_{x \rightarrow \infty} \left( \frac{x+5}{x+2} \right)^{x+3}$

$$= \lim_{x \rightarrow \infty} \left( 1 + \frac{3}{x+2} \right)^{\frac{x+2}{3} \times \frac{(x+3) \times 3}{x+2}}$$

$$= \lim_{x \rightarrow \infty} \left[ \left( 1 + \frac{3}{x+2} \right)^{\frac{x+2}{3}} \right]^{\frac{3(1+\frac{3}{x})}{(1+\frac{2}{x})}}$$

$$= e^{3 \lim_{x \rightarrow \infty} \frac{(1+\frac{3}{x})}{(1+\frac{2}{x})}}$$

$$= e^3$$



Let DE =  $h$  m

**In  $\triangle BED$**

$$\tan 45^\circ = \frac{DE}{BE} = \frac{h}{BE}$$

$$1 = \frac{h}{BE}$$

$$BE = h$$

**In  $\triangle ABC$**

$$\tan 30^\circ = \frac{AB}{AC} = \frac{AB}{BE}$$

$$\frac{1}{\sqrt{3}} = \frac{30}{h}$$

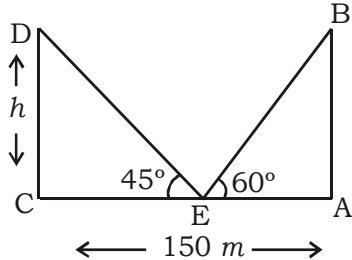
$$h = 30\sqrt{3}$$

height of the tower = CD = CE + DE

$$= 30 + 30\sqrt{3}$$

$$= 30(\sqrt{3} + 1) \text{ m}$$

60. (C)



Let height of pole =  $h$  m = CD = AB

**In  $\triangle DCE$**

$$\tan 45^\circ = \frac{CD}{CE} = \frac{h}{CE}$$

$$CE = h$$

$$\text{then } AE = (150 - h) \text{ m}$$

**In  $\triangle ABE$**

$$\tan 60^\circ = \frac{AB}{AE}$$

$$\sqrt{3} = \frac{h}{150 - h}$$

$$150\sqrt{3} - h\sqrt{3} = h$$

$$150\sqrt{3} = h(\sqrt{3} + 1)$$

$$h = \frac{150\sqrt{3}}{\sqrt{3} + 1} = 75(3 - \sqrt{3})$$

61. (C)  $\cos^{-1} x + \tan^{-1} \left( \frac{1}{3} \right) = \frac{\pi}{2}$

$$\cos^{-1} x = \frac{\pi}{2} - \tan^{-1} \left( \frac{1}{3} \right)$$

$$\cos^{-1} x = \cot^{-1} \left( \frac{1}{3} \right)$$

$$\cos^{-1} x = \tan^{-1} (3)$$

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$$\cos^{-1} x = \cos^{-1} \frac{1}{\sqrt{10}}$$

$$\left[ \because \tan^{-1} x = \cos^{-1} \frac{1}{\sqrt{1+x^2}} \right]$$

$$x = \frac{1}{\sqrt{10}}$$

$$62. (B) \tan \left[ \frac{\pi}{4} - \frac{1}{2} \cos^{-1} \frac{x}{y} \right] + \tan \left[ \frac{\pi}{4} + \frac{1}{2} \cos^{-1} \frac{x}{y} \right]$$

$$\text{Let } \frac{1}{2} \cos^{-1} \frac{x}{y} = \theta$$

$$\frac{x}{y} = \cos 2\theta$$

$$\Rightarrow \tan \left[ \frac{\pi}{4} - \theta \right] + \tan \left[ \frac{\pi}{4} - \theta \right]$$

$$\Rightarrow \frac{1 - \tan \theta}{1 + \tan \theta} + \frac{1 + \tan \theta}{1 - \tan \theta}$$

$$\Rightarrow \frac{1 + \tan^2 \theta - 2 \tan \theta + 1 + \tan^2 \theta + 2 \tan \theta}{1 - \tan^2 \theta}$$

$$\Rightarrow \frac{2 \sec^2 \theta}{\frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta}}$$

$$\Rightarrow \frac{2}{\cos 2\theta}$$

$$\Rightarrow \frac{2y}{x}$$

63. (C) Given that A = {3, 4, 5, 6} and B = {4, 5}  
 $(A \times B) = \{(3, 4), (3, 5), (4, 4), (4, 5), (5, 4), (5, 5), (6, 4), (6, 5)\}$   
 $(B \times A) = \{(4, 3), (4, 4), (4, 5), (4, 6), (5, 3), (5, 4), (5, 5), (5, 6)\}$   
 $(A \times B) \cap (B \times A) = \{(4, 4), (4, 5), (5, 4), (5, 5)\}$

$$64. (D) \frac{x\omega^9 + y\omega^{13} + z\omega^{17}}{y + z\omega^7 + x\omega^5}$$

$$\Rightarrow \frac{x + y\omega + z\omega^2}{y + z\omega + x\omega^2}$$

$$\Rightarrow \frac{\omega(x + y\omega + z\omega^2)}{\omega(y + z\omega + x\omega^2)}$$

$$\Rightarrow \frac{\omega(x + y\omega + z\omega^2)}{(y\omega + z\omega^2 + x\omega^3)}$$

$$\Rightarrow \frac{\omega(x + y\omega + z\omega^2)}{(x + y\omega + z\omega^2)}$$

$$\Rightarrow \omega$$

$$65. (A) 0.4\overline{35} = \frac{435 - 4}{990} = \frac{431}{990}$$

$$66. (B) A = \begin{bmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ 1+x^2 & 1+y^2 & 1+z^2 \end{bmatrix}$$

$$|A| = \begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ 1+x^2 & 1+y^2 & 1+z^2 \end{vmatrix}$$

$$= \begin{vmatrix} x & y & z \\ x^2 & y^2 & z \\ 1 & 1 & 1 \end{vmatrix} + \begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ x^2 & y^2 & z^2 \end{vmatrix}$$

$$= \begin{vmatrix} x & y & z \\ x^2 & y^2 & z^2 \\ 1 & 1 & 1 \end{vmatrix} + 0 \quad (\because \text{two Rows are identical})$$

$$C_2 \rightarrow C_2 - C_1, C_3 \rightarrow C_3 - C_1$$

$$= \begin{vmatrix} x & y-x & z-x \\ x^2 & y^2-x^2 & z^2-x^2 \\ 1 & 0 & 0 \end{vmatrix}$$

$$= (y-x)(z-x) \begin{vmatrix} x & 1 & 1 \\ x^2 & y+x & z+x \\ 1 & 0 & 0 \end{vmatrix}$$

$$C_3 \rightarrow C_3 - C_2$$

$$= (y-x)(z-x) \begin{vmatrix} x & 1 & 0 \\ x^2 & y+x & z-y \\ 1 & 0 & 0 \end{vmatrix}$$

$$= (y-x)(z-x) [x \times 0 - 1(-(z-y) + 0)]$$

$$= (y-x)(z-x)(z-y)$$

$$= (x-y)(y-z)(z-x)$$

$$67. (C) \cos 36^\circ \cos 72^\circ \cos 108^\circ \cos 144^\circ$$

$$\Rightarrow \cos 36^\circ \cdot \cos 72^\circ \cos(180 - 72)^\circ \cos(180 - 36)^\circ$$

$$\Rightarrow \cos 36^\circ \cdot \cos 72^\circ (-\cos 72)^\circ (-\cos 36)^\circ$$

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$$\Rightarrow \cos 36^\circ \cdot \cos^2 72^\circ$$

$$\Rightarrow (\cos 36^\circ)^2 \cdot (\sin 18^\circ)^2$$

$$\Rightarrow \left( \frac{\sqrt{5}+1}{4} \right)^2 \left( \frac{\sqrt{5}-1}{4} \right)^2$$

$$\Rightarrow \left[ \frac{(\sqrt{5}+1)(\sqrt{5}-1)}{16} \right]^2$$

$$\Rightarrow \left[ \frac{4}{16} \right]^2$$

$$\Rightarrow \frac{1}{16}$$

$$68. (B) \tan 9^\circ - \tan 27^\circ - \tan 63^\circ + \tan 81^\circ$$

$$\Rightarrow \cot 81^\circ - \cot 63^\circ - \tan 63^\circ + \tan 81^\circ$$

$$\Rightarrow (\tan 81^\circ + \cot 81^\circ) - (\tan 63^\circ + \cot 63^\circ)$$

$$= \frac{\sin^2 81^\circ + \cos^2 81^\circ}{\sin 81^\circ \cdot \cos 81^\circ} - \frac{\sin^2 63^\circ + \cos^2 63^\circ}{\sin 63^\circ \cdot \cos 63^\circ}$$

$$= \frac{2 \times 1}{2 \sin 81^\circ \cdot \cos 81^\circ} - \frac{2 \times 1}{2 \sin 63^\circ \cdot \cos 63^\circ}$$

$$= \frac{2}{\sin 162^\circ} - \frac{2}{\sin 126^\circ}$$

$$= \frac{2}{\sin 18^\circ} - \frac{2}{\cos 36^\circ}$$

$$= \frac{2}{\frac{\sqrt{5}-1}{4}} - \frac{2}{\frac{\sqrt{5}+1}{4}}$$

$$= \frac{8}{\sqrt{5}-1} - \frac{8}{\sqrt{5}+1}$$

$$= 8 \left[ \frac{2}{4} \right]$$

$$= 4$$

$$69. (C) \lim_{x \rightarrow \infty} x^{\frac{3}{2}} \left( \sqrt{x^3+1} - \sqrt{x^3-1} \right)$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{x^{\frac{3}{2}} \left( \sqrt{x^3+1} - \sqrt{x^3-1} \right)}{\left( \sqrt{x^3+1} + \sqrt{x^3-1} \right)} \times \left( \sqrt{x^3+1} + \sqrt{x^3-1} \right)$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{x^{\frac{3}{2}} (x^3+1 - x^3+1)}{\sqrt{x^3+1} + \sqrt{x^3-1}}$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{2x^{\frac{3}{2}}}{\sqrt{1+\frac{1}{x^3}} + \sqrt{1-\frac{1}{x^3}}}$$

$$= \frac{2}{\sqrt{1+0} + \sqrt{1-0}}$$

$$= \frac{2}{2} = 1$$

$$70. (B) y = a \sin (\log x) - b \cos (\log x) \quad \dots(i)$$

On differentiating both side w.r.t 'x'

$$\frac{dy}{dx} = a \cos (\log x) \times \frac{1}{x} + b \sin (\log x) \times \frac{1}{x}$$

$$x \frac{dy}{dx} = a \cos (\log x) + b \sin (\log x) \quad \dots(ii)$$

again, differentiating both side w.r.t. 'x'

$$x \cdot \frac{d^2y}{dx^2} + \frac{dy}{dx} \cdot 1 = -a \sin (\log x) \times \frac{1}{x} + b \cos$$

$$(\log x) \times \frac{1}{x}$$

$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} = -[a \sin (\log x) - b \cos (\log x)]$$

$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} = -y$$

$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} + y = 0$$

$$71. (C) y = \frac{\log x}{x}$$

on differentiating both side w.r.t 'x'

$$\frac{dy}{dx} = \frac{x \cdot \frac{1}{x} - \log x \cdot 1}{x^2}$$

$$\frac{dy}{dx} = \frac{1 - \log x}{x^2}$$

again, differentiating both side w.r.t. 'x'

$$\frac{d^2y}{dx^2} = \frac{x^2 \left( 0 - \frac{1}{x} \right) - (1 - \log x) \times 2x}{(x^2)^2}$$

$$\frac{d^2y}{dx^2} = \frac{x(2 \log x - 3)}{x^4}$$

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$$\frac{d^2y}{dx^2} = \frac{(2\log x - 3)}{x^3}$$

$$72. (D) f(x) = \begin{cases} \frac{\sin x + x \cos x}{x}, & \text{if } x \neq 0 \\ k, & \text{if } x = 0 \end{cases}$$

is continuous at  $x = 0$   
then

$$\text{L.H.L} = \text{R.H.L.} = f(0)$$

$$\text{L.H.L} = \lim_{x \rightarrow 0^-} f(x) = f(0)$$

$$\lim_{x \rightarrow 0} \frac{\sin x + x \cos x}{x} = k$$

by L-Hospital's Rule

$$\lim_{x \rightarrow 0} \frac{\cos x + x(-\sin x) + \cos x \cdot 1}{1} = k$$

$$\cos 0 + 0 + \cos 0 = k \\ k = 2$$

$$73. (A) I = \int \frac{x^2 + 1}{(x^2 + 4)(x^2 + 25)} dx$$

$$I = \int \left[ \frac{8}{7} \frac{1}{x^2 + 25} - \frac{1}{7} \frac{1}{x^2 + 4} \right] dx$$

$$I = \left[ \frac{8}{7} \times \frac{1}{5} \tan^{-1} \frac{x}{5} - \frac{1}{7} \times \frac{1}{2} \tan^{-1} \frac{x}{2} \right] + c$$

$$I = \frac{8}{35} \tan^{-1} \frac{x}{5} - \frac{1}{14} \tan^{-1} \frac{x}{2} + c$$

$$74. (C) I = \int \left\{ \frac{1}{\log x} - \frac{1}{(\log x)^2} \right\} dx$$

Let  $\log x = t \Rightarrow x = e^t$

$$\frac{1}{x} dx = dt$$

$$dx = x dt \\ dx = e^t dt$$

$$I = \int \left( \frac{1}{t} - \frac{1}{t^2} \right) e^t dt$$

$$I = e^t \cdot \frac{1}{t} + c$$

$$\left[ \because \int e^x [f(x) + f'(x)] dx = e^x \cdot f(x) \right]$$

$$I = \frac{x}{\log x} + c$$

$$75. (C) I = \int_2^3 \frac{\sqrt{5-x}}{\sqrt{x} + \sqrt{5-x}} dx \quad \dots(i)$$

$$I = \int_2^3 \frac{\sqrt{x}}{\sqrt{5-x} + \sqrt{x}} dx \quad \dots(ii)$$

$$\left[ \because \int_a^b f(x) dx = \int_a^b f(a+b-x) dx \right]$$

On adding equation (i) and equation (ii)

$$2I = \int_2^3 1 dx$$

$$2I = [x]_2^3$$

$$2I = 3 - 2$$

$$I = \frac{1}{2}$$

$$76. (D) I = \int_{0.2}^{3.5} [x] dx \text{ where } [.] \text{ is greatest integer.}$$

$$I = \int_{0.2}^1 [x] dx + \int_1^2 [x] dx + \int_2^3 [x] dx + \int_3^{3.5} [x] dx$$

$$I = \int_{0.2}^1 0 dx + \int_1^2 1 dx + \int_2^3 2 dx + \int_3^{3.5} 3 dx$$

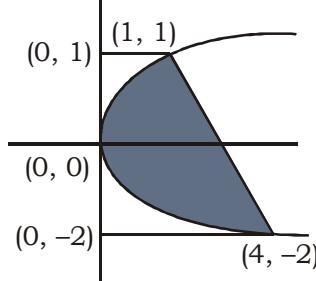
$$I = 0 + (x)_1^2 + 2(x)_2^3 + 3(x)_3^{3.5}$$

$$I = (2-1) + 2(3-2) + 3(3.5-3)$$

$$= 1 + 2 + 3 \times \frac{1}{2}$$

$$I = 4.5$$

77. (B)



Parabola  $y^2 = x$

$$x_1 \Rightarrow x = y^2 \quad \dots(i)$$

$$\text{and line } x_2 \Rightarrow x = 2 - y \quad \dots(ii)$$

On solving equation (i) and equation (ii)

$$x = 1, x = 4$$

$$y = 1, y = -2$$

$$\text{Area} = \left| \int_{-2}^1 (x_1 - x_2) dx \right|$$

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$$\begin{aligned}
 &= \left| \int_{-2}^1 (y^2 - 2 + y) dx \right| \\
 &= \left| \left[ \frac{y^3}{3} - 2y + \frac{y^2}{2} \right]_{-2}^1 \right| \\
 &= \left| \left( \frac{1}{3} - 2 + \frac{1}{2} \right) - \left( -\frac{8}{3} + 4 + 2 \right) \right| \\
 &= \left| \frac{-7}{6} - \left( \frac{10}{3} \right) \right| \\
 &= \left| \frac{-27}{6} \right| \\
 &= \frac{9}{2}
 \end{aligned}$$

78. (B)  $f(x) = \frac{1}{\sqrt{x+|x|}}$

$x+|x| > 0$   
 $|x| > -x$   
 $x > 0$

Domain of the function =  $R^+$

79. (D) Given  $f(x) = \frac{5x+3}{4x-5}$

$$\begin{aligned}
 f[f(x)] &= f\left[\frac{5x+3}{4x-5}\right] \\
 &= \frac{5\left(\frac{5x+3}{4x-5}\right) + 3}{4\left(\frac{5x+3}{4x-5}\right) - 5} \\
 &= \frac{25x+15+12x-15}{20x+12-20x+25} \\
 &= \frac{37x}{37}
 \end{aligned}$$

$f[f(x)] = x$

80. (A)  $R_1 = \{(1, a), (1, b), (1, c)\}$   
 $R_2 = \{(1, c), (2, b), (2, a)\}$

81. (D) Given that

$$5f(x) + 3f\left(\frac{1}{x}\right) = \frac{1}{x} + 7 \quad \dots(i)$$

on putting  $x = \frac{1}{x}$

$$5f\left(\frac{1}{x}\right) + 3f(x) = x + 7 \quad \dots(ii)$$

On solving equation (i) and equation (ii)

$$25f(x) - 9f(x) = \frac{5}{x} + 35 - 3x - 21$$

$$16f(x) = \frac{5}{x} - 3x + 14$$

On putting  $x = 1$

$$16f(1) = 5 - 3 + 14$$

$$16f(1) = 16$$

$$f(1) = 1$$

82. (B)

$$\begin{vmatrix} y & x & y+z \\ z & y & x+y \\ x & z & z+x \end{vmatrix}$$

$$R_1 \rightarrow R_1 + R_2 + R_3$$

$$= \begin{vmatrix} x+y+z & x+y+z & 2(x+y+z) \\ z & y & x+y \\ x & z & z+x \end{vmatrix}$$

$$= (x+y+z) \begin{vmatrix} 1 & 1 & 2 \\ z & y & x+y \\ x & z & z+x \end{vmatrix}$$

$$C_1 \rightarrow C_1 - C_2, C_3 \rightarrow C_3 - 2C_2$$

$$= (x+y+z) \begin{vmatrix} 0 & 1 & 0 \\ z-y & y & x-y \\ x-z & z & x-z \end{vmatrix}$$

$$\begin{aligned}
 &= (x+y+z) [0 - 1 \{(z-y)(x-z) - (x-z)(x-y)\} + 6] \\
 &= -(x+y+z) [xz - z^2 - xy + yz - x^2 + xy + xz - yz] \\
 &= (x+y+z) (x^2 + z^2 - 2xz) \\
 &= (x+y+z) (x-z)^2
 \end{aligned}$$

83. (B)  $\tan\left(7\frac{1}{2}\right)^\circ = \frac{2 \sin^2\left(7\frac{1}{2}\right)^\circ}{2 \sin\left(7\frac{1}{2}\right)^\circ \cos\left(7\frac{1}{2}\right)^\circ}$

$$= \frac{1 - \cos 15^\circ}{\sin 15^\circ}$$

$$= \frac{1 - \frac{\sqrt{3} + 1}{2\sqrt{2}}}{\frac{\sqrt{3} - 1}{2\sqrt{2}}}$$

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$$\begin{aligned}
 &= \frac{2\sqrt{2} - \sqrt{3} - 1}{\sqrt{3} - 1} \times \frac{\sqrt{3} + 1}{\sqrt{3} + 1} \\
 &= \frac{2\sqrt{6} - 3 - \sqrt{3} + 2\sqrt{2} - \sqrt{3} - 1}{2} \\
 &= \frac{2\sqrt{6} - 2\sqrt{3} + 2\sqrt{2} - 4}{2} \\
 &= \sqrt{6} - \sqrt{3} + \sqrt{2} - 2
 \end{aligned}$$

84. (B)  $f(x) = \sin^{-1} \left( \log_3 \frac{x}{4} \right)$

We know that domain of  $\sin^{-1} x = x \in [-1, 1]$

$$-1 \leq \log_3 \frac{x}{4} \leq 1$$

$$3^{-1} \leq \frac{x}{4} \leq 3^1$$

$$\frac{1}{3} \leq \frac{x}{4} \leq 3$$

$$\frac{4}{3} \leq x \leq 12$$

domain of the function  $\Rightarrow x \in \left[ \frac{4}{3}, 12 \right]$

85. (C)  $f(x) = \begin{cases} \frac{e^x + 1}{e^x - 1}, & \text{when } x \neq 0 \\ 0, & \text{when } x = 0 \end{cases}$

$$\text{L. H. L.} = \lim_{x \rightarrow 0^-} f(x) = \lim_{h \rightarrow 0} f(0-h)$$

$$= \lim_{h \rightarrow 0} \frac{\frac{1}{e^{-h}} + 1}{\frac{1}{e^{-h}} - 1}$$

$$= \frac{e^{-\infty} + 1}{e^{-\infty} - 1}$$

$$= \frac{0+1}{0-1} = -1$$

$$\text{R.H.L.} = \lim_{x \rightarrow 0^+} f(x) = \lim_{h \rightarrow 0} f(0+h)$$

$$= \lim_{h \rightarrow 0} \frac{\frac{1}{e^h} + 1}{\frac{1}{e^h} - 1}$$

$$\begin{aligned}
 &1 + \frac{1}{e^h} \\
 &= \lim_{h \rightarrow 0} \frac{e^h}{e^h - 1} \\
 &= \frac{1+0}{1-0} = 1
 \end{aligned}$$

L.H.L.  $\neq$  R.H.L.

So  $f(x)$  is discontinuous at  $x = 0$

86. (C)  $f(x) = \begin{cases} px^2 - 3, & \text{if } x \leq 2 \\ -\frac{3}{2}x + 4p, & \text{if } x > 2 \end{cases}$

$$\text{L.H.D.} = \lim_{h \rightarrow 0} \frac{f(2-h) - f(2)}{-h}$$

$$= \lim_{h \rightarrow 0} \frac{(p(2-h)^2 - 3) - (4p-3)}{-h}$$

$$= \lim_{h \rightarrow 0} \frac{h(hp-4p)}{h}$$

$$= 0 - 4p = -4p$$

$$\text{R.H.D.} = \lim_{h \rightarrow 0} \frac{f(2+h) - f(2)}{h}$$

$$= \lim_{h \rightarrow 0} \frac{-\frac{3}{2}(2+h) + 4p - (4p-3)}{h}$$

$$= -\frac{3}{2}$$

$f(x)$  is derivable at  $x = 2$

So L.H.D. = R.H.D.

$$-ap = -\frac{3}{2}$$

$$p = \frac{3}{8}$$

87. (B) curve  $x^2 + y^2 - 2x - 9y + 20 = 0$   
equation of tangent at  $(x_1, y_1)$

$$xx_1 + yy_1 - (x + x_1) - \frac{9}{2}(y + y_1) + 20 = 0$$

here  $(x_1, y_1) = (2, 4)$

$$2x + 4y - (x + 2) - \frac{9}{2}(y + 4) + 20 = 0$$

$$2x + 4y - x - 2 - \frac{9}{2}y - 18 + 20 = 0$$

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$$x - \frac{y}{2} = 0$$

$$x = \frac{y}{2}$$

$$2x = y$$

$$2x - y = 0$$

88. (A)  $f(x) = 2x^3 - 3x^2 - 12x + 4$

on differentiating both side w.r.t. 'x'

$$f'(x) = 6x^2 - 6x - 12$$

again, differentiating both side w.r.t.'x'

$$f''(x) = 12x - 6 \quad \dots(\text{ii})$$

for maxima and minima

$$f'(x) = 0$$

$$6x^2 - 6x - 12 = 0$$

$$x^2 - x - 2 = 0$$

$$(x - 2)(x + 1) = 0$$

$$x = -1, 2$$

On putting  $x = -1$  in equation (ii)

$$f''(-1) = -12 - 6 = -18 \text{ (maxima)}$$

on putting  $x = 2$  in equation (ii)

$$f''(2) = 12 \times 2 - 6 = 18 \text{ (minima)}$$

Hence  $f(x)$  is maximum at  $x = -1$

89. (B) Given that  $|\vec{a}| = 20$ ,  $|\vec{b}| = 2$

$$\vec{a} \cdot \vec{b} = 24$$

$$\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$$

$$24 = 20 \times 2 \cos \theta$$

$$\cos \theta = \frac{3}{5}$$

$$|\vec{a} \times \vec{b}| = |\vec{a}| |\vec{b}| \sin \theta |\hat{n}|$$

$$= 20 \times 2 \times \frac{4}{5} \times 1$$

$$= 32$$

90. (B)

91. (B)  $\left(\frac{1-i}{1+i}\right)^3 - \left(\frac{1+i}{1-i}\right)^3 = x + iy$

$$\Rightarrow \frac{[(1-i)^2]^3 - [(1+i)^2]^3}{[(1+i)(1-i)]^3} = x + iy$$

$$\Rightarrow \frac{(-2i)^3 - (2i)^3}{2^3} = x + iy$$

$$\Rightarrow \frac{8i + 8i}{8} = x + iy$$

$$\Rightarrow \frac{16i}{8} = x + iy$$

$$\Rightarrow 2i = x + iy$$

$$x = 0, y = 2$$

$$\text{then } x - y = -2$$

92. (A)  $i^{15} + 3i^{17} + 3i^{35} - 4i^{39} - 6i^{44}$

$$= i^3 + 3i + 3i^3 - 4i^3 - 6$$

$$= -i + 3i - 3i + 4i - 6$$

$$= 3i - 6$$

93. (B) time is 8 : 35

formula

$$\text{angle } (\theta) = \left| \frac{11M - 60H}{2} \right| \text{ Where M = Minute}$$

$$H = \text{hour}$$

$$= \left| \frac{11 \times 35 - 60 \times 8}{2} \right|$$

$$= \left| \frac{385 - 480}{2} \right|$$

$$= \frac{95}{2} = \left( 47 \frac{1}{2} \right)^\circ$$

94. (D) Sine Rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} = k$$

$$a = k \sin A, b = k \sin B, c = k \sin C$$

$$\frac{b^2 - c^2}{a^2} = \frac{k^2 \sin^2 B - k^2 \sin^2 C}{k^2 \sin^2 A}$$

$$= \frac{\sin^2 B - \sin^2 C}{\sin^2 A}$$

$$= \frac{\sin(B+C) \sin(B-C)}{\sin^2(\pi - (B+C))}$$

$$= \frac{\sin(B+C) \sin(B-C)}{\sin^2(B+C)}$$

$$= \frac{\sin(B-C)}{\sin(B+C)}$$

95. (C) We know that  $\cos A = \frac{b^2 + c^2 - a^2}{2bc}$

$$\cos B = \frac{c^2 + a^2 - b^2}{2ca}, \cos C = \frac{a^2 + b^2 - c^2}{2ab}$$

then

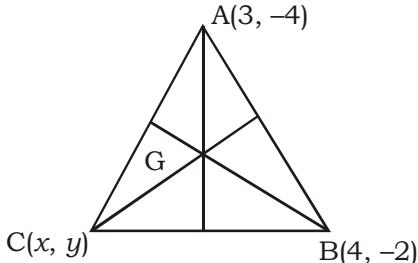
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$$\begin{aligned} \frac{\cos A}{a} + \frac{\cos B}{b} + \frac{\cos C}{c} \\ = \frac{b^2 + c^2 - a^2}{2abc} + \frac{c^2 + a^2 - b^2}{2abc} + \frac{a^2 + b^2 - c^2}{2abc} \\ = \frac{a^2 + b^2 + c^2}{2abc} \end{aligned}$$

96. (B)  $\tan 10^\circ \tan 30^\circ \tan 50^\circ \tan 70^\circ$   
 $\Rightarrow \tan 30^\circ (\tan 10^\circ \tan 50^\circ \tan 70^\circ)$   
 $\Rightarrow \tan 30^\circ \times \tan 30^\circ$   
 $[\because \tan \theta \tan (60^\circ - \theta) \tan (60^\circ + \theta) = \tan 30^\circ]$   
 $\Rightarrow \frac{1}{\sqrt{3}} \times \frac{1}{\sqrt{3}} = \frac{1}{3}$

97. (A)



Let third vertex of the triangle =  $(x, y)$   
given  $G(3, -2)$

Co-ordinate of centroid

$$3 = \frac{x+3+4}{3} \text{ and } -2 = \frac{y-4-2}{3}$$

$$9 = x+7 \quad -6 = y-6$$

$$x=2 \quad \text{and} \quad y=0$$

third vertex  $C(x, y) = (2, 0)$

98. (C) Points  $(1, 2)$ ,  $(5, -3)$  and  $(3, -\lambda)$   
these points lie on the straight line,  
then

$$\begin{vmatrix} 1 & 2 & 1 \\ 5 & -3 & 1 \\ 3 & -\lambda & 1 \end{vmatrix} = 0$$

$$1(-3+\lambda) - 2(5-3) + 1(-5\lambda+9) = 0$$

$$\lambda = \frac{1}{2}$$

99. (B) In point  $(x, y)$ ,  $x$  can positive or negative  
but distance never negative.

So perpendicular distance from the  $y$ -axis  
 $= |x|$

100. (C) Parabola

$$(y+2)^2 = 16(x-3)$$

$$\begin{aligned} Y^2 = 16X &\quad \text{where } X = x-3 \\ 4a = 16 &\quad Y = y+2 \\ a = 4 & \end{aligned}$$

$$\begin{aligned} \text{parameter } X = at^2 &\quad \text{and } Y = 2at \\ x-3 = 4t^2 &\quad y+2 = 2 \times 4 \times t \\ x = 4t^2 + 3 &\quad y = 8t-2 \\ \text{parameter } (4t^2 + 3, 8t-2) & \end{aligned}$$

101. (B) ellipse  $\frac{x^2}{4} + \frac{y^2}{9} = 1$  ... (i)

and circle  $x^2 + y^2 = 4$   
 $x^2 = 4 - y^2$  ... (ii)

On solving equation (i) and (ii)

$$y = 0, x = \pm 2$$

point  $(2, 0)$  and  $(-2, 0)$

Thus ellipse and circle intersect at two points.

102. (C) Given that  $\frac{x^2}{16} + \frac{y^2}{9} = 1$

We know that

**The locus of the point of intersection of two perpendicular tangents drawn on the ellipse is  $x^2 + y^2 = a^2 + b^2$ .**

$$\text{then } x^2 + y^2 = 16 + 9$$

$$x^2 + y^2 = 25$$

Which is director circle.

103. (C) 3, 9, 27, 81

$$\begin{aligned} \text{G.M.} &= (3 \times 9 \times 27 \times 81)^{1/4} \\ &= (3^1 \times 3^2 \times 3^3 \times 3^4)^{1/4} \\ &= (3^{10})^{1/4} \\ &= 3^{5/2} \\ &= \sqrt{243} = 9\sqrt{3} \end{aligned}$$

104. (B) Given that

$$\Sigma x_i = 12, \Sigma y_i = 36, \Sigma x_i y_i = 112 \text{ and } n = 5$$

We know that

$$\begin{aligned} \text{cov}(x, y) &= \frac{\sum x_i y_i}{n} - \frac{\sum x_i \sum y_i}{n^2} \\ &= \frac{112}{5} - \frac{12 \times 36}{25} \\ &= \frac{560 - 432}{25} \\ &= \frac{128}{25} = 5.12 \end{aligned}$$

105. (B) The value of  $\sin \theta$  lies between -1 and 1.

The value of ' $\cos \theta$ ' lies between -1 and 1.

106. (B)  $2 \sin^2 x = 1$

$$\sin^2 x = \frac{1}{2}$$

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$$\sin^2 x = \sin^2 \frac{\pi}{4}$$

$$\text{then } x = n\pi \pm \frac{\pi}{4}$$

107. (A)  $5\theta = 90$

$$2\theta + 3\theta = 90$$

$$2\theta = (90 - 3\theta)$$

$$\cos 2\theta = \cos (90 - 3\theta)$$

$$1 - 2 \sin^2 \theta = \sin 3\theta$$

$$1 - 2 \sin^2 \theta = 3 \sin \theta - 4 \sin^3 \theta$$

$$4 \sin^3 \theta - 2 \sin^2 \theta - 3 \sin \theta + 1 = 0$$

$$(\sin \theta - 1)(4 \sin^2 \theta + 2 \sin \theta - 1) = 0$$

$$\sin \theta - 1 \neq 0$$

$$\text{because } \theta \neq 90^\circ$$

$$4 \sin^2 \theta + 2 \sin \theta - 1 = 0$$

$$\sin \theta = \frac{-2 \pm \sqrt{(2)^2 - 4 \times 4 \times (-1)}}{2 \times 4}$$

$$\sin \theta = \frac{-2 \pm \sqrt{20}}{8}$$

$$\sin \theta = \frac{-2 \pm 2\sqrt{5}}{8}$$

$$\sin \theta = \frac{-1 \pm \sqrt{5}}{4}$$

$$\text{here } \theta = 18^\circ$$

$$\sin 18^\circ = \frac{\sqrt{5} - 1}{4}$$

because  $\sin x \geq 0$  between  $\left[0, \frac{\pi}{2}\right]$

108. (A)  $\int_0^2 x^m (2-x)^n dx = k \int_0^2 x^n (2-x)^m dx$

$$\text{Property } \int_0^a f(x) dx = \int_0^a f(a-x) dx$$

$$\int_0^2 (2-x)^m x^n dx = k \int_0^2 x^n (2-x)^m dx$$

$$k = 1$$

109. (A) Given that

$$\int_{-1}^2 f(x) dx = \frac{7}{5} \text{ and } \int_{-1}^4 f(x) dx = \frac{4}{3}$$

$$\int_{-1}^2 f(x) dx + \int_2^4 f(x) dx = \int_{-1}^4 f(x) dx$$

$$\frac{7}{5} + \int_2^4 f(x) dx = \frac{4}{3}$$

$$\int_2^4 f(x) dx = \frac{4}{3} - \frac{7}{5}$$

$$= \frac{-1}{15}$$

(110-112) :

110. (B)  $I = \int \frac{1}{(x+x^6)} dx$

$$I = \int \frac{1}{x(x+x^5)} dx$$

$$I = \int \frac{x^4}{x^5(1+x^5)} dx$$

$$\text{Let } x^5 = t$$

$$5x^4 dx = dt$$

$$x^4 dx = \frac{1}{5} dt$$

$$I = \frac{1}{5} \int \frac{1}{t(1+t)} dt$$

$$I = \frac{1}{5} \int \left[ \frac{1}{t} - \frac{1}{1+t} \right] dx$$

$$I = \frac{1}{5} [\log t - \log (1+t)] + c$$

$$I = \frac{1}{5} \left[ \log \frac{t}{1+t} \right] + c$$

$$I = \frac{1}{5} \log \left[ \frac{x^5}{1+x^5} \right] + c$$

$$f(x) = \frac{1}{5} \log \left[ \frac{x^5}{1+x^5} \right]$$

111. (B)  $I = \int \frac{x^5}{x+x^6} dx = \int \frac{x^5+1-1}{(1+x^5)} dx$

$$I = \int \left( \frac{1}{x} - \frac{1}{x+x^6} \right) dx$$

$$= \log x - f(x) + c$$

112. (B)  $\int \frac{\sin x}{\cos x + \cos^6 x} dx$

$$\text{Let } \cos x = t$$

$$-\sin x dx = dt$$

$$\sin x dx = -dt$$

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$$\Rightarrow \int \frac{-dt}{t+t^6}$$

$$\Rightarrow -\int \frac{1}{t+t^6} dt$$

$$\Rightarrow -f(t) + c$$

$$\Rightarrow -f(\cos x) + c$$

113. (C) Let  $y = \sqrt{10 + 3\sqrt{10 + 3\sqrt{10 + \dots}}}$

$$y = \sqrt{10 + 3y}$$

$$y^2 = 10 + 3y$$

$$y^2 - 3y - 10 = 0$$

$$(y-5)(y+2) = 0$$

$$y = 5, -2$$

then the value of expression = 5

**(114-116) :**

114. (B) equation

$$3x^2 + 5x + 4 = 0$$

**sum of the roots  $\alpha + \beta = \frac{-5}{3}$**

product of the root  $\alpha.\beta = \frac{4}{3}$

115. (C)  $\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta$

$$= \left(\frac{-5}{3}\right)^2 - 2 \times \frac{4}{3}$$

$$= \frac{25}{9} - \frac{8}{3}$$

$$= \frac{1}{9}$$

116. (A) sum of the roots =  $\frac{1}{\alpha} + \frac{1}{\beta}$

$$= \frac{\alpha + \beta}{\alpha\beta}$$

$$= \frac{\frac{-5}{3}}{\frac{4}{3}}$$

$$= -\frac{5}{4}$$

product of the roots =  $\frac{1}{\alpha} \times \frac{1}{\beta}$

$$= \frac{1}{4} \cdot \frac{3}{3}$$

$$= \frac{3}{4}$$

equation

$x^2 - (\text{sum of the roots})x + \text{Product of the Roots} = 0$

$$x^2 + \frac{5}{4}x + \frac{3}{4} = 0$$

$$4x^2 + 5x + 3 = 0$$

117. (A)  $\tan^{-1} \frac{x}{y} + \tan^{-1} \left( \frac{x+y}{x-y} \right)$

$$\Rightarrow \tan^{-1} \left[ \frac{\frac{x}{y} + \frac{x+y}{x-y}}{1 - \frac{x}{y} \times \frac{x+y}{x-y}} \right]$$

$$\Rightarrow \tan^{-1} \left( \frac{x^2 + y^2}{-(x^2 + y^2)} \right)$$

$$\Rightarrow \tan^{-1} (-1)$$

$$\Rightarrow \tan^{-1} \left[ \tan \left( -\frac{\pi}{4} \right) \right]$$

$$\Rightarrow -\frac{\pi}{4}$$

118. (A)  $2 \tan^{-1} \left( \frac{1}{3} \right) + \tan^{-1} \left( \frac{1}{7} \right)$

$$\Rightarrow \tan^{-1} \left( \frac{\frac{2}{3}}{1 - \frac{1}{9}} \right) + \tan^{-1} \left( \frac{1}{7} \right)$$

$$\Rightarrow \tan^{-1} \frac{3}{4} + \tan^{-1} \left( \frac{1}{7} \right)$$

$$\Rightarrow \tan^{-1} \left[ \frac{\frac{3}{4} + \frac{1}{7}}{1 - \frac{3}{4} \times \frac{1}{7}} \right]$$

$$\Rightarrow \tan^{-1} \left[ \frac{25}{28} \right]$$

$$\Rightarrow \tan^{-1} (1)$$


  
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$$\Rightarrow \frac{\pi}{4}$$

$$\Rightarrow \frac{1}{\sin^2 15^\circ + \sin^2 45^\circ + \sin 15^\circ \cdot \sin 45^\circ}$$

Assertion (A) is true.

Reason (R) is also true and R is cor  
explanation of A.

119. (B)

$$\begin{array}{r}
 10001 \\
 11001 \\
 1101 \\
 110 \\
 \hline
 10 \\
 \hline
 11111
 \end{array}$$

$$\Rightarrow \frac{1}{\left(\frac{\sqrt{3}-1}{2\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2 + \frac{\sqrt{3}-1}{2\sqrt{2}} \times \frac{1}{\sqrt{2}}}$$

$$\Rightarrow \frac{1}{\frac{4-2\sqrt{3}}{8} + \frac{1}{2} + \frac{\sqrt{3}-1}{4}}$$

120. (B)

$$\frac{\sin 15^\circ - \sin 45^\circ}{\sin^3 15^\circ - \sin^3 45^\circ}$$

$$\Rightarrow \frac{8}{4 - 2\sqrt{3} + 4 + 2\sqrt{3} - 2}$$

$$\Rightarrow \frac{\sin 15^\circ - \sin 45^\circ}{(\sin 15^\circ - \sin 45^\circ)(\sin^2 15^\circ + \sin^2 45^\circ + \sin 15^\circ \cdot \sin 45^\circ)}$$

$$\Rightarrow \frac{8}{6} = \frac{4}{3}$$

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2007, OUTRAM LINES, 1ST FLOOR, OPPOSITE MUKHERJEE NAGAR POLICE STATION, DELHI-110009

**NDA (MATHS) MOCK TEST - 76 (Answer Key)**

- |         |         |         |         |          |          |
|---------|---------|---------|---------|----------|----------|
| 1. (B)  | 21. (A) | 41. (D) | 61. (C) | 81. (D)  | 101. (B) |
| 2. (C)  | 22. (A) | 42. (B) | 62. (B) | 82. (B)  | 102. (C) |
| 3. (D)  | 23. (B) | 43. (D) | 63. (C) | 83. (B)  | 103. (C) |
| 4. (A)  | 24. (A) | 44. (C) | 64. (D) | 84. (B)  | 104. (B) |
| 5. (D)  | 25. (D) | 45. (C) | 65. (A) | 85. (C)  | 105. (B) |
| 6. (C)  | 26. (C) | 46. (A) | 66. (B) | 86. (C)  | 106. (B) |
| 7. (B)  | 27. (B) | 47. (D) | 67. (C) | 87. (B)  | 107. (A) |
| 8. (A)  | 28. (B) | 48. (A) | 68. (B) | 88. (A)  | 108. (A) |
| 9. (B)  | 29. (C) | 49. (C) | 69. (C) | 89. (B)  | 109. (A) |
| 10. (D) | 30. (A) | 50. (D) | 70. (B) | 90. (B)  | 110. (B) |
| 11. (C) | 31. (B) | 51. (B) | 71. (C) | 91. (B)  | 111. (B) |
| 12. (C) | 32. (B) | 52. (A) | 72. (D) | 92. (A)  | 112. (B) |
| 13. (A) | 33. (A) | 53. (B) | 73. (A) | 93. (B)  | 113. (C) |
| 14. (B) | 34. (A) | 54. (A) | 74. (C) | 94. (D)  | 114. (B) |
| 15. (C) | 35. (B) | 55. (C) | 75. (C) | 95. (C)  | 115. (C) |
| 16. (D) | 36. (C) | 56. (B) | 76. (D) | 96. (B)  | 116. (A) |
| 17. (B) | 37. (A) | 57. (A) | 77. (B) | 97. (A)  | 117. (A) |
| 18. (C) | 38. (A) | 58. (B) | 78. (B) | 98. (C)  | 118. (A) |
| 19. (B) | 39. (C) | 59. (D) | 79. (D) | 99. (B)  | 119. (B) |
| 20. (C) | 40. (B) | 60. (C) | 80. (A) | 100. (C) | 120. (B) |

**Note :** If your opinion differ regarding any answer, please message the mock test and Question number to 8860330003

**Note :** If you face any problem regarding result or marks scored, please contact : 9313111777

**Note :** Whatsapp with Mock Test No. and Question No. at 705360571 for any of the doubts. Join the group and you may also share your suggestions and experience of Sunday Mock Test.